Lecture 7: Recurrent Neural Networks

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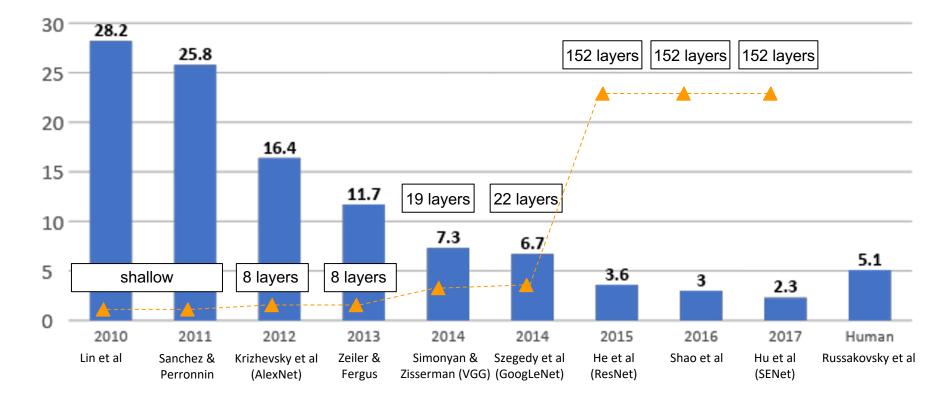
Lecture 8 - 1

Training "Feedforward" Neural Networks

- **1. One time setup:** activation functions, preprocessing, weight initialization, regularization, gradient checking
- **2. Training dynamics:** babysitting the learning process, parameter updates, hyperparameter optimization
- **3. Evaluation:** model ensembles, test-time augmentation, transfer learning

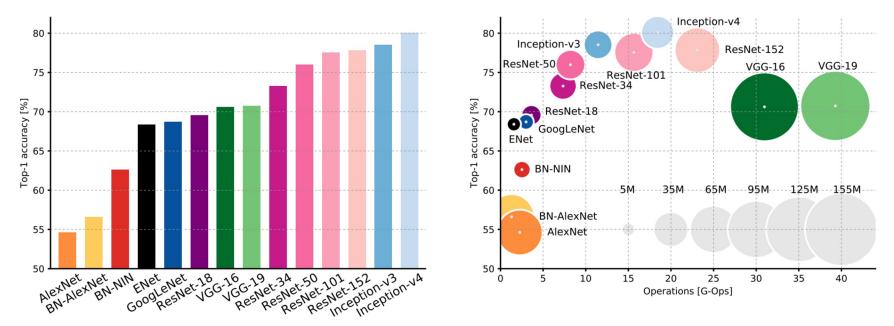
<u>Lecture 8</u> - 2 April 23, 2023

ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners



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Lecture 8 - 3

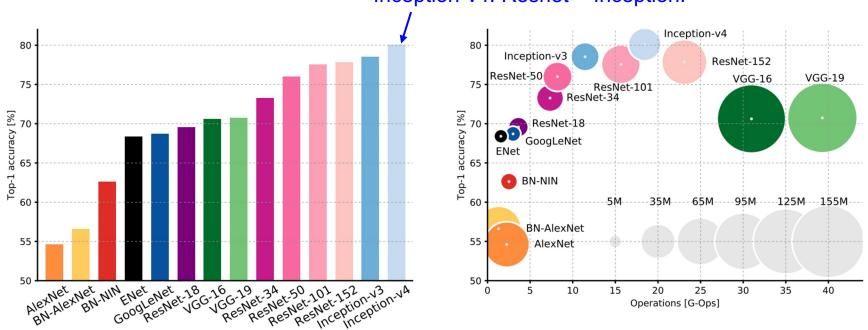


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Lecture 8 - 4



Comparing complexity... Inception-v4: Resnet + Inception!

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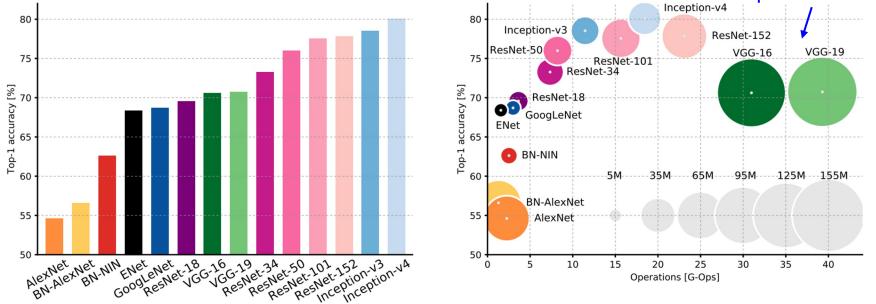
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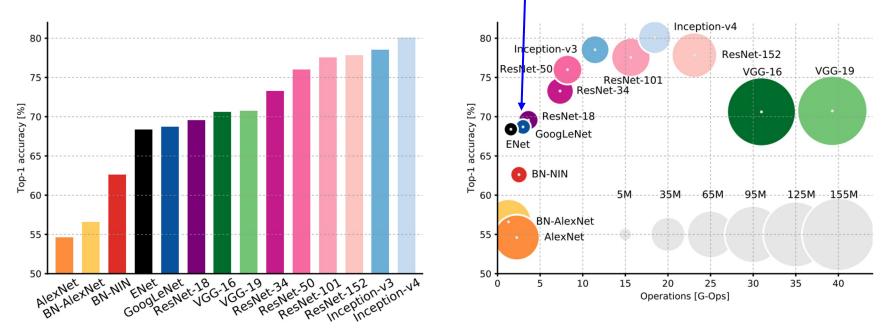


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GoogLeNet:

Lecture 8 -

7

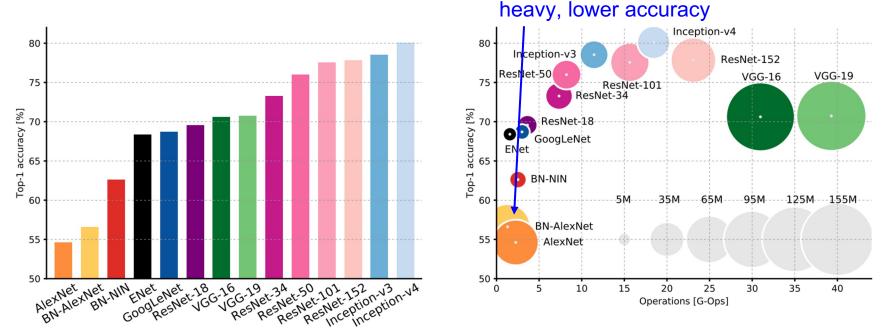
most efficient

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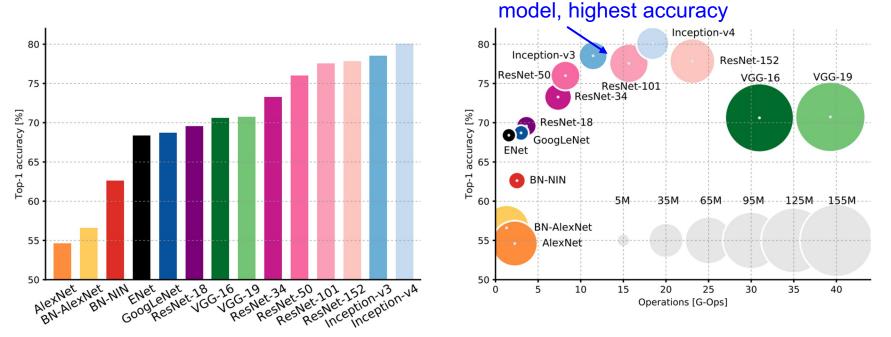
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AlexNet:

Smaller compute, still memory



ResNet:

Moderate efficiency depending on

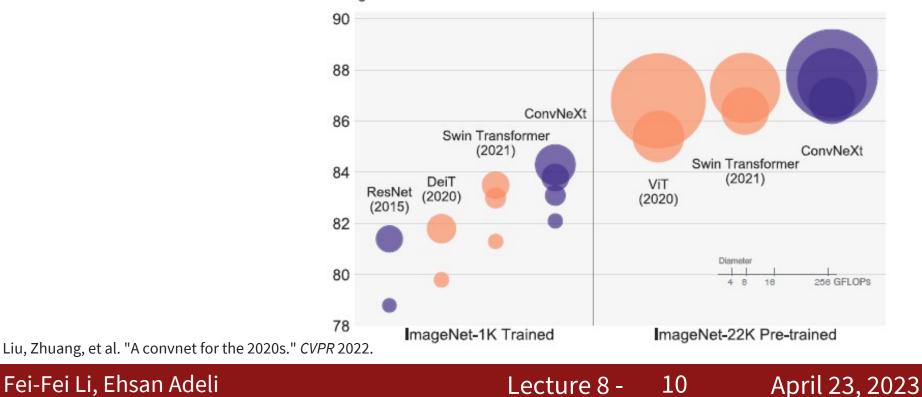
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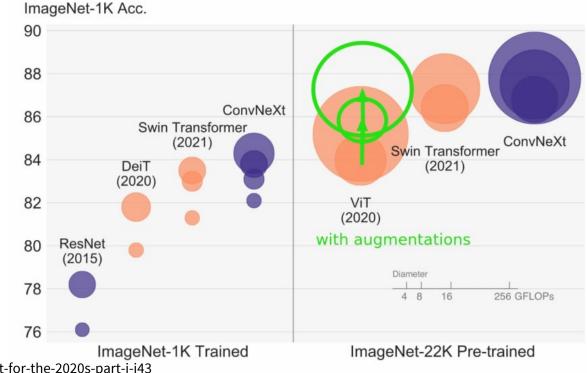
More complexity...



mageNet-1K Acc

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More complexity...

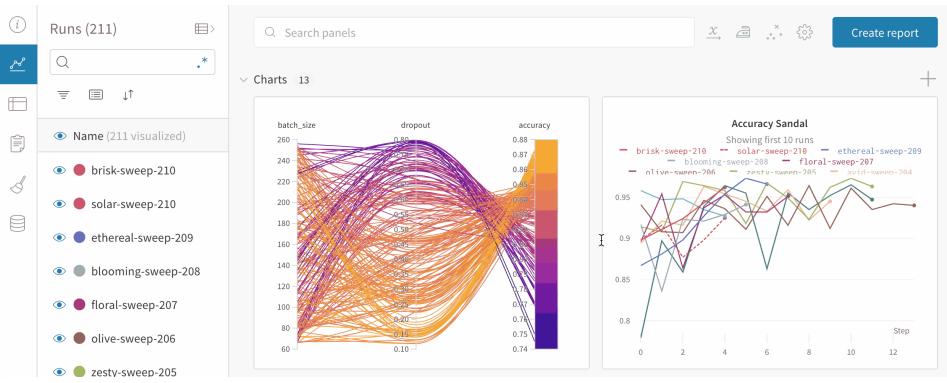


https://dev.to/rohitgupta24/convnext-a-convnet-for-the-2020s-part-i-i43

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Lecture 8 - 11

Evaluate models and tune hyperparameters



https://docs.wandb.ai/guides/track/app

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Lecture 8 - 12

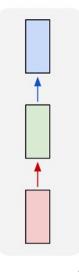
Today: Recurrent Neural Networks

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"Vanilla" Neural Network

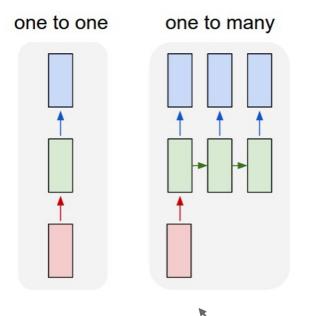
one to one



📏 Vanilla Neural Networks

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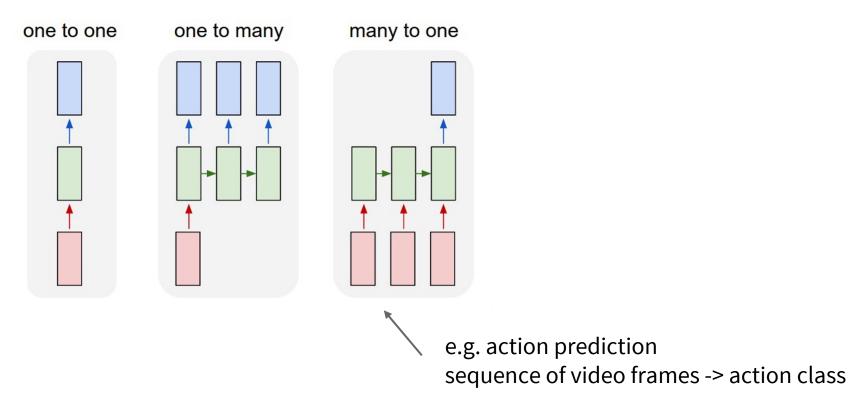
Lecture 8 - 14



e.g. Image Captioning image -> sequence of words

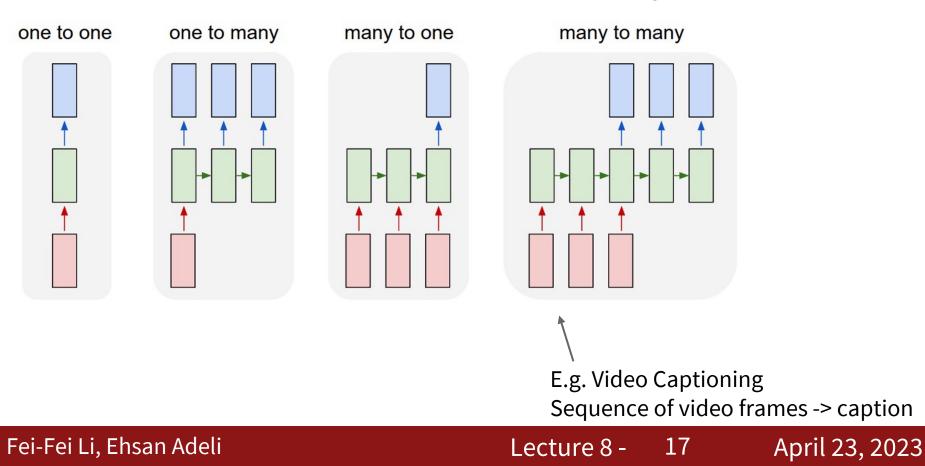
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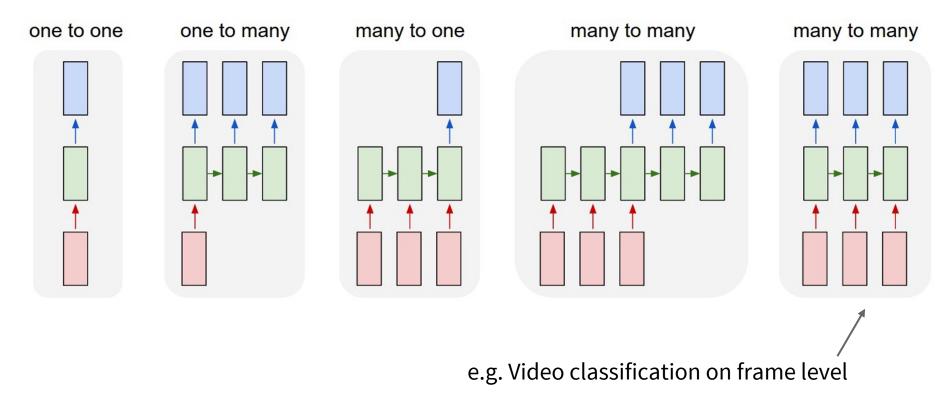
Lecture 8 - 15



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Lecture 8 - 16

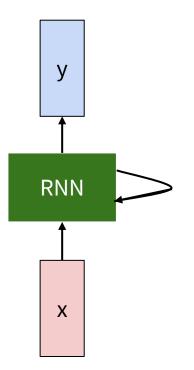




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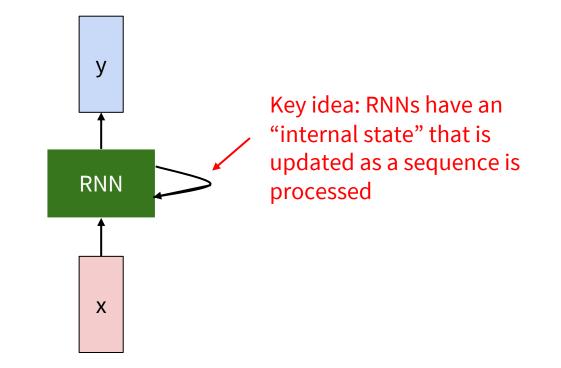
Recurrent Neural Network



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Lecture 8 - 21

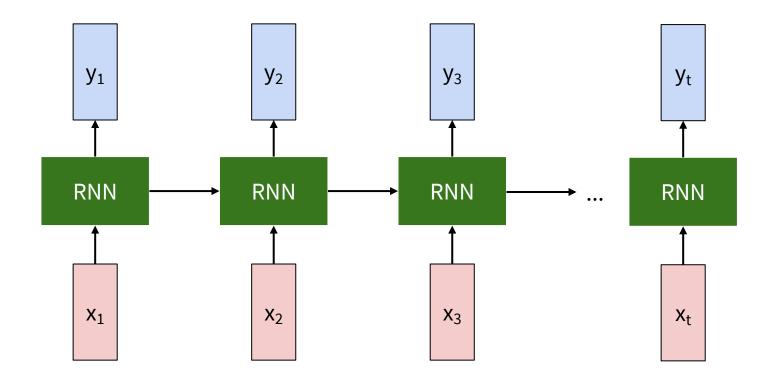
Recurrent Neural Network



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Lecture 8 - 22

Unrolled RNN

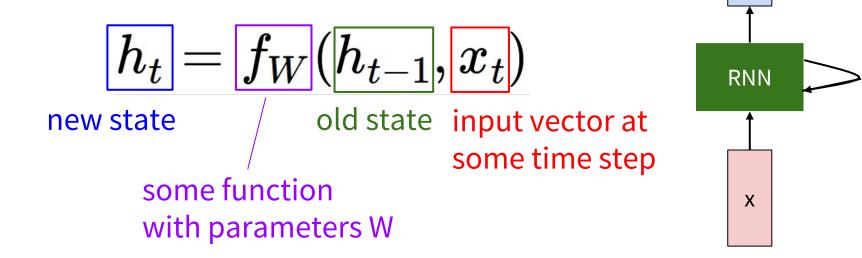


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Lecture 8 - 23 Apri

RNN hidden state update

We can process a sequence of vectors x by applying a recurrence formula at every time step:



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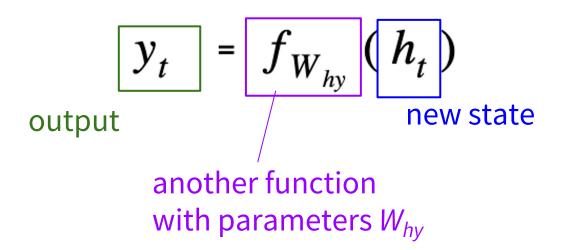
Lecture 8 - 24 Ap

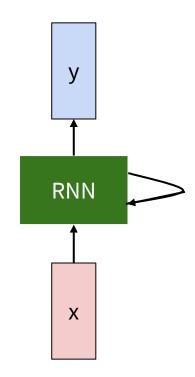
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y

RNN output generation

We can process a sequence of vectors x by applying a recurrence formula at every time step:

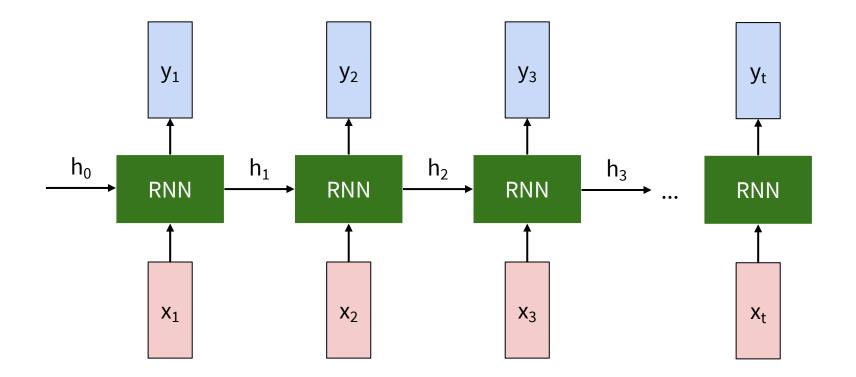




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Recurrent Neural Network



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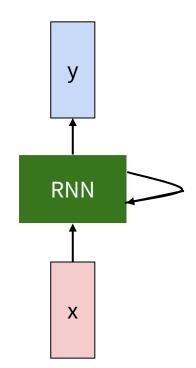
Lecture 8 - 26 Apr

Recurrent Neural Network

We can process a sequence of vectors x by applying a recurrence formula at every time step:

$$h_t = f_W(h_{t-1}, x_t)$$

Notice: the same function and the same set of parameters are used at every time step.

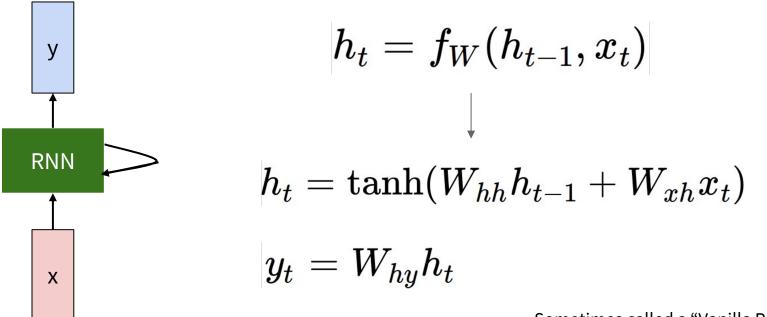


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(Vanilla) Recurrent Neural Network

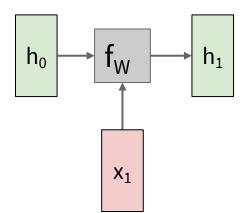
The state consists of a single "hidden" vector h:



Sometimes called a "Vanilla RNN" or an "Elman RNN" after Prof. Jeffrey Elman

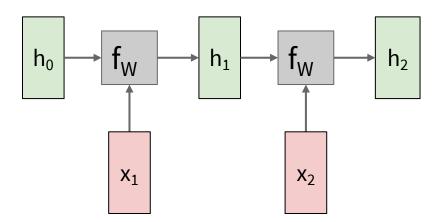
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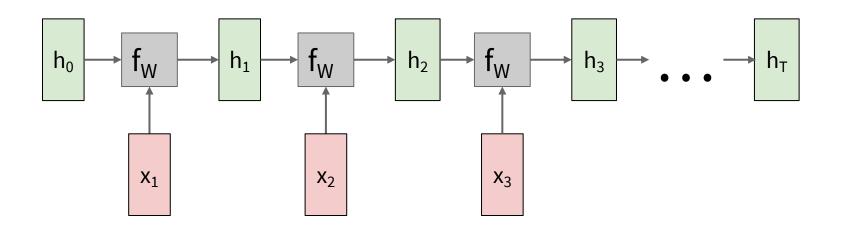
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Lecture 8 - 29



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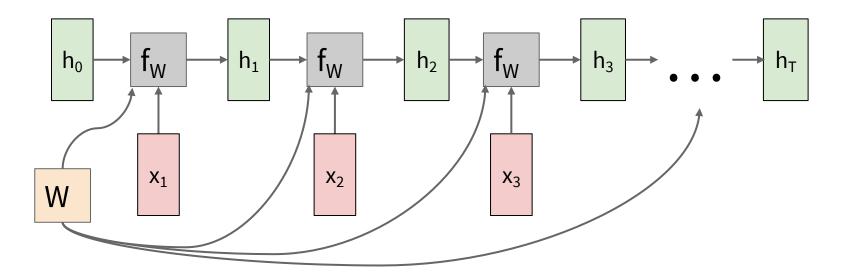
Lecture 8 - 30



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Lecture 8 - 31 A

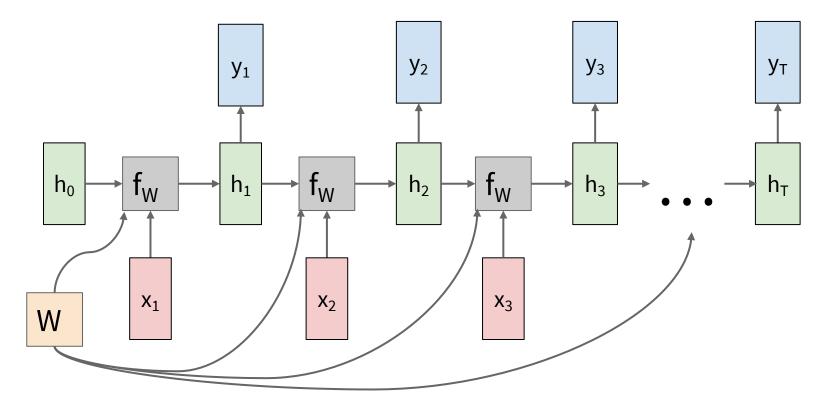
Re-use the same weight matrix at every time-step



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Lecture 8 - 32

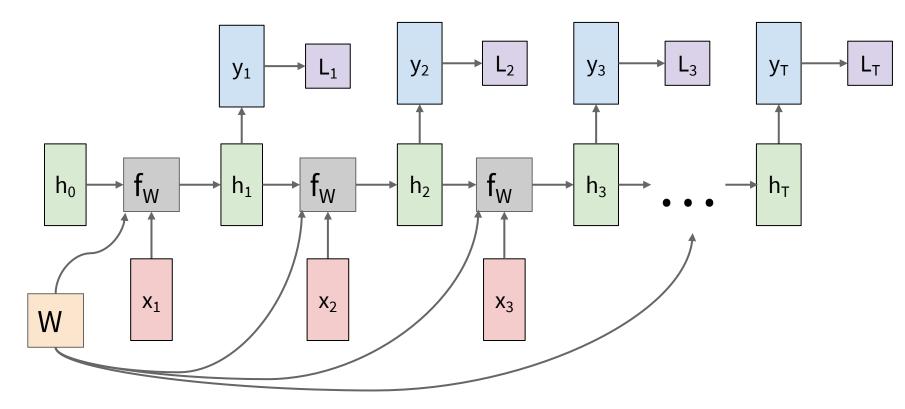
RNN: Computational Graph: Many to Many



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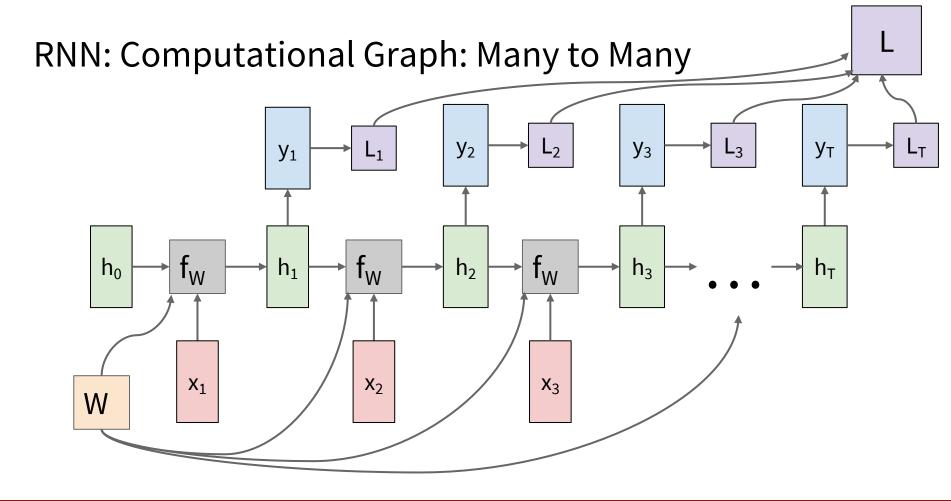
Lecture 8 - 33

RNN: Computational Graph: Many to Many



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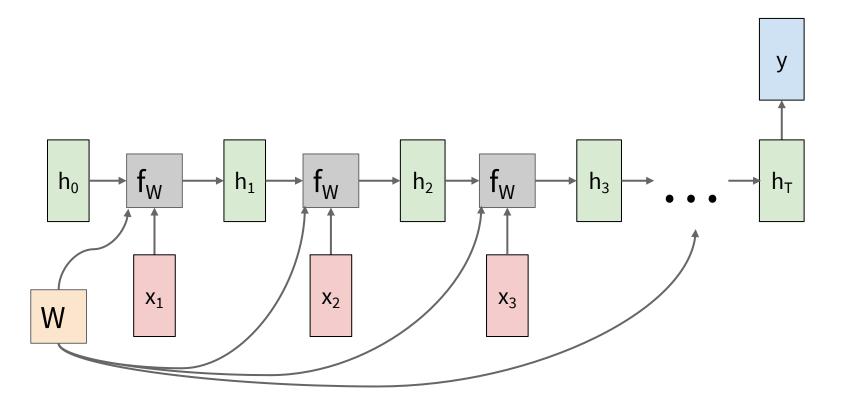
Lecture 8 - 34



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Lecture 8 - 35

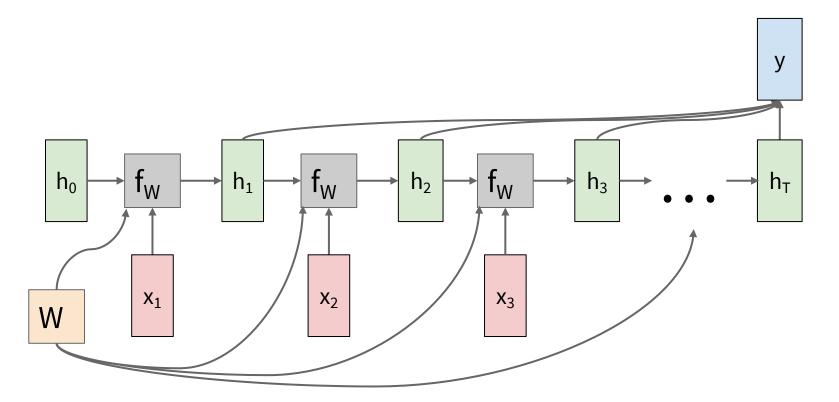
RNN: Computational Graph: Many to One



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Lecture 8 - 36

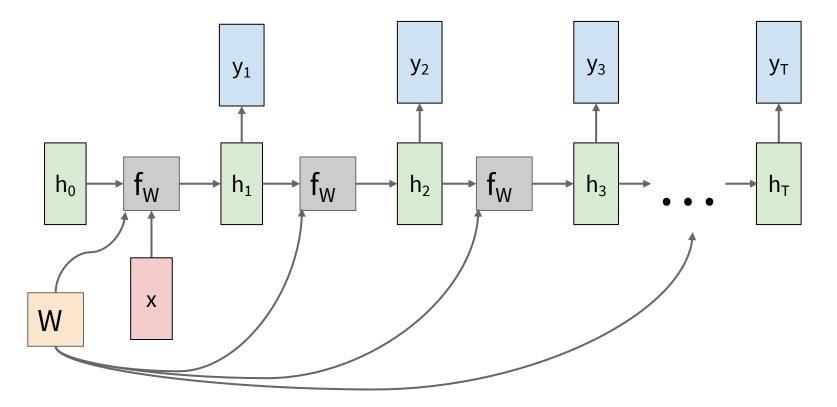
RNN: Computational Graph: Many to One



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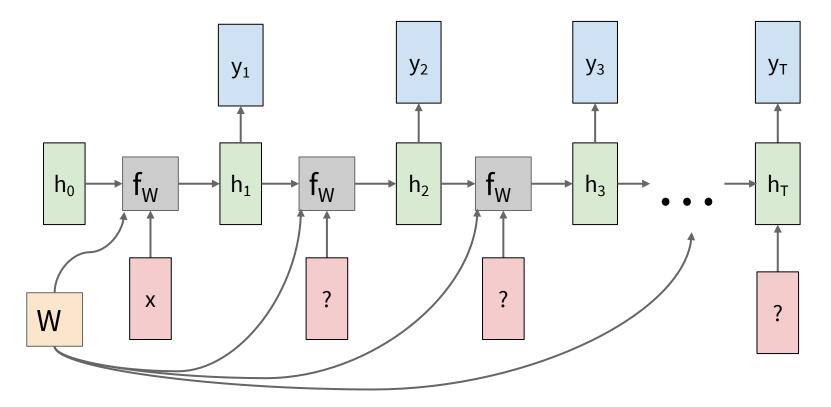
RNN: Computational Graph: One to Many



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Lecture 8 - 38

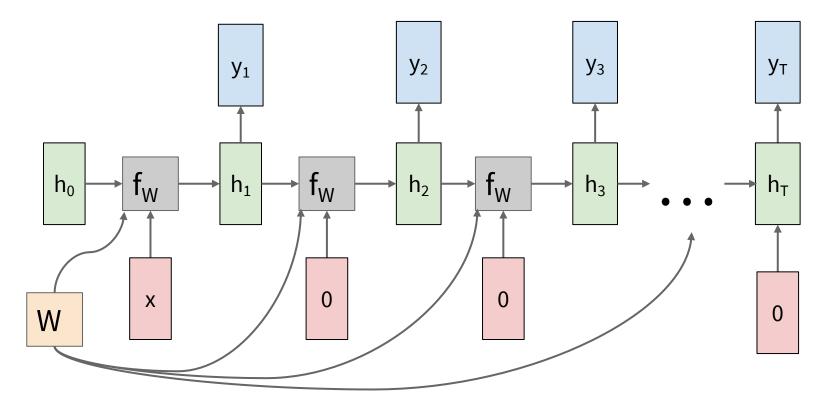
RNN: Computational Graph: One to Many



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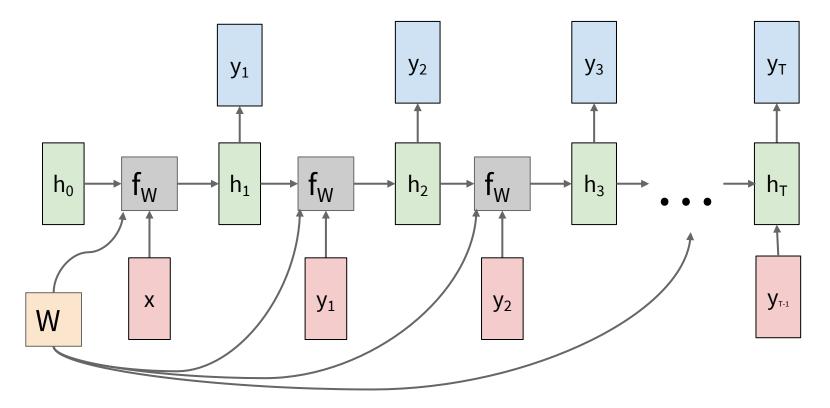
RNN: Computational Graph: One to Many



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RNN: Computational Graph: One to Many

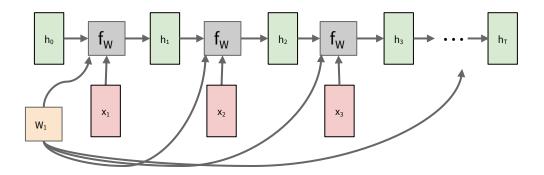


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Lecture 8 - 41

Sequence to Sequence: Many-to-one + one-to-many

Many to one: Encode input sequence in a single vector



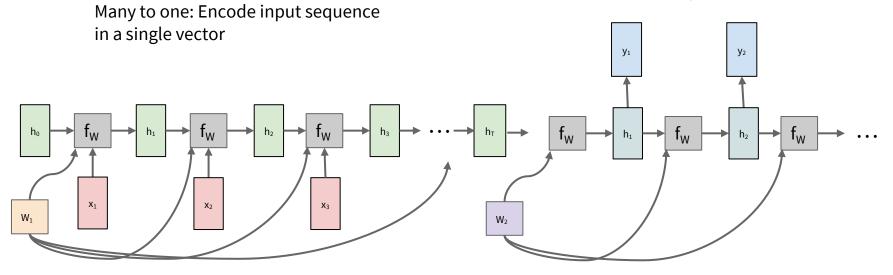
Sutskever et al, "Sequence to Sequence Learning with Neural Networks", NIPS 2014

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Sequence to Sequence: Many-to-one + one-to-many

One to many: Produce output sequence from single input vector



Sutskever et al, "Sequence to Sequence Learning with Neural Networks", NIPS 2014

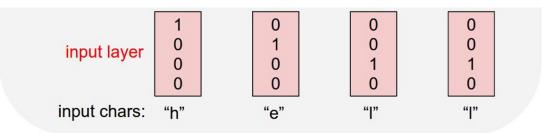
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Example: Character-level **Language Model**

Vocabulary: [h,e,l,o]

Example training sequence: "hello"



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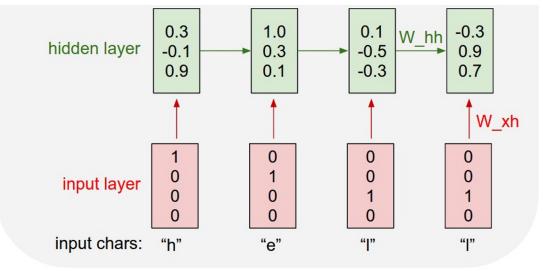
Lecture 8 - 44

Example: Character-level Language Model

Vocabulary: [h,e,l,o]

Example training sequence: "hello"

$$h_t = anh(W_{hh}h_{t-1} + W_{xh}x_t)$$



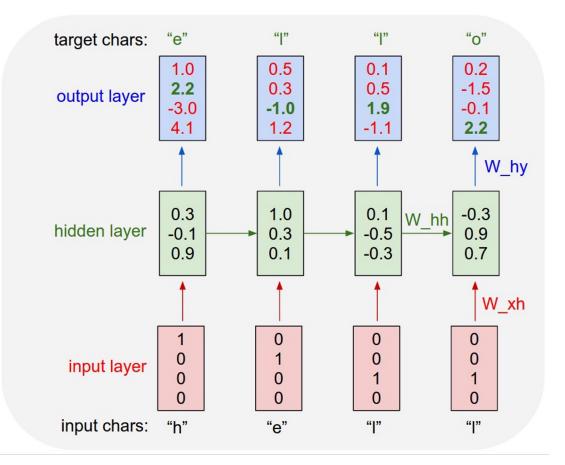
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Example: Character-level Language Model

Vocabulary: [h,e,l,o]

Example training sequence: "hello"

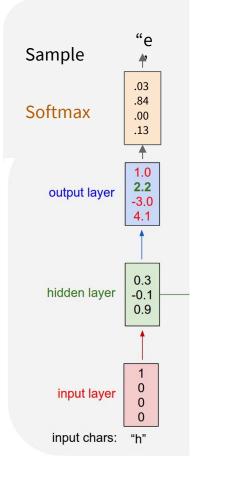


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Lecture 8 - 46

Vocabulary: [h,e,l,o]

At test-time sample characters one at a time, feed back to model

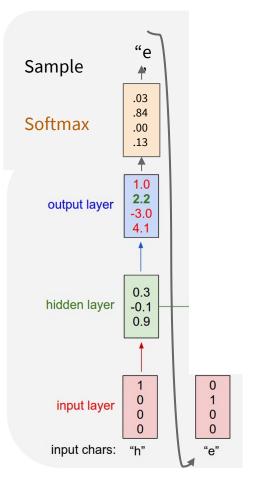


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Lecture 8 - 47

Vocabulary: [h,e,l,o]

At test-time sample characters one at a time, feed back to model

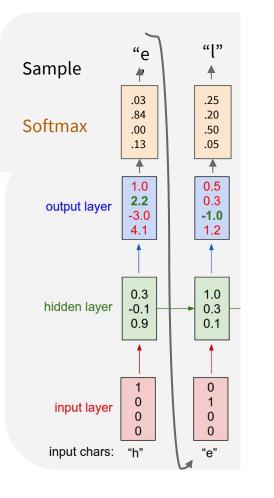


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Lecture 8 - 48

Vocabulary: [h,e,l,o]

At test-time sample characters one at a time, feed back to model

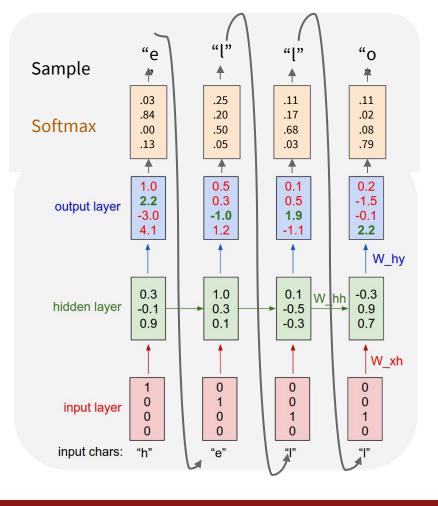


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Lecture 8 - 49

Vocabulary: [h,e,l,o]

At test-time sample characters one at a time, feed back to model

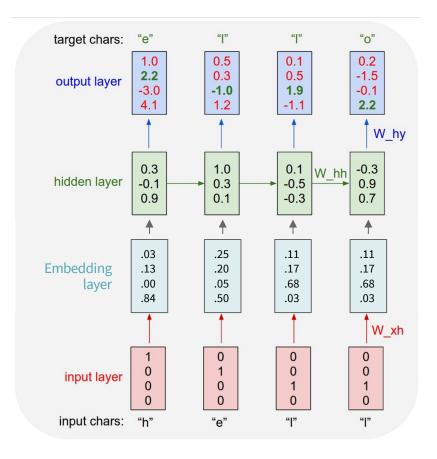


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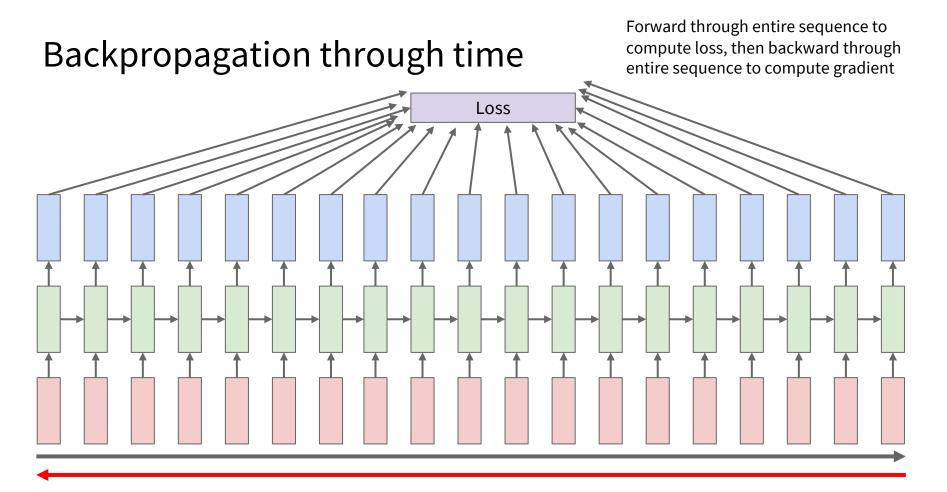
$$\begin{bmatrix} w_{11} & w_{12} & w_{13} & w_{14} \end{bmatrix} \begin{bmatrix} 1 \\ w_{11} \end{bmatrix} \begin{bmatrix} w_{11} \\ w_{21} & w_{22} & w_{23} & w_{14} \end{bmatrix} \begin{bmatrix} 0 \\ 0 \end{bmatrix} = \begin{bmatrix} w_{21} \\ w_{31} & w_{32} & w_{33} & w_{14} \end{bmatrix} \begin{bmatrix} 0 \\ w_{31} \end{bmatrix} \begin{bmatrix} w_{31} \\ w_{41} & w_{42} & w_{43} & w_{44} \end{bmatrix} \begin{bmatrix} 0 \\ 0 \end{bmatrix} \begin{bmatrix} w_{41} \end{bmatrix}$$

Matrix multiplication with a one-hot vector just extracts a column from the weight matrix. We often put a separate embedding layer between the input and hidden layers.



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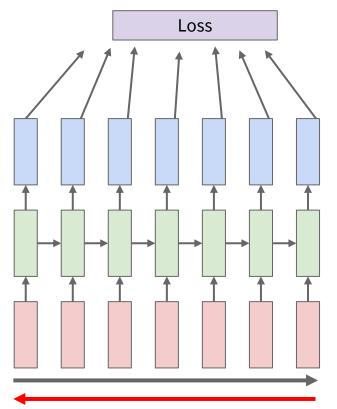
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Lecture 8 - 52 A

Truncated Backpropagation through time

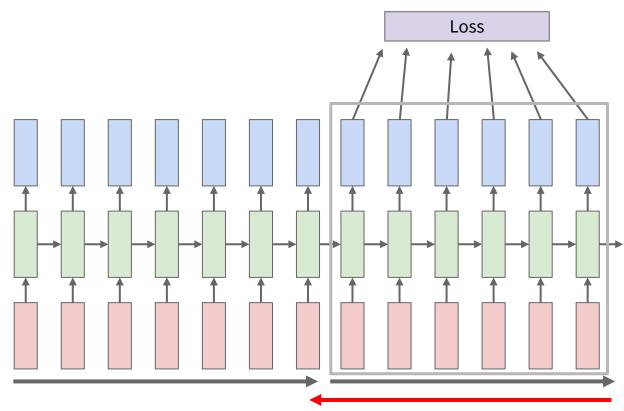


Run forward and backward through chunks of the sequence instead of whole sequence

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Truncated Backpropagation through time

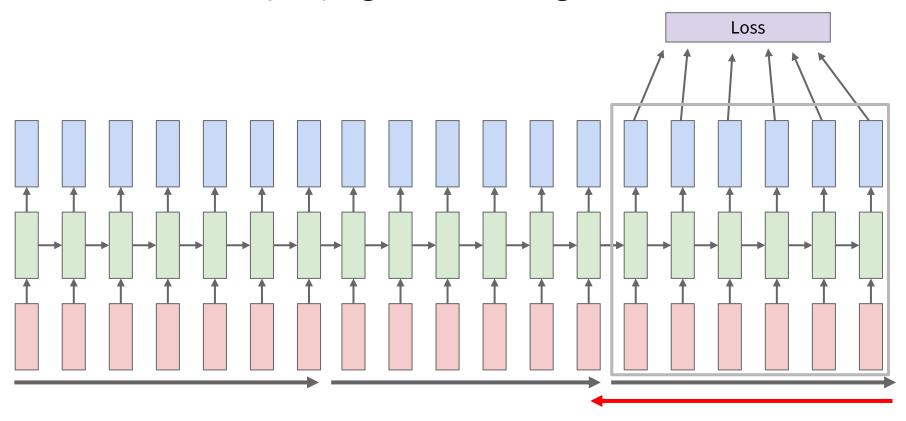


Carry hidden states forward in time forever, but only backpropagate for some smaller number of steps

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Truncated Backpropagation through time



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Lecture 8 - 55

min-char-rnn.py gist: 112 lines of Python

```
Minimal character-level Vanilla RNN model. Written by Andrej Karpathy (@karpathy)
3 BSD License
4 ***
 5 import numpy as np
7 # data I/0
 8 data = open('input.txt', 'r').read() # should be simple plain text file
 o chars = list(set(data))
10 data_size, vocab_size = len(data), len(chars)
11 print 'data has %d characters, %d unique.' % (data_size, vocab_size)
12 char_to_ix = { ch:i for i, ch in enumerate(chars) }
13 ix_to_char = { i:ch for i,ch in enumerate(chars) }
15 # hyperparameters
16 hidden_size = 100 # size of hidden layer of neurons
17 seq_length = 25 # number of steps to unroll the RNN for
18 learning_rate = 1e-1
21 Wxh = np.random.randn(hidden_size, vocab_size)*0.01 # input to hidden
22 Whh = np.random.randn(hidden_size, hidden_size)*0.01 # hidden to hidden
23 Why = np.random.randn(vocab_size, hidden_size)*0.01 # hidden to output
24 bh = np.zeros((hidden_size, 1)) # hidden bias
25 by = np.zeros((vocab_size, 1)) # output bias
27 def lossFun(inputs, targets, hprev):
     ......
28
      inputs, targets are both list of integers.
      hprev is Hx1 array of initial hidden state
      returns the loss, gradients on model parameters, and last hidden state
      .....
      xs, hs, ys, ps = {}, {}, {}, {}
34
      hs[-1] = np.copy(hprev)
     loss = 0
     # forward pass
      for t in xrange(len(inputs));
        xs[t] = np.zeros((vocab_size,1)) # encode in 1-of-k representation
38
        xs[t][inputs[t]] = 1
        hs[t] = np.tanh(np.dot(Wxh, xs[t]) + np.dot(Whh, hs[t-1]) + bh) # hidden state
        ys[t] = np.dot(Why, hs[t]) + by # unnormalized log probabilities for next chars
        ps[t] = np.exp(ys[t]) / np.sum(np.exp(ys[t])) # probabilities for next chars
        loss += -np.log(ps[t][targets[t],0]) # softmax (cross-entropy loss)
44 # backward pass: compute gradients going backwards
dWxh, dWhh, dWhy = np.zeros_like(Wxh), np.zeros_like(Whh), np.zeros_like(Why)
      dbh, dby = np.zeros_like(bh), np.zeros_like(by)
       dhnext = np.zeros_like(hs[0])
      for t in reversed(xrange(len(inputs))):
        dy = np.copy(ps[t])
        dy[targets[t]] -= 1 # backprop into y
50
        dWhy += np.dot(dy, hs[t].T)
52 dby += dy
53 dh = np.dot(Why.T, dy) + dhnext # backprop into h
54 dhraw = (1 - hs[t] * hs[t]) * dh # backprop through tanh nonlinearity
        dbb += dbraw
        dWxh += np.dot(dhraw, xs[t].T)
        dwhh += np.dot(dhraw, hs[t-1].T)
        dhnext = np.dot(Whh.T, dhraw)
      for dparam in [dWxh, dWhh, dWhy, dbh, dby]:
```

np.clip(dparam, -5, 5, out=dparam) # clip to mitigate exploding gradients
return loss, dwkh, dwhh, dwhy, dbh, dby, hs[len(inputs)-1]

```
63 def sample(h, seed_ix, n):
64 ....
65
       sample a sequence of integers from the model
      h is memory state, seed ix is seed letter for first time step
66
68 x = np.zeros((vocab_size, 1))
69 x[seed_ix] = 1
      ixes = [1]
      for t in xrange(n):
        h = np.tanh(np.dot(Wxh, x) + np.dot(Whh, h) + bh)
        y = np.dot(Why, h) + by
        p = np.exp(y) / np.sum(np.exp(y))
        ix = np.random.choice(range(vocab_size), p=p.ravel())
        x = np.zeros((vocab_size, 1))
         x[ix] = 1
         ixes.append(ix)
       return ixes
80
81 n, p = 0, 0
82 mWxh, mWhh, mWhy = np.zeros like(Wxh), np.zeros like(Whh), np.zeros like(Why)
as mbh, mby = np.zeros like(bh), np.zeros like(by) # memory variables for Adagrad
84 smooth_loss = -np.log(1.0/vocab_size)*seq_length # loss at iteration 0
85 while True:
86 # prepare inputs (we're sweeping from left to right in steps seq_length long)
       if n+seq length+1 >= len(data) or n == 0:
        hprev = np.zeros((hidden_size,1)) # reset RNN memory
       p = 0 # go from start of data
       inputs = [char_to_ix[ch] for ch in data[p:p+seq_length]]
       targets = [char_to_ix[ch] for ch in data[p+1:p+seq_length+1]]
94 if n % 100 == 0;
         sample_ix = sample(hprev, inputs[0], 200)
95
96
         txt = ''.join(ix_to_char[ix] for ix in sample_ix)
         print '---- \n %s \n----' % (txt, )
99
      # forward seq_length characters through the net and fetch gradient
       loss. dwxh. dwhh. dwhy, dbh, dby, hprev = lossFun(inputs, targets, hprev)
       smooth_loss = smooth_loss * 0.999 + loss * 0.001
       if n % 100 == 0: print 'iter %d, loss: %f' % (n, smooth_loss) # print progress
      # perform parameter update with Adagrad
       for param, dparam, mem in zip([Wxh, Whh, Why, bh, by],
                                    [dwxh, dwhh, dwhy, dbh, dby],
                                    [mWxh, mWhh, mWhy, mbh, mby]):
108
         mem += dparam * dparam
         param += -learning_rate * dparam / np.sqrt(mem + 1e-8) # adagrad update
      p += seg length # move data pointer
```

112 n += 1 # iteration counter

(https://gist.github.com/karpathy/d4dee5 66867f8291f086)

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Lecture 8 - 56

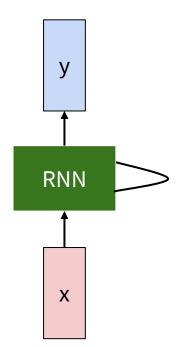
THE SONNETS

by William Shakespeare

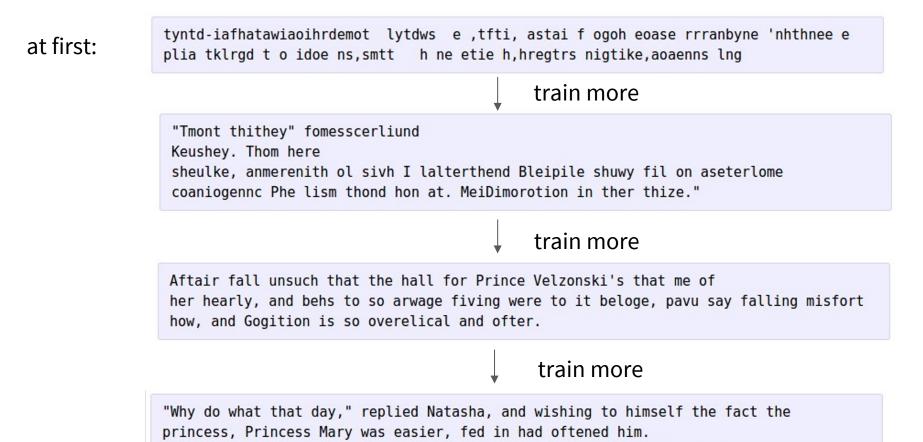
From fairest creatures we desire increase, That thereby beauty's rose might never die, But as the riper should by time decease, His tender heir might bear his memory: But thou, contracted to thine own bright eyes, Feed'st thy light's flame with self-substantial fuel, Making a famine where abundance lies, Thyself thy foe, to thy sweet self too cruel: Thou that art now the world's fresh ornament, And only herald to the gaudy spring, Within thine own bud buriest thy content, And tender churl mak'st waste in niggarding: Pity the world, or else this glutton be, To eat the world's due, by the grave and thee.

When forty winters shall besiege thy brow, And dig deep trenches in thy beauty's field, Thy youth's proud livery so gazed on now, Will be a tatter'd weed of small worth held: Then being asked, where all thy beauty lies, Where all the treasure of thy lusty days; To say, within thine own deep sunken eyes, Were an all-eating shame, and thriftless praise. How much more praise deserv'd thy beauty's use, If thou couldst answer 'This fair child of mine Shall sum my count, and make my old excuse,' Proving his beauty by succession thine! This were to be new made when thou art old, And see thy blood warm when thou feel'st it cold.

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Lecture 8 - 57



Pierre aking his soul came to the packs and drove up his father-in-law women.

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Lecture 8 - 58

PANDARUS:

Alas, I think he shall be come approached and the day When little srain would be attain'd into being never fed, And who is but a chain and subjects of his death, I should not sleep.

Second Senator:

They are away this miseries, produced upon my soul, Breaking and strongly should be buried, when I perish The earth and thoughts of many states.

DUKE VINCENTIO:

Well, your wit is in the care of side and that.

Second Lord:

They would be ruled after this chamber, and my fair nues begun out of the fact, to be conveyed, Whose noble souls I'll have the heart of the wars.

Clown:

Come, sir, I will make did behold your worship.

VIOLA: I'll drink it.

VIOLA:

Why, Salisbury must find his flesh and thought That which I am not aps, not a man and in fire, To show the reining of the raven and the wars To grace my hand reproach within, and not a fair are hand, That Caesar and my goodly father's world; When I was heaven of presence and our fleets, We spare with hours, but cut thy council I am great, Murdered and by thy master's ready there My power to give thee but so much as hell: Some service in the noble bondman here, Would show him to her wine.

KING LEAR:

O, if you were a feeble sight, the courtesy of your law, Your sight and several breath, will wear the gods With his heads, and my hands are wonder'd at the deeds, So drop upon your lordship's head, and your opinion Shall be against your honour.

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Lecture 8 - 59

The Stacks Project: open source algebraic geometry textbook

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Latex source

http://stacks.math.columbia.edu/

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Lecture 8 -

For $\bigoplus_{n=1,...,m}$ where $\mathcal{L}_{m_{\bullet}} = 0$, hence we can find a closed subset \mathcal{H} in \mathcal{H} and any sets \mathcal{F} on X, U is a closed immersion of S, then $U \to T$ is a separated algebraic space.

Proof. Proof of (1). It also start we get

 $S = \operatorname{Spec}(R) = U \times_X U \times_X U$

and the comparicoly in the fibre product covering we have to prove the lemma generated by $\coprod Z \times_U U \to V$. Consider the maps M along the set of points Sch_{fppf} and $U \to U$ is the fibre category of S in U in Section, ?? and the fact that any U affine, see Morphisms, Lemma ??. Hence we obtain a scheme S and any open subset $W \subset U$ in Sh(G) such that $Spec(R') \to S$ is smooth or an

 $U = \bigcup U_i \times_{S_i} U_i$

which has a nonzero morphism we may assume that f_i is of finite presentation over S. We claim that $\mathcal{O}_{X,x}$ is a scheme where $x, x', s'' \in S'$ such that $\mathcal{O}_{X,x'} \to \mathcal{O}'_{X',x'}$ is separated. By Algebra, Lemma ?? we can define a map of complexes $\operatorname{GL}_{S'}(x'/S'')$ and we win.

To prove study we see that $\mathcal{F}|_U$ is a covering of \mathcal{X}' , and \mathcal{T}_i is an object of $\mathcal{F}_{X/S}$ for i > 0 and \mathcal{F}_p exists and let \mathcal{F}_i be a presheaf of \mathcal{O}_X -modules on \mathcal{C} as a \mathcal{F} -module. In particular $\mathcal{F} = U/\mathcal{F}$ we have to show that

$$\widetilde{M}^{\bullet} = \mathcal{I}^{\bullet} \otimes_{\mathrm{Spec}(k)} \mathcal{O}_{S,s} - i_X^{-1} \mathcal{F})$$

is a unique morphism of algebraic stacks. Note that

 $Arrows = (Sch/S)_{fppf}^{opp}, (Sch/S)_{fppf}$

and

 $V = \Gamma(S, \mathcal{O}) \longmapsto (U, \operatorname{Spec}(A))$

is an open subset of X. Thus U is affine. This is a continuous map of X is the inverse, the groupoid scheme S.

Proof. See discussion of sheaves of sets.

The result for prove any open covering follows from the less of Example ??. It may replace S by $X_{spaces, \acute{e}tale}$ which gives an open subspace of X and T equal to S_{Zar} , see Descent, Lemma ??. Namely, by Lemma ?? we see that R is geometrically regular over S.

Lemma 0.1. Assume (3) and (3) by the construction in the description.

Suppose $X = \lim |X|$ (by the formal open covering X and a single map $\underline{\operatorname{Proj}}_X(\mathcal{A}) = \operatorname{Spec}(B)$ over U compatible with the complex

 $Set(\mathcal{A}) = \Gamma(X, \mathcal{O}_{X, \mathcal{O}_X}).$

When in this case of to show that $\mathcal{Q} \to C_{Z/X}$ is stable under the following result in the second conditions of (1), and (3). This finishes the proof. By Definition ?? (without element is when the closed subschemes are catenary. If T is surjective we may assume that T is connected with residue fields of S. Moreover there exists a closed subspace $Z \subset X$ of X where U in X' is proper (some defining as a closed subset of the uniqueness it suffices to check the fact that the following theorem

(1) f is locally of finite type. Since S = Spec(R) and Y = Spec(R).

Proof. This is form all sheaves of sheaves on X. But given a scheme U and a surjective étale morphism $U \to X$. Let $U \cap U = \coprod_{i=1,...,n} U_i$ be the scheme X over S at the schemes $X_i \to X$ and $U = \lim_i X_i$.

The following lemma surjective restrocomposes of this implies that $\mathcal{F}_{x_0} = \mathcal{F}_{x_0} = \mathcal{F}_{\mathcal{X},...,0}$.

Lemma 0.2. Let X be a locally Noetherian scheme over S, $E = \mathcal{F}_{X/S}$. Set $\mathcal{I} = \mathcal{J}_1 \subset \mathcal{I}'_n$. Since $\mathcal{I}^n \subset \mathcal{I}^n$ are nonzero over $i_0 \leq \mathfrak{p}$ is a subset of $\mathcal{J}_{n,0} \circ \overline{A}_2$ works.

Lemma 0.3. In Situation ??. Hence we may assume q' = 0.

Proof. We will use the property we see that \mathfrak{p} is the mext functor (??). On the other hand, by Lemma ?? we see that

 $D(\mathcal{O}_{X'}) = \mathcal{O}_X(D)$

where K is an F-algebra where δ_{n+1} is a scheme over S.

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Lecture 8 - 61

Proof. Omitted.

Lemma 0.1. Let C be a set of the construction.

Let C be a gerber covering. Let F be a quasi-coherent sheaves of O-modules. We have to show that

$$\mathcal{O}_{\mathcal{O}_X} = \mathcal{O}_X(\mathcal{L})$$

Proof. This is an algebraic space with the composition of sheaves \mathcal{F} on $X_{\acute{e}tale}$ we have

$$\mathcal{O}_X(\mathcal{F}) = \{morph_1 \times_{\mathcal{O}_X} (\mathcal{G}, \mathcal{F})\}$$

where \mathcal{G} defines an isomorphism $\mathcal{F} \to \mathcal{F}$ of \mathcal{O} -modules.

Lemma 0.2. This is an integer Z is injective.

Proof. See Spaces, Lemma ??.

Lemma 0.3. Let S be a scheme. Let X be a scheme and X is an affine open covering. Let $U \subset X$ be a canonical and locally of finite type. Let X be a scheme. Let X be a scheme which is equal to the formal complex.

The following to the construction of the lemma follows.

Let X be a scheme. Let X be a scheme covering. Let

 $b: X \to Y' \to Y \to Y \to Y' \times_X Y \to X.$

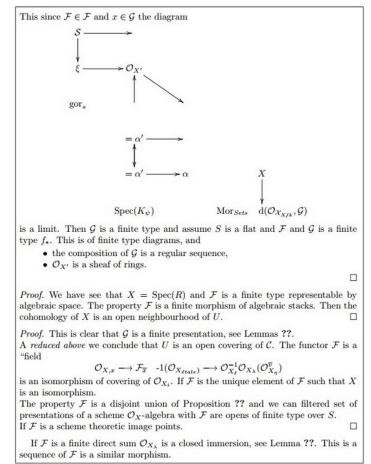
be a morphism of algebraic spaces over S and Y.

Proof. Let X be a nonzero scheme of X. Let X be an algebraic space. Let \mathcal{F} be a quasi-coherent sheaf of \mathcal{O}_X -modules. The following are equivalent

(1) \mathcal{F} is an algebraic space over S.

(2) If X is an affine open covering.

Consider a common structure on X and X the functor $\mathcal{O}_X(U)$ which is locally of finite type. \Box



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Lecture 8 - 62

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ill block	block: discard bdi_unregister()	9 days ago	Carabian								
ill crypto	Merge git://git.kernel.org/pub/so	HTTPS clone URL									
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init	init: fix regression by supporting devices with major:minor:offset fo a month ago										

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Lecture 8 - 63

```
static void do command(struct seg file *m, void *v)
{
 int column = 32 << (cmd[2] & 0x80);</pre>
 if (state)
   cmd = (int)(int_state ^ (in 8(&ch->ch_flags) & Cmd) ? 2 : 1);
 else
   seq = 1;
 for (i = 0; i < 16; i++) {
   if (k & (1 << 1))
      pipe = (in use & UMXTHREAD UNCCA) +
        ((count & 0x0000000fffffff8) & 0x000000f) << 8;
   if (count == 0)
      sub(pid, ppc_md.kexec_handle, 0x2000000);
   pipe set bytes(i, 0);
 /* Free our user pages pointer to place camera if all dash */
 subsystem_info = &of_changes[PAGE_SIZE];
 rek controls(offset, idx, &soffset);
 /* Now we want to deliberately put it to device */
 control check polarity(&context, val, 0);
 for (i = 0; i < COUNTER; i++)
   seq puts(s, "policy ");
```

Generated C code

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Lecture 8 - 64

```
1*
   Copyright (c) 2006-2010, Intel Mobile Communications. All rights reserved.
    This program is free software; you can redistribute it and/or modify it
* under the terms of the GNU General Public License version 2 as published by
 * the Free Software Foundation.
         This program is distributed in the hope that it will be useful,
 * but WITHOUT ANY WARRANTY; without even the implied warranty of
     MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the
   GNU General Public License for more details.
    You should have received a copy of the GNU General Public License
     along with this program; if not, write to the Free Software Foundation,
* Inc., 675 Mass Ave, Cambridge, MA 02139, USA.
*/
#include <linux/kexec.h>
#include <linux/errno.h>
#include <linux/io.h>
#include <linux/platform_device.h>
#include <linux/multi.h>
#include <linux/ckevent.h>
#include <asm/io.h>
#include <asm/prom.h>
#include <asm/e820.h>
#include <asm/system info.h>
#include <asm/setew.h>
#include <asm/pgproto.h>
```

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Lecture 8 - 65

```
#include <asm/io.h>
#include <asm/prom.h>
#include <asm/e820.h>
#include <asm/system info.h>
#include <asm/setew.h>
#include <asm/pgproto.h>
#define REG_PG vesa slot addr pack
#define PFM NOCOMP AFSR(0, load)
#define STACK DDR(type) (func)
#define SWAP_ALLOCATE(nr)
                            (e)
#define emulate sigs() arch get unaligned child()
#define access rw(TST) asm volatile("movd %%esp, %0, %3" : : "r" (0)); \
 if ( type & DO READ)
static void stat PC SEC read mostly offsetof(struct seq argsqueue, \
         pC>[1]);
static void
os_prefix(unsigned long sys)
{
#ifdef CONFIG PREEMPT
 PUT_PARAM_RAID(2, sel) = get_state_state();
 set_pid_sum((unsigned long)state, current_state_str(),
           (unsigned long)-1->lr_full; low;
}
```

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Lecture 8 - 66

OpenAI Codex



/* &dd this image of a
rocketship:
https://i1.sndcdn.com/artworks
-j8xjG7zc1wmTe07b-06183wt500x500.jpg */
var rocketship =
document.createElement('img');
rocketship.src =
'https://i1.sndcdn.com/artwork
s-j8xjG7zc1wmTe07b-06183wt500x500.jpg';
document.body.appendChild(rock
etship);

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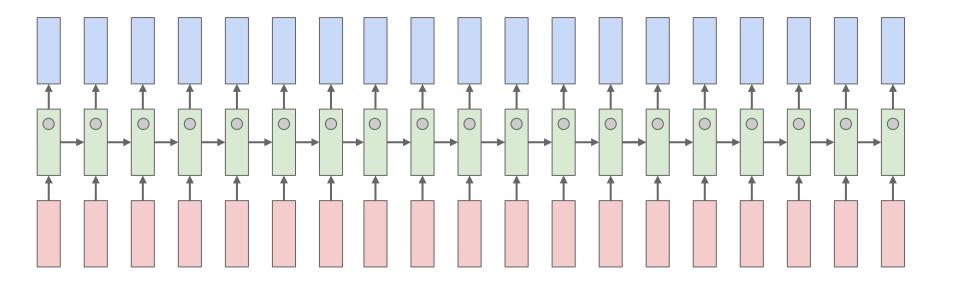


https://openai.com/blog/openai-codex/

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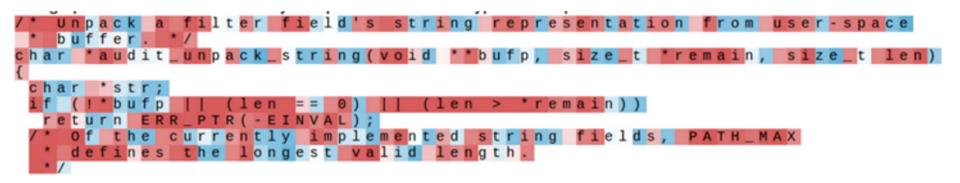
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Lecture 8 - 68



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"You mean to imply that I have nothing to eat out of.... On the contrary, I can supply you with everything even if you want to give dinner parties," warmly replied Chichagov, who tried by every word he spoke to prove his own rectitude and therefore imagined Kutuzov to be animated by the same desire.

Kutuzov, shrugging his shoulders, replied with his subtle penetrating smile: "I meant merely to say what I said."

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quote detection cell

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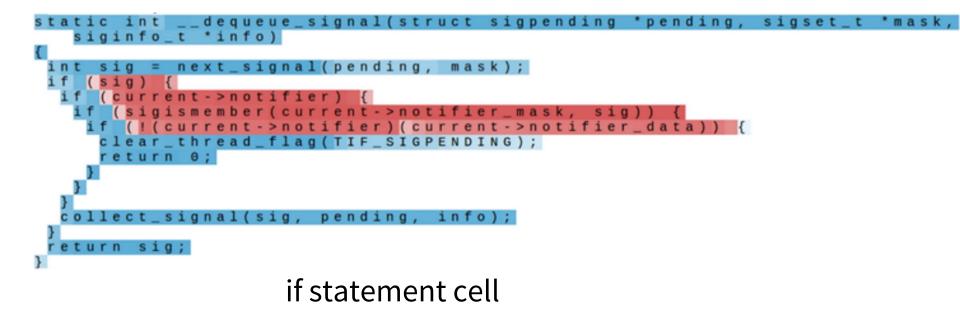
The sole importance of the crossing of the Berezina that it plainly and indubitably proved the fallacy of all the plans for cutting off the enemy's retreat and the soundness of the only possible line of action--the one Kutuzov and the general mass of the army demanded -- namely, simply to follow the enemy up. The French crowd fled a continually increasing speed and all its energy was directed to reaching its goal. It fled like a wounded animal and it was impossible to block its path. This was shown not so much by the arrangements it made for crossing as by what took place at the bridges. When the bridges broke down, unarmed soldiers, people from Moscow and women with children o were with the French transport, all--carried on by vis inertiae-pressed forward into boats and into the ice-covered water and did not. surrender.

line length tracking cell

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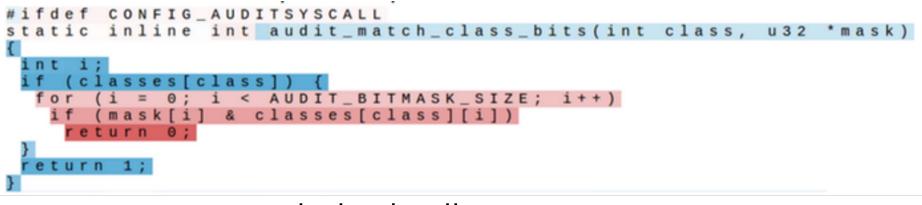
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code depth cell

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RNN tradeoffs

RNN Advantages:

- Can process any length of the input
- Computation for step *t* can (in theory) use information from many steps back
- Model size does not increase for longer input
- The same weights are applied on every timestep, so there is symmetry in how inputs are processed.

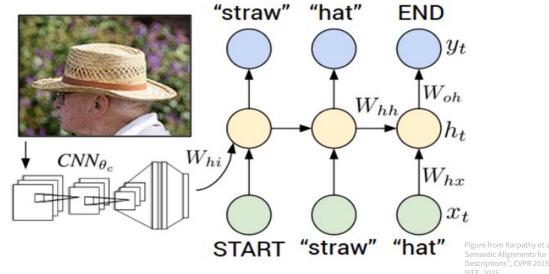
RNN Disadvantages:

- Recurrent computation is slow
- In practice, difficult to access information from many steps back

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Image Captioning



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Explain Images with Multimodal Recurrent Neural Networks, Mao et al.

Deep Visual-Semantic Alignments for Generating Image Descriptions, Karpathy and Fei-Fei

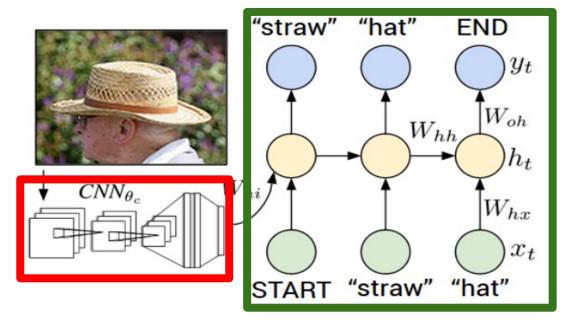
Show and Tell: A Neural Image Caption Generator, Vinyals et al.

Long-term Recurrent Convolutional Networks for Visual Recognition and Description, Donahue et al.

Learning a Recurrent Visual Representation for Image Caption Generation, Chen and Zitnick

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Recurrent Neural Network



Convolutional Neural Network

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Lecture 8 - 77

test image



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image

conv-64 conv-64 maxpool

conv-128

conv-128

maxpool

conv-256

conv-256

maxpool

conv-512

conv-512

maxpool

conv-512

conv-512

maxpool

FC-4096 FC-4096

FC-1000

softmax

test image



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image



maxpool

conv-128

conv-128

maxpool

conv-256 conv-256

maxpool

conv-512

conv-512

maxpool

conv-512

conv-512

maxpool

FC-4096 FC-4096 FC-1000 softwax

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Lecture 8 -

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test image

image



conv-128

conv-128

maxpool

conv-256 conv-256 maxpool

conv-512 conv-512

maxpool

conv-512

conv-512

maxpool

FC-4096 FC-4096

x0 <START>

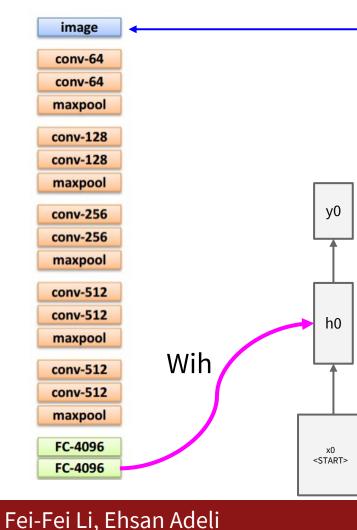


test image



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Lecture 8 -81

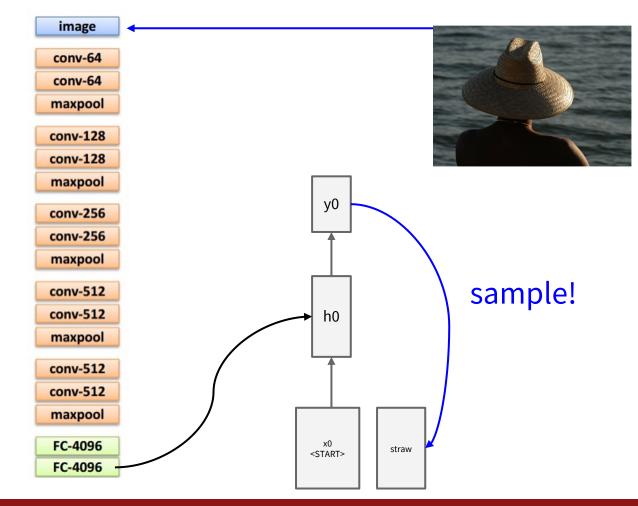


before: h = tanh($W_{xh} * x + W_{hh} * h$)

now: h = tanh($W_{xh} * x + W_{hh} * h + W_{ih} * v$)

test image

Lecture 8 - 82

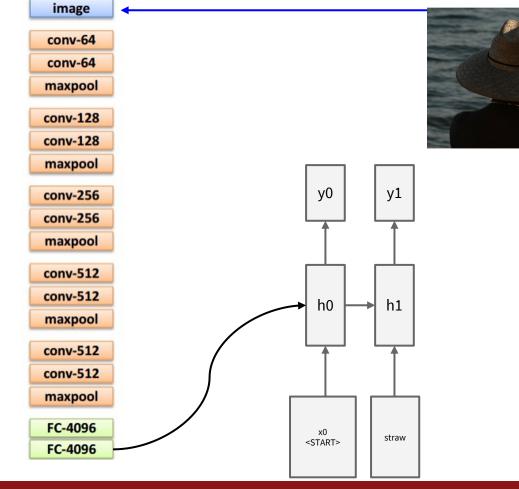


test image

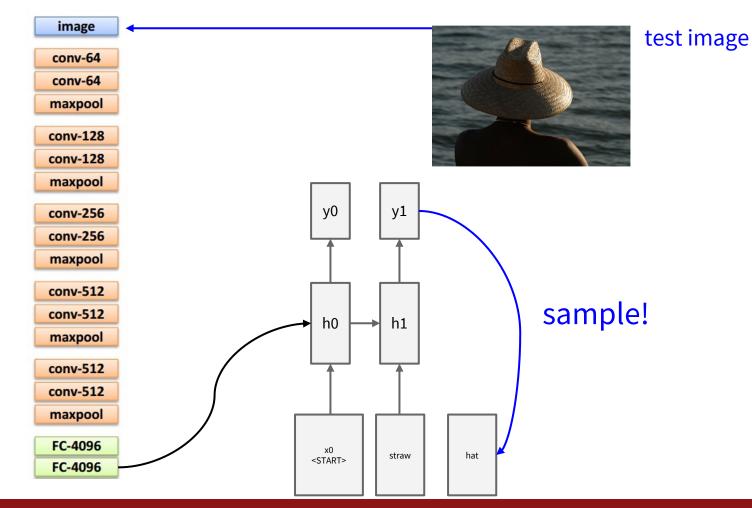
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Lecture 8 - 83

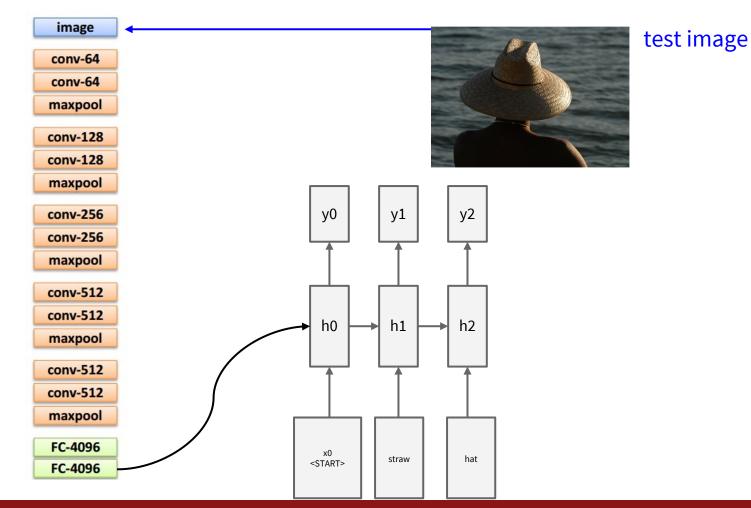




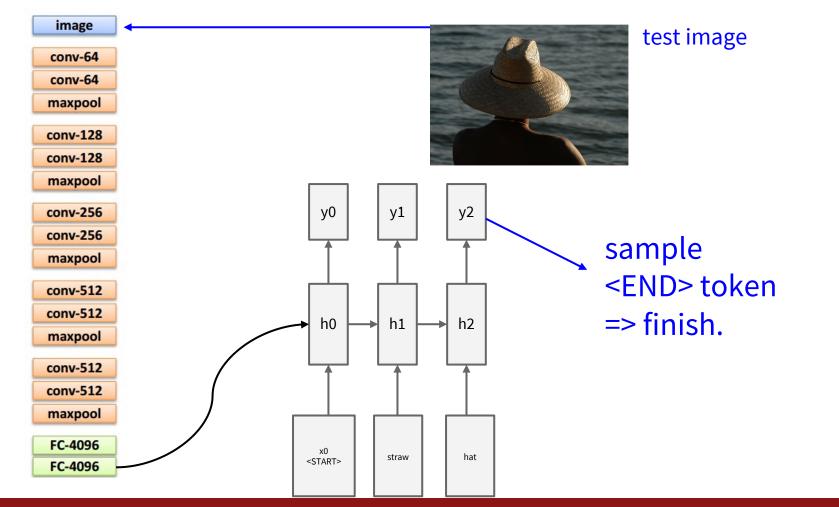
Lecture 8 - 84



Lecture 8 - 85



Lecture 8 - 86



Lecture 8 - 87

Image Captioning: Example Results

Captions generated using neuraltalk2 All images are CC0 Public domain: cat suitcase, cat tree, dog, bear, surfers, giraffe, motorcycle





A cat sitting on a suitcase on the floor



Two people walking on the beach with surfboards

A cat is sitting on a tree branch



A tennis player in action on the court



A dog is running in the grass

with a frisbee

Two giraffes standing in a grassy field



A white teddy bear sitting in the grass



A man riding a dirt bike on a dirt track

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Captions generated using <u>neuraltalk2</u> All images are <u>CCO Public domain</u>; <u>fur coat</u> <u>handstand</u>, <u>spider web</u>, <u>baseball</u>

Image Captioning: Failure Cases



A woman is holding a cat in her hand



A person holding a computer mouse on a desk



A woman standing on a beach holding a surfboard



A bird is perched on a tree branch



A man in a baseball uniform throwing a ball

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Visual Question Answering (VQA)



- Q: What endangered animal is featured on the truck?
- A: A bald eagle.
- A: A sparrow.
- A: A humming bird.
- A: A raven.



- Q: Where will the driver go if turning right?
- A: Onto 24 ³/₄ Rd. A: Onto 25 ³/₄ Rd.
- A: Onto 23 ¾ Rd.
- A: Onto Main Street.



- Q: When was the picture taken?
- A: During a wedding.
- A: During a bar mitzvah.
- A: During a funeral.
- A: During a Sunday church



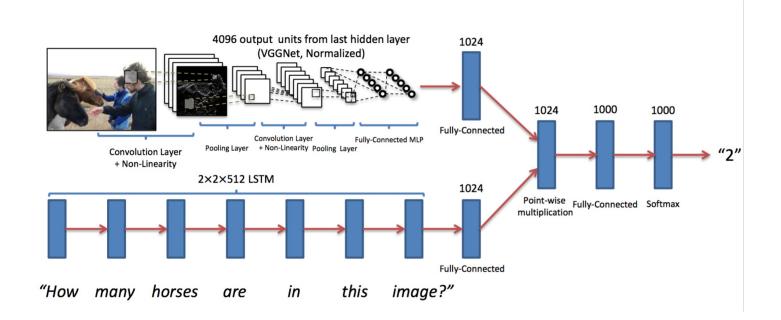
- Q: Who is under the umbrella?
- A: Two women.
- A: A child.
- A: An old man.
- A: A husband and a wife.

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Agrawal et al, "VQA: Visual Question Answering", ICCV 2015 Zhu et al, "Visual 7W: Grounded Question Answering in Images", CVPR 2016 Figure from Zhu et al, copyright IEEE 2016. Reproduced for educational purposes.

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Visual Question Answering (VQA)



Agrawal et al, "Visual 7W: Grounded Question Answering in Images", CVPR 2015 Figures from Agrawal et al, copyright IEEE 2015. Reproduced for educational purposes.

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Visual Dialog: Conversations about images



Das et al, "Visual Dialog", CVPR 2017 Figures from Das et al, copyright IEEE 2017. Reproduced with permission.

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Visual Language Navigation: Go to the living room

Agent encodes instructions in language and uses an RNN to generate a series of movements as the visual input changes after each move.

Wang et al, "Reinforced Cross-Modal Matching and Self-Supervised Imitation Learning for Vision-Language Navigation", CVPR 2018 Figures from Wang et al, copyright IEEE 2017. Reproduced with permission.

Instruction

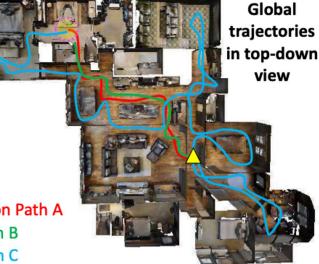
Turn right and head towards the *kitchen*. Then turn left, pass a *table* and enter the *hallway*. Walk down the hallway and turn into the *entry way* to your right *without doors*. Stop in front of the *toilet*.



Initial Position Target Position

Demonstration Path A
 Executed Path B
 Executed Path C

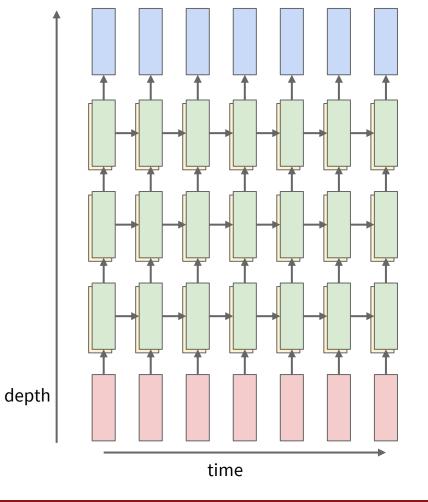
Local visual scene



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Multilayer RNNs



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Long Short Term Memory (LSTM)

Vanilla RNN

LSTM

$$h_t = \tanh\left(W\begin{pmatrix}h_{t-1}\\x_t\end{pmatrix}\right)$$

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

96

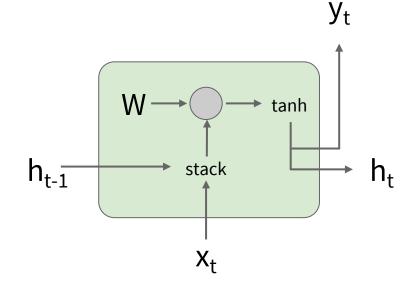
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Hochreiter and Schmidhuber, "Long Short Term Memory", Neural Computation 1997

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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



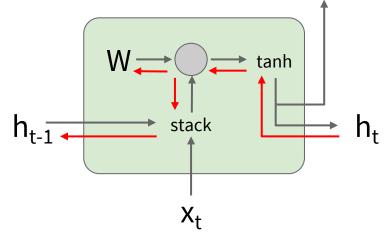
$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$
$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$
$$= \tanh\left(W\begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$

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y_t

Backpropagation from h_t to h_{t-1} multiplies by W (actually W_{hh}^T)



Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

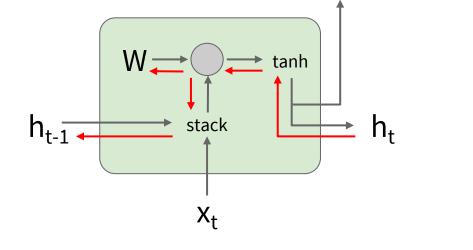
$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$
$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$
$$= \tanh\left(W\begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$

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y_t

Backpropagation from h_t to h_{t-1} multiplies by W (actually W_{hh}^T)



Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

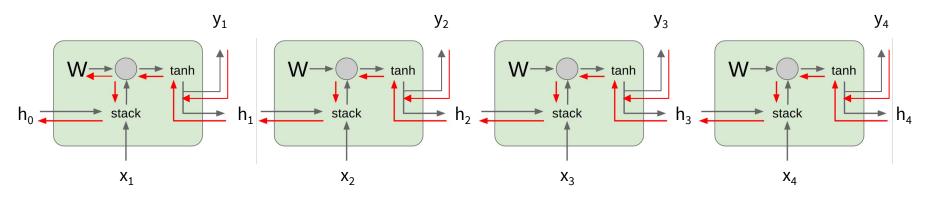
$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$
$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$
$$= \tanh\left(W\begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$

$$rac{\partial h_t}{\partial h_{t-1}} = tanh'(W_{hh}h_{t-1}+W_{xh}x_t)W_{hh}$$

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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



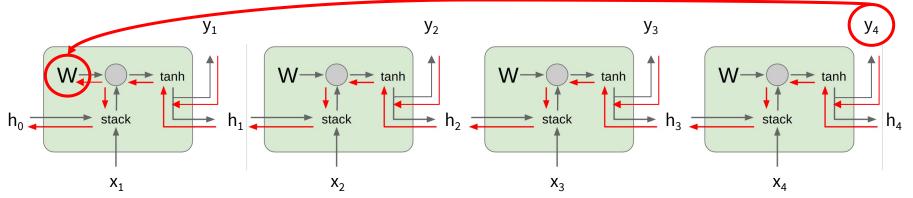
$$rac{\partial L}{\partial W} = \sum_{t=1}^T rac{\partial L_t}{\partial W}$$

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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:



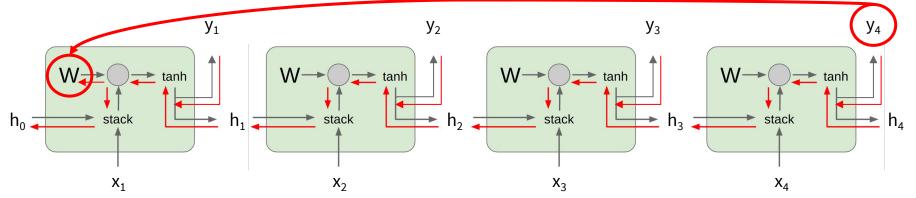
$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$
 $rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} rac{\partial h_t}{\partial h_{t-1}} \dots rac{\partial h_T}{\partial W}$

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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:



$$rac{\partial L}{\partial W} = \sum_{t=1}^T rac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} rac{\partial h_t}{\partial h_{t-1}} \dots rac{\partial h_1}{\partial W} = rac{\partial L_T}{\partial h_T} (\prod_{t=2}^T rac{\partial h_t}{\partial h_{t-1}}) rac{\partial h_1}{\partial W}$$

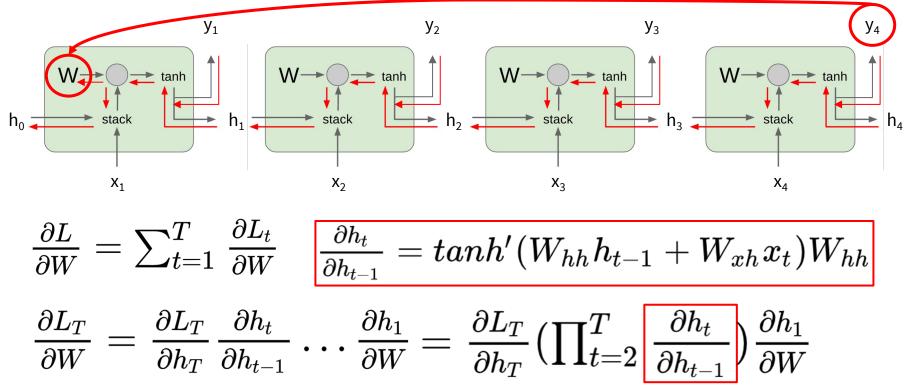
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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:

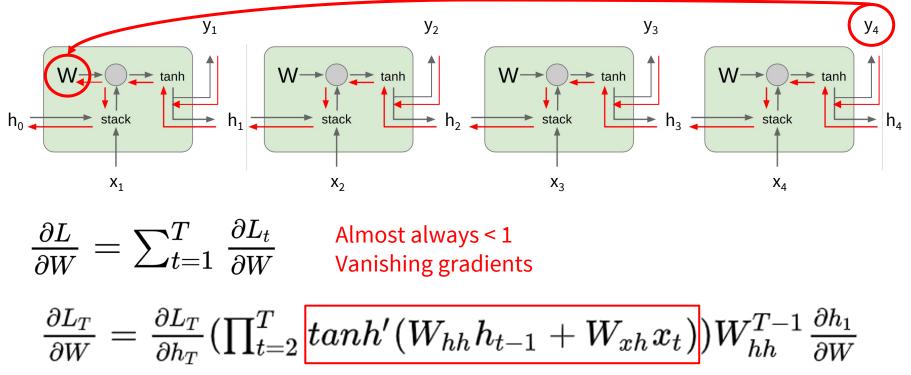


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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:

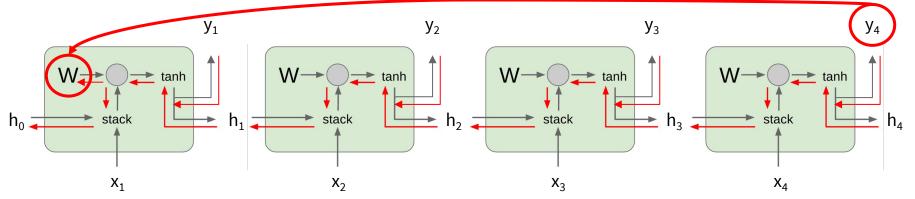


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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:



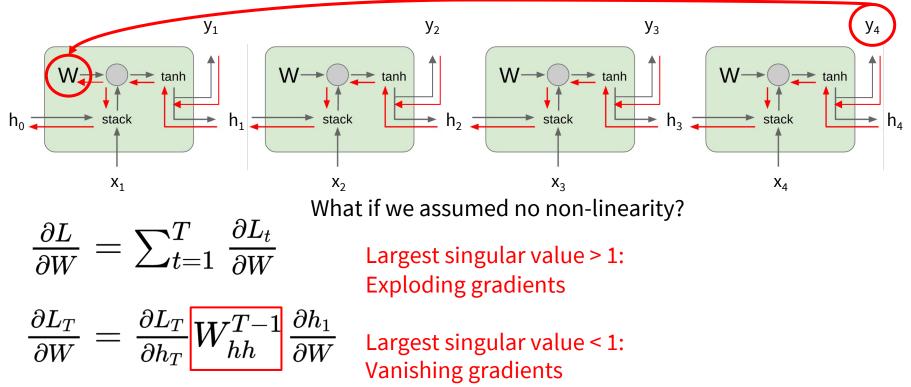
 $rac{\partial L}{\partial W} = \sum_{t=1}^T rac{\partial L_t}{\partial W}$ What if we assumed no non-linearity?

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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:

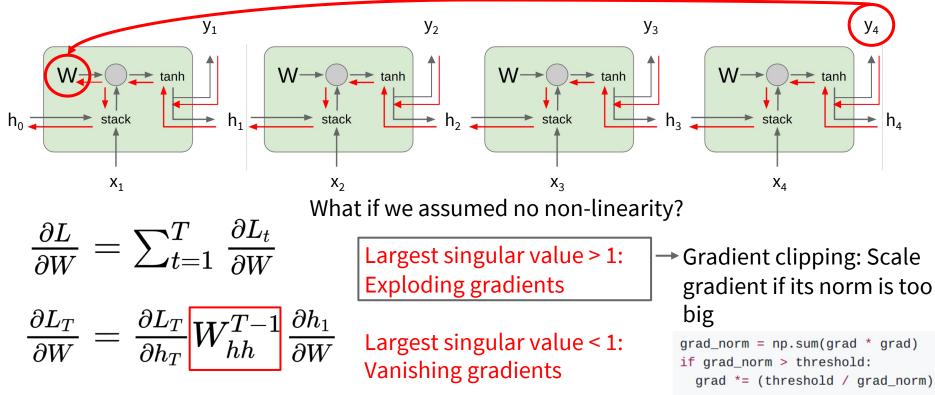


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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:



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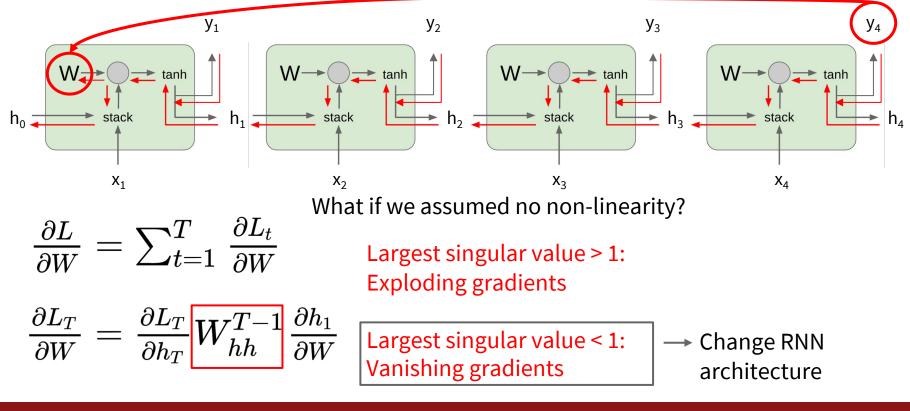
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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

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Gradients over multiple time steps:



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Long Short Term Memory (LSTM)

Vanilla RNN

LSTM

$$h_t = \tanh\left(W\begin{pmatrix}h_{t-1}\\x_t\end{pmatrix}\right)$$

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

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Hochreiter and Schmidhuber, "Long Short Term Memory", Neural Computation 1997

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Long Short Term Memory (LSTM)

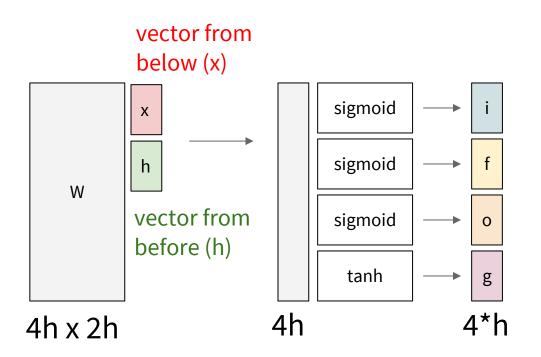
Vanilla RNN LSTM $h_{t} = \tanh\left(W\begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$ $\mathsf{Four gates}$ $\begin{pmatrix}i\\f\\o\\g\end{pmatrix} = \begin{pmatrix}\sigma\\\sigma\\d\\tanh\end{pmatrix}W\begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}$ $\mathsf{Cell state}$ $\mathsf{Hidden state}$ $h_{t} = o \odot \tanh(c_{t})$

Hochreiter and Schmidhuber, "Long Short Term Memory", Neural Computation 1997

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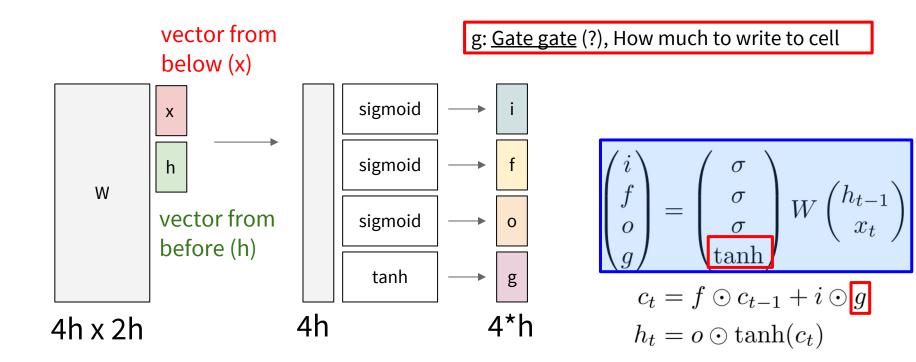
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Long Short Term Memory (LSTM) [Hochreiter et al., 1997]



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Lecture 8 - 111



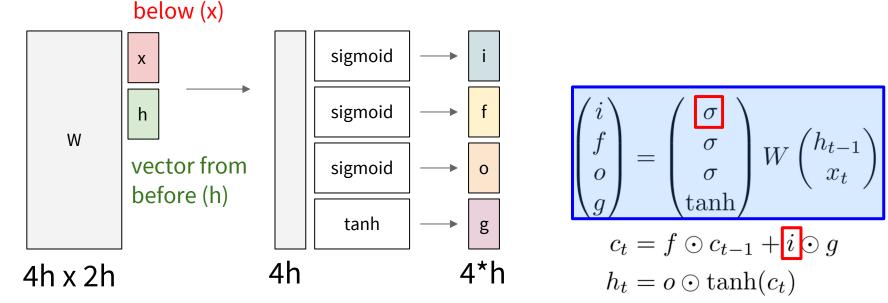
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vector from

i: Input gate, whether to write to cell

g: Gate gate (?), How much to write to cell



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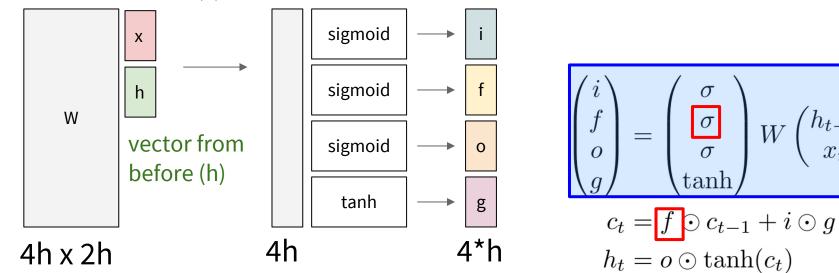
Lecture 8 - 113

vector from

i: Input gate, whether to write to cell

f: Forget gate, Whether to erase cell

g: <u>Gate gate</u> (?), How much to write to cell



below (x)

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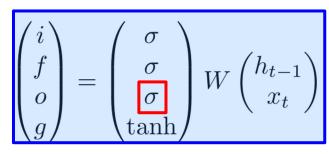
Lecture 8 -114

vector from

below (x) sigmoid Х sigmoid h W vector from sigmoid 0 before (h) tanh g 4*h 4h 4h x 2h

i: <u>Input gate</u>, whether to write to cellf: Forget gate. Whether to erase cello: <u>Output gate</u>, How much to reveal cell

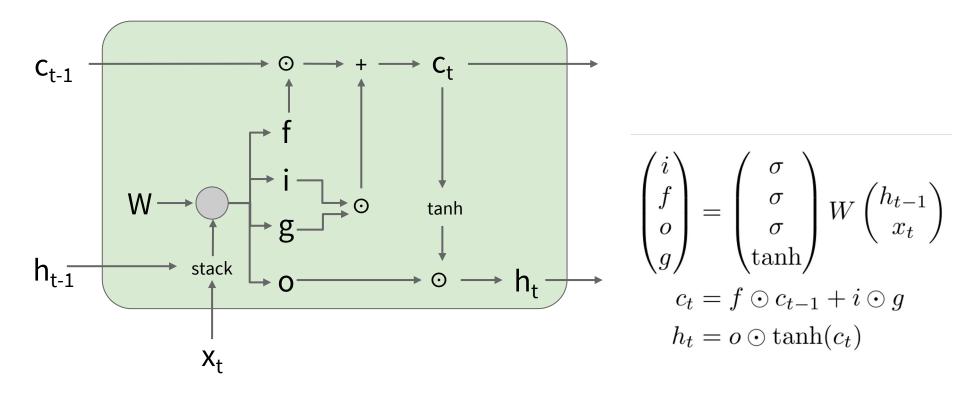
g: Gate gate (?), How much to write to cell



$$c_t = f \odot c_{t-1} + i \odot g$$
$$h_t = o \odot \tanh(c_t)$$

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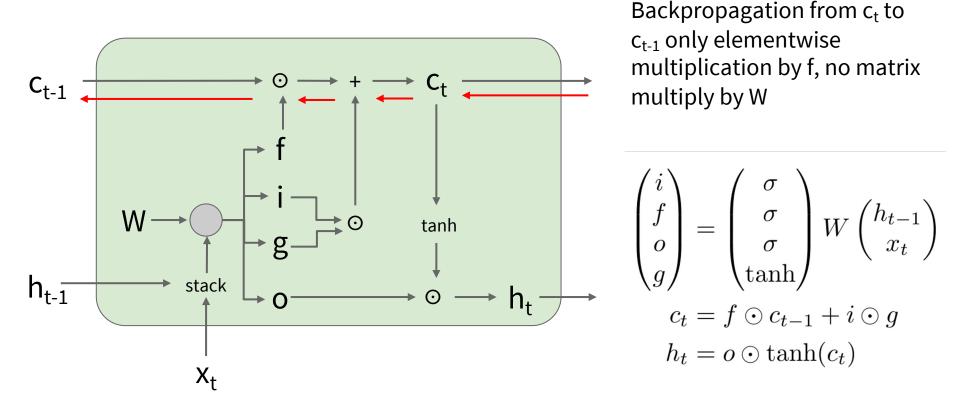
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Long Short Term Memory (LSTM): Gradient Flow [Hochreiter et al., 1997]

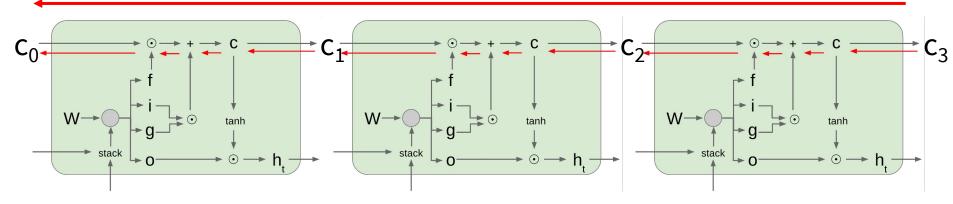


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Long Short Term Memory (LSTM): Gradient Flow [Hochreiter et al., 1997]

Uninterrupted gradient flow!



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Lecture 8 -

Do LSTMs solve the vanishing gradient problem?

The LSTM architecture makes it easier for the RNN to preserve information over many timesteps

- e.g. if the f = 1 and the i = 0, then the information of that cell is preserved indefinitely.
- By contrast, it's harder for vanilla RNN to learn a recurrent weight matrix Wh that preserves info in hidden state

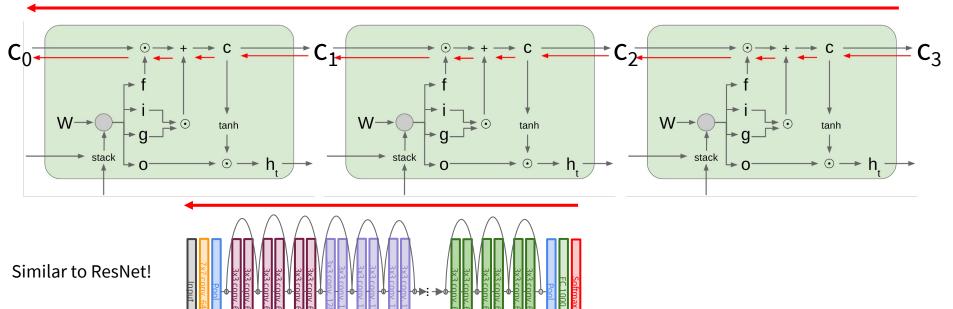
LSTM doesn't guarantee that there is no vanishing/exploding gradient, but it does provide an easier way for the model to learn long-distance dependencies

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Long Short Term Memory (LSTM): Gradient Flow [Hochreiter et al., 1997]

Uninterrupted gradient flow!

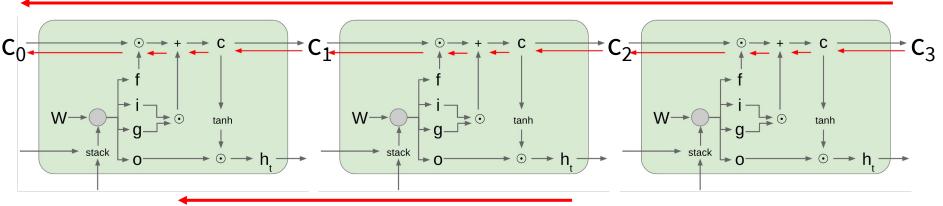


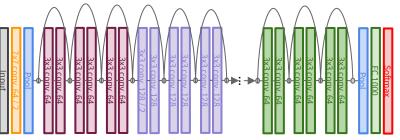
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Lecture 8 - 120

Long Short Term Memory (LSTM): Gradient Flow [Hochreiter et al., 1997]

Uninterrupted gradient flow!





In between: Highway Networks $g = T(x, W_T)$ $y = g \odot H(x, W_H) + (1 - g) \odot x$

Srivastava et al, "Highway Networks", ICML DL Workshop 2015

Similar to ResNet!

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Lecture 8 - 121

Other RNN Variants

GRU [Learning phrase representations using rnn encoderdecoder for statistical machine translation, Cho et al. 2014]

$$r_t = \sigma(W_{xr}x_t + W_{hr}h_{t-1} + b_r)$$

$$z_t = \sigma(W_{xz}x_t + W_{hz}h_{t-1} + b_z)$$

$$\tilde{h}_t = \tanh(W_{xh}x_t + W_{hh}(r_t \odot h_{t-1}) + b_h)$$

$$h_t = z_t \odot h_{t-1} + (1 - z_t) \odot \tilde{h}_t$$

[LSTM: A Search Space Odyssey, Greff et al., 2015] [An Empirical Exploration of Recurrent Network Architectures, Jozefowicz et al., 2015]

MUT1:

$$z = \operatorname{sigm}(W_{\operatorname{xz}}x_t + b_z)$$

$$r = \operatorname{sigm}(W_{\operatorname{xr}}x_t + W_{\operatorname{hr}}h_t + b_r)$$

$$h_{t+1} = \operatorname{tanh}(W_{\operatorname{hh}}(r \odot h_t) + \operatorname{tanh}(x_t) + b_{\operatorname{h}}) \odot z$$

$$+ h_t \odot (1 - z)$$

MUT2:

$$z = \operatorname{sigm}(W_{xz}x_t + W_{hz}h_t + b_z)$$

$$r = \operatorname{sigm}(x_t + W_{hr}h_t + b_r)$$

$$h_{t+1} = \operatorname{tanh}(W_{hh}(r \odot h_t) + W_{xh}x_t + b_h) \odot z$$

$$+ h_t \odot (1 - z)$$

MUT3:

$$z = \operatorname{sigm}(W_{xx}x_t + W_{hx}\tanh(h_t) + b_z)$$

$$r = \operatorname{sigm}(W_{xr}x_t + W_{hr}h_t + b_r)$$

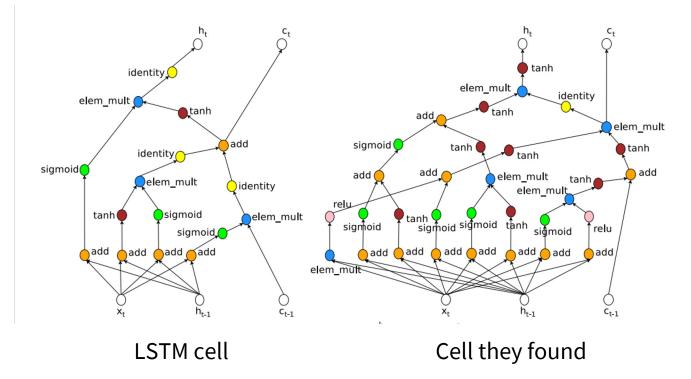
$$h_{t+1} = \operatorname{tanh}(W_{hh}(r \odot h_t) + W_{xh}x_t + b_h) \odot z$$

$$+ h_t \odot (1 - z)$$

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Neural Architecture Search for RNN architectures



Zoph et Le, "Neural Architecture Search with Reinforcement Learning", ICLR 2017 Figures copyright Zoph et al, 2017. Reproduced with permission.

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Summary

- RNNs allow a lot of flexibility in architecture design
- Vanilla RNNs are simple but don't work very well
- Common to use LSTM or GRU: their additive interactions improve gradient flow
- Backward flow of gradients in RNN can explode or vanish. Exploding is controlled with gradient clipping. Vanishing is controlled with additive interactions (LSTM)
- Better/simpler architectures are a hot topic of current research, as well as new paradigms for reasoning over sequences
- Better understanding (both theoretical and empirical) is needed.

Next time: Attention and Transformers

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