

# Learning Causalities behind Human Trajectories

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## Abstract

We present a fully un-supervised framework to learn the causalities behind human navigation. Using automatically extracted trajectories from aerial videos, we learn to model the interactions between moving targets and their static surrounding. This is in contrast to traditional approaches which use handcrafted functions such as “Social forces” or focus on one type of interactions given limited labeled data.

We use an end-to-end trainable recurrent convolutional architecture to predict where targets move next. Thanks to both the representation power of Convolutional Neural Networks (CNN) and the Long Short-Term Memory (LSTM) recurrent network, our approach is able to infer “navigable” paths without explicitly using scene labels or recognizing the target’s physical class (e.g. pedestrian, cyclist, or driver). Given the raw crop region surrounding a target, our method predicts its trajectory for the next frames. Although the used trajectories are error-prone, our learned model outperforms previous methods on public datasets as well as a newly collected one made of aerial views.

Prediction, forecasting, human trajectory, human-space interaction, Long Short-Term Memory, LSTM, Convolutional Neural Network, CNN.

## 1. Introduction

Human navigation is not random. When pedestrians and cyclists navigate their way through cities or school campuses, they respect a set of rules. They avoid each others, prefer to stay on sidewalks, and sharply turn at intersections while keeping a personal distance to their surrounding. All these behaviors obey social and safety rules. In this work, we aim to jointly learn to model these interactions between humans (referred to as *human-human*), and their static surrounding (referred to as *human-space*)<sup>1</sup>. The capability to model these interactions is used to predict where humans will move next. Such prediction goal is key to a wide range of applications - from the development of simulators, socially-aware robots [41], early warning systems

<sup>1</sup>Note that *humans* in this work includes any moving target such as bicyclists, drivers, or skateboarders.



Figure 1. We propose an end-to-end trainable recurrent convolutional architecture to predict where targets move next. Given the raw crop image surrounding a target (the yellow bounding boxes), our method predicts its trajectory for the next frames (the blue arrows).

for autonomous agents, to the design of intelligent tracking systems in smart environments [75].

Like any other prediction task, the ability to robustly predict human navigation highly depends on the available data and the capacity of the model to jointly reason on multiple cues. To date, we argue that data has guided and constrained the design of previous methods. From Helbing *et al.* [24], who proposed hand-crafted set of functions that mimics “social forces”, to Kitani *et al.* [32] who used static scene labels to predict the long-term trajectories, most of previous work relied on limited amount of labeled data. As a result, they accurately modeled simple interactions and were penalized to generalize to complex subtle interactions coming from mutual interactions between humans and the space.

Recently, Alahi *et al.* [1] have used ground truth pedestrians’ trajectories to learn the complex interactions between humans. However, they only focus on pedestrians (as opposed to multiple classes of targets such as bicyclists, skateboards, and vehicles), and did not model the human-space interactions. Inspired by their work to develop a data-driven method to learn interactions, we propose to jointly learn both human-space and human-human interactions in a fully un-supervised framework, i.e., given error-prone trajectories.

In this work, we study the representation power of a recurrent convolutional architecture to learn to predict the long-term motion trajectory of any target. We demonstrate the performance of our method using aerial views from campus scenes where several classes of targets such as pedestrians, bicyclists, skateboarders, cars or buses interact in complex crowded environments. At training, instead of using ground truth trajectories (as previous meth-

ods), we use the output of a state-of-the-art Multi-Target Tracking (MTT) algorithm. Thanks to the recent success of public challenges, the community has made great progress in MTT. We show that the current performance of a state-of-the-art MTT algorithm is good enough to learn to predict any target trajectory. For each tracked target, our recurrent convolutional network takes as input the surrounding raw image around the target, and outputs its future trajectory (see Figure 1).

In summary, the contributions of our paper are as follows:

- (i) *Recurrent convolutional architecture for human prediction.* Inspired by the recent success of hybrid architectures that use both Convolutional Neural Networks (CNN) and Long-Short Term Memory networks (LSTM) for different sequence prediction tasks such as handwriting [ ] or image captioning task [20], we adapt these architectures to predict any target’s motion dynamics. While LSTMs have the ability to learn and reproduce long sequences thus helping us model dependencies between multiple sequences correlated in time, the CNN with its hierarchical feature representation help us learn how this sequences interact in space, *i.e.* what is “navigable” (see Section 3).
- (ii) *Un-supervised framework.* Our second contribution relies on the un-supervised nature of our learning scheme. We show that we do not need to use ground truth trajectories to learn the causalities behind navigation. Our model is robust to tracking errors.
- (iii) *Campus drone dataset.* Finally, we publicly share a new dataset of UAV videos where more than 20K trajectories are labeled from 6 difference classes of targets leading to several hundred thousands of interactions. More details are available in Section 4.

In Section 5, we demonstrate the strength of our approach with respect to previous works that relies on a pre-classification step [32, ?]. Our method is capable, from aerial views, to predict any target’s trajectory without explicitly classifying its class (e.g., pedestrian, bicyclist, or car) neither its surrounding scene labels (e.g., side walk, grass, or building). It hence facilitates its usage in learning the dynamic of any other agents in other fields such as ants or mice for biological studies.

We believe that not only is this setting closer to any real world scenario, but also important for considering many interesting cases where people change their path drastically from their previous time step to accommodate the change in their static surroundings. For instance, to make a sharp right turn at a cross roads. The most interesting issue being tackled over here is that, we consider both human-human and human-space interactions at the same time, which could explain very typical cases of human behaviour where

a person not only accommodate social norms and how other people are walking around them, but also the constraints imposed by their surroundings. Clearly such complex interactions cannot be modelled by hand-crafted features or heuristics. Hence we come up with a data driven approach to learn all these complex scenarios while also reasoning about subtle underlying interactions.

One of the major contribution of this paper is to introduce a hybrid model that uses in a first place moving agent detector and tracker, to extract directly from the raw images the position and trajectories of the moving agent. We then use a CNN to extract static semantics and feed it to the LSTM for jointly reasoning about the future trajectories of people in a crowded space. This architecture, which we refer to as the Space-Time Network (because it encodes information both in time and space to predict trajectories of people in the future), can automatically learn typical interactions that take place among trajectories. This model leverages existing human trajectory datasets without the need for any additional annotations to learn common sense rules and conventions that humans observe in while moving in any kind of environment.

## 2. Related work

Methods to forecast human navigation can be grouped into two categories: the ones modeling the dynamic content, *human-human* interactions, and the ones focusing on the static scene, *human-space* interactions. We briefly present an overview of past works for both approaches. We also discuss relevant Recurrent Neural Network (RNN) models for sequence prediction tasks.

**Human-human interactions.** Helbing and Molnar [24] presented a pedestrian motion model with attractive and repulsive forces referred to as the *Social Force* model. This has been shown to achieve competitive results even on modern pedestrian datasets [39, 49]. This method was later extended to robotics [41] and activity understanding [43, 72, 50, 38, 37, 9, 10].

Similar approaches have been used to model human-human interactions with strong priors for the model. Treuille *et. al.* [60] use continuum dynamics, Antonini *et. al.* [3] propose a Discrete Choice framework and Wang *et. al.* [67], Tay *et. al.* [59] use Gaussian processes. Such functions have also been used to study stationary groups [73, 48]. These works target smooth motion paths and do not handle the problems associated with discretization.

Another line of work uses well-engineered features and attributes to improve tracking and forecasting. Alahi *et. al.* [1] presented a social affinity feature by learning from human trajectories in crowd their relative positions, while Yu *et. al.* [73] proposed the use of human-attributes to improve

216 forecasting in dense crowds. They also use an agent-based  
217 model similar to [6]. Rodriguez et al. [54] analyze videos  
218 with high-density crowds to track and count people.

219 Most of these models provide hand-crafted energy po-  
220 tentials based on relative distances and rules for specific  
221 scenes. In contrast, we propose a method to learn human-  
222 human interactions in a more generic data-driven fashion.

223 **Human-space interactions.** Human-space models try to  
224 predict the motion and/or action to be carried out by peo-  
225 ple in a video using the static space information. A large  
226 body of work learns motion patterns through clustering tra-  
227 jectories [26, 30, 46, 77]. More approaches can be found in  
228 [45, 52, 34, 4, 15, 33]. Kitani *et. al.* in [32] use *Inverse*  
229 *Reinforcement Learning* to predict human paths in static  
230 scenes. They infer walkable paths in a scene by modeling  
231 human-space interactions. Walker in [66] predict the behav-  
232 ior of generic agents (*e.g.*, a vehicle) in a visual scene given  
233 a large collection of videos. Ziebart et al. [79, 23] presented  
234 a planning based approach.

235 Turek [61, 40] used a similar idea to identify the func-  
236 tional map of a scene. Other approaches like [27, 18, 42, 36]  
237 showed the use of scene semantics to predict goals and paths  
238 for human navigation. Scene semantics has also been used  
239 to predict multiple object dynamics [16, 36, 34, 28]. These  
240 works are mostly restricted to the use of static scene infor-  
241 mation to predict human motion or activity. In our work,  
242 we focus on modeling dynamic crowd interactions for path  
243 prediction.

244 More recent works have also attempted to predict future  
245 human actions. In particular, Ryoo *et. al.* [55, 8, 69, 65,  
246 44, 58] forecast actions in streaming videos. More relevant  
247 to our work, is the idea of using a RNN model to predict  
248 future events in videos [53, 57, 64, 56, 31]. Along similar  
249 lines, we predict future trajectories in scenes.

250 **CNN and LSTM models for sequence prediction.** Re-  
251 cently Recurrent Neural Networks (RNN) and their vari-  
252 ants including Long Short Term Memory (LSTM) [25] and  
253 Gated Recurrent Units [12] have proven to be very suc-  
254 cessful for sequence prediction tasks. : speech recogni-  
255 tion [20, 11, 13], machine translation [5], .At the same time  
256 both standalone Convolutional Neural Networks have also  
257 shown some success in these tasks. However where these  
258 architectures best shine is when they are part of a hybrid  
259 model that uses the advantages of both LSTMs and CNNs.  
260 image/video classification [7, 21, 68, 47], human dynamics  
261 [17] and caption generation [62, 29, 74, 14, 71] to name a  
262 few. RNN models have also proven to be effective for tasks  
263 with densely connected data such as semantic segmentation  
264 [76], scene parsing [51] and even as an alternative to Con-  
265 volutional Neural Networks [63]. These works show that  
266 RNN models are capable of learning the dependencies be-

270 tween spatially correlated data such as image pixels. This  
271 motivates us to extend the sequence generation model from  
272 Graves et al. [19] to our setting. In particular, Graves et  
273 al. [19] predict isolated handwriting sequences; while in  
274 our work we jointly predict multiple correlated sequences  
275 corresponding to human trajectories.

### 276 3. Our Method - Space Time Network 277

278 The interplay between the static and dynamic content of  
279 a scene guides human navigation. For instance, a person  
280 can decide to turn because (s)he arrives at an intersection or  
281 needs to avoid a group of people moving towards him. Such  
282 deviation in trajectory cannot be predicted by observing the  
283 person’s past behavior in isolation.

284 This motivates our work to jointly model the static sur-  
285 rounding of a target in addition to its dynamic one. In this  
286 section, we describe our model that uses CNN to learn a  
287 representation from the static surrounding combined with  
288 LSTM-based architecture to predict the trajectories of any  
289 target in a scene.

#### 290 3.1. Problem formulation 291

292 We aim to predict the trajectory of a target given its ob-  
293 served short-term motion and surrounding visual informa-  
294 tion. Each scene is first preprocessed to obtain the spa-  
295 tial coordinates of the all moving targets at different time-  
296 instants using a MTT algorithm. . At any time-instant  
297  $t$ , the  $i^{th}$  target in the scene is represented by his/her xy-  
298 coordinates  $(x_t^i, y_t^i)$  and its surrounding raw image (a crop  
299 rectangular image of  $100 m^2$  centered on the target). We  
300 observe the positions of all the targets from time 1 to  $T_{obs}$ ,  
301 and predict their positions for time instants  $T_{obs+1}$  to  $T_{pred}$ .

302 This task is similar to a sequence generation problem  
303 [19], where the input sequence corresponds to the cropped  
304 images of a target and the output sequence denotes his/her  
305 future positions at different time-instants.

#### 306 3.2. Recurrent convolutional architecture - Space 307 Time Network 308

309 Every target has a different motion pattern: they move  
310 with different velocities, acceleration and have different  
311 gaits. We need a model which can understand such target-  
312 specific motion properties from a limited set of initial ob-  
313 servations.

314 We expect the hidden states of an LSTM to capture these  
315 time varying motion-properties, and we expect the CNN  
316 to extract rich scene semantic features that tells the LSTM  
317 how targets are interacting with the space around them. We  
318 jointly train this model to be robust towards saliency in both  
319 time and space domain.

320 We prove empirically that this is indeed the case and  
321 that the model is able to predict turns that are not heuristic  
322

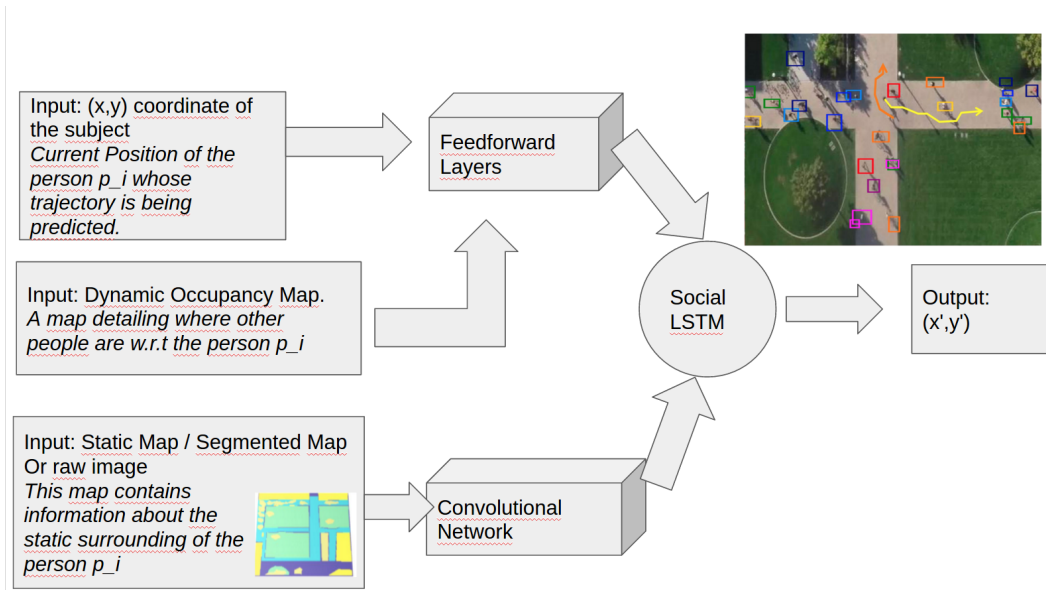


Figure 2. An overview of the hybrid CNN-LSTM model called the Space Time Network

based and are dependent on human reasoning about space and time around them.

In order to jointly reason across multiple people, we share the states between neighboring LSTMs. This introduces a new challenge: every person has a different number of neighbors and in very dense crowds [2], this number could be prohibitively high. Hence, we need a compact representation which combines the information from all neighboring states. We handle this by using neighborhood pooling layers. At every time-step, the LSTM cell receives pooled hidden-state information from the LSTM cells of neighbors as well as a vector representing features of the static scene around them from the CNN. While pooling the information, we try to preserve the spatial information through grid based pooling as explained below.

The hidden state  $h_t^i$  of the LSTM at time  $t$  captures the latent representation of the  $i^{th}$  person in the scene at that instant. This representation is shared with neighbors by building a neighborhood hidden-state tensor  $H_t^i$ . Given a hidden-state dimension  $D$ , and neighborhood size  $N_o$ , there is a  $N_o \times N_o \times D$  tensor  $H_t^i$  for the  $i^{th}$  trajectory:

$$H_t^i(m, n, :) = \sum_{j \in N_i} \mathbf{1}_{mn}[x_t^j - x_t^i, y_t^j - y_t^i] h_{t-1}^j \quad (1)$$

where  $h_{t-1}^j$  is the hidden state of the LSTM corresponding to the  $j^{th}$  person at  $t-1$ ,  $\mathbf{1}_{mn}[x, y]$  is an indicator function to check if  $(x, y)$  is in the  $(m, n)$  cell of the grid, and  $N_i$  is the set of neighbors corresponding to person  $i$ . The pooled

neighborhood hidden-state tensor is embed into a vector  $a_t^i$  and the co-ordinates into  $e_t^i$ .

Also we embed the scene around the person  $i$  as  $c_t^i$  using a convolutional network architecture. These embeddings are concatenated and used as the input to the LSTM cell of the corresponding trajectory at time  $t$ . This introduces the following recurrence:

$$\begin{aligned} r_t^i &= \phi(x_t^i, y_t^i; W_r) \\ e_t^i &= \phi(a_t^i, H_t^i; W_e) \\ c_t^i &= CNN(c_t^i; W_c) \\ h_t^i &= \phi(a_t^i, h_{t-1}^i, e_t^i, c_t^i; W_l) \end{aligned}$$

where  $\phi(\cdot)$  is an embedding function with ReLU non-linearity,  $W_r$  and  $W_e$  and  $W_c$  are embedding weights. The LSTM weights are denoted by  $W_l$ .

## 4. Campus Dataset

We aim to learn the remarkable human capability to navigate in complex and crowded scenes. Existing datasets mainly capture the behavior of humans in spaces occupied by a single class of object, e.g., pedestrian-only scenes [49, 39, 1]. However, in practice, pedestrians share the spaces with other classes of objects such as bicyclists, or skateboarders to name a few. For instance, on university campuses, a large variety of these objects interacts at peak hours. We want to study social navigation in these complex and crowded scenes occupied by several classes of objects.

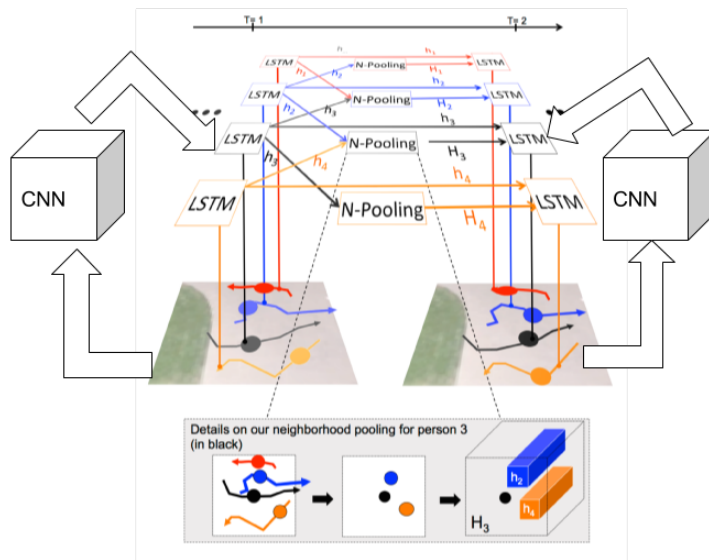


Figure 3. A more in depth representation of the Space Time Network. The Convolutional Networks are given as input a small local patch of space around the object that we want to predict the future of motion for. It is the CNNs job to extract information from these images to provide as input to the LSTM. Additional the LSTM given as input the occupancy map of people around it that indicates where people are moving with respect to the persons current position and also the current (x,y) co-ordinates of the person whose future trajectory is being predicted. We use a separate LSTM network for each trajectory in a scene. The LSTMs are then connected to each other through a neighborhood pooling (N- pooling) layer. Unlike the traditional LSTM, this pooling layer allows spatially proximal LSTMs to share information with each other. The variables in the figure are explained in Eq. 2. The bottom row shows the N-pooling for one person in the scene. The hidden-states of all LSTMs within a certain radius are pooled together and used as an input at the next time-step

To the best of our knowledge, we have collected the first large-scale dataset that has images and videos of various types of targets interacting in a real-world university campus. Our dataset captures the following types of interactions:

- target-target interactions, *e.g.*, a bicyclist avoiding a pedestrian,
- target-space interactions, *e.g.*, a skateboarder turning around a roundabout.

**Target-target interactions** We say that two targets interact when their collision energy (described by [49]) is non-zero, *e.g.*, a pedestrian avoiding a skateboarder. These interactions involve multiple physical classes of targets (pedestrians, bicyclists, or skateboarders to name a few), resulting into 185K annotated target-target interactions. We intentionally collected data at peak hours (between class breaks

Dataset	Frames	Targets	Interactions	Physical class
ISENGARD	134079	2044	6472	6
HOBBITON	138513	3821	14084	6
EDORAS	47864	1186	4684	5
MORDOR	139364	4542	68459	6
FANGORN	249967	3126	45520	6
THE VALLEY	219712	4845	46062	6
TOTAL	929499	19564	185281	6

Table 1. Our campus dataset characteristics. We group the scenes and refer to them using fictional places from the "Lord of the Rings".

in our case) to observe high density crowds. For instance, during a period of 20 seconds, we observe in average from 20 to 60 targets in a scene (of approximately  $900m^2$ ).

**Target-space interactions.** We say that a target interacts with the space when its trajectory deviates from a linear one

in the absence of other targets in its surrounding, *e.g.*, a skateboarder turning around a roundabout. To further analyze these interactions, we also labeled the scene semantics of more than 100 static scenes with the following labels: road, roundabout, sidewalk, grass, building, and bike rack (see Figure 4). We have approximately 40k “target-space” interactions.

To the best of our knowledge, it is the first dataset to depict complex interactions at such a scale. Tables 1 and 2 present more details on our collected dataset. The scenes are grouped into 6 areas based on their physical proximity on campus. The dataset comprises more than 19K targets consisting of 11.2K pedestrians, 6.4K bicyclists, 1.3k cars, 0.3K skateboarders, 0.2K golf carts, and 0.1K buses.

Each scene is captured with a 4k camera mounted on a quadrotor platform hovering above various intersections on a University campus at an altitude of approximately eighty meters. The videos are also available for further research in detection, recognition, tracking from UAV data. The videos have been processed (*i.e.* undistorted and stabilized), and annotated with their class label and their trajectory in time and space is identified.

Our dataset can be used to conduct research in activity and scene understanding. For example, the collected trajectories can be used to infer the functionality map of a scene [22, 70, 78, 35], *e.g.*, infer sitting areas, and improve image segmentation. We envision our dataset to be an ideal testbed for pushing the limits of visually intelligent machines. It enables the design of new methods that allow learning multi-target interactions at a large scale as well as pushing research on multi-target tracking.

Dataset	Bi	Ped	Skate	Carts	Car	Bus
ISENGARD	1004	926	57	19	23	15
HOBBITON	163	2493	24	18	1065	58
EDORAS	224	956	2	2	2	0
MORDOR	2594	1492	111	154	165	26
FANGORN	1017	1991	50	30	27	11
THE VALLEY	1362	3358	89	21	10	5
TOTAL	6364	11216	333	244	1292	115

Table 2. Details on the number of objects in our campus dataset. Bi = bicyclist, Ped = pedestrian, Skate = skateboarders.

## 5. Results and Experiments

### 5.1. Training

We train the our architecture the Space-Time Network on three different settings. We use two different kinds of trajectories. 1) we produce synthetic trajectories by simulating an number of pedestrians, using a Social Force model. We made this model “multi-class” by using 3 different sets of Social Parameters. 2) We use real world trajectories captured from the campus dataset. Also we use

two different type of backgrounds. 1) black and white , walkable and non walkable, image patches prepared from intuitive understanding of scene semantics, *i.e.* cross roads, bridges etc, and trajectories overlayed on the map based on social-force principles. 2) Real world images of places from the campus dataset that are pre-segmented using .

Thus we experiment on three datasets whose description are as follows:- 1) Data1: black and white (walkable , non-walkable) regions with synthetic trajectories. 2) Data2: Pre-Segmented static scene map from campus dataset with synthetic trajectories. 3) Data3: Pre-Segmented static scene map from campus dataset with real world trajectories also from the campus dataset. The following is summarization of the experiments and the results we got:

Some of the models in the above table are detailed below. A baseline-LSTM is a vanilla LSTM model with 256 hidden units and tanh activations. The ‘social’ LSTM model is the LSTM model that associates a LSTM cell to each of pedestrain walking in the scene. This LSTM model does not take as input the static segmented scene map as input. Each of these LSTM communicates with the other LSTM by way of sharing weights and also by the ‘neighborhood’ pooling layer that is explained above. These LSTMs also use 256 hidden units in its cell. The Feedforward Space-Time Network uses a feedforward layer instead of the convolutional neural netowrk to extract static scene semantics. The segegmented scene is passed through 3 feedforward ReLU layers (4096,1025,256) to extract semantic information about the human-space interactions. The best performing model is the Space-Time Network model that replaces the feedforward layers in the above Feedforward social LSTM model with a 6 layeres Convolutional Neural Network with the following architectural details. (Conv-BN-Relu-Pool)\*2 — (Conv-Relu-Pool) — Feedforward\*3.

## 6. Conclusion

We have presented a hybrid model called Space-Time Network that can jointly reason across multiple individuals to predict human trajectories in a scene. We use one LSTM for each trajectory and share the information between the LSTMs through the a neighborhood pooling layer. We also extract static scene semantics using a convolutional neural network. Our proposed model outperforms state-of-the-art methods on publicly available datasets. In addition, we qualitatively show that our model successfully predicts various non-linear behaviors arising from social interactions as well as human-space interactions Future work will extend our model to multi-class settings where several objects such as bicycles, skateboards, carts, and pedestrians share the same space. Each object will have its own label in the occupancy map.

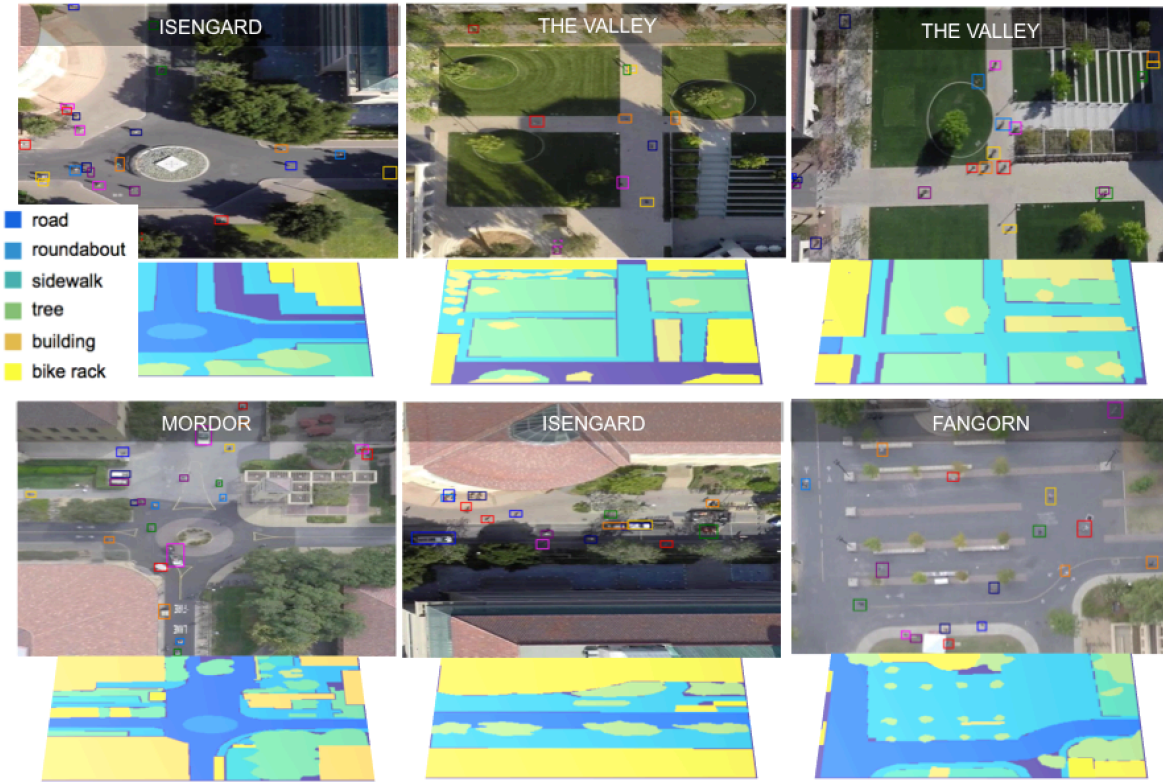


Figure 4. Some examples of the scenes captured in our dataset. We have annotated all the targets (with bounding boxes) as well as the static scene semantics (rows 2, 4, and 6). The color codes associated to target bounding boxes represents different track IDs.

Experiment	Dataset					
	Data1		Data2		Data3	
	NLL	AD Err	NLL	AD Err	NLL	AD Err
Baseline LSTM	3.3614	5.3259	5.5124	7.8951	6.2158	8.9657
Social-LSTM w/o static scene map	1.9524	2.1985	3.5548	4.0370	3.7804	4.9935
Space-Time Network (feedforward)	-2.1578	0.9882	-1.2208	1.2015	-1.0632	1.4429
Space-Time Network (CNN)	-10.215	0.5547	-8.8521	0.6215	-8.6004	0.2854

Table 3. Quantitative Results (AD-Err holds for the Average Displacement error in meters between the predicted trajectory and the ground truth for synthetic data)

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Figure 5.

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