Reparameterization of Complex Geological Models Using Neural Style Transfer

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Introduction

In the field of reservoir engineering, lower dimensional reparameterization for complex geological models is an important but challenging problem. Properties for complex geological models such as facies are non-Gaussian. Existing methods such as principal component analysis (PCA) and optimization-based PCA (O-PCA) need improvement especially for unconditional models [1].

In this study, we explore the application of neural style transfer for the reparameterization of non-Gaussian geological models. Our idea is to use the neural style transfer algorithm as a post-processing step after traditional PCA transformation. The purpose is to apply the neural style transfer algorithm to transfer the Gaussian-like PCA model to match the style of the original non-Gaussian model.

Methodology



y

 y_c

Content Target

Loss Network (VGG-16)

x

Input

Image

Image Transform Net

original model as style image **CNN-PCA:** Perform O-PCA to further post-process the model **O-PCA: Post-processed Reservoir Models**



PCA model

Ø

 $\phi, relu3_3$

feat

Procedures & Equations

Perform PCA on original models to reduce dimension

$$X_c = \begin{bmatrix} \mathbf{m}_1 - \bar{\mathbf{m}} & \mathbf{m}_2 - \bar{\mathbf{m}} & \dots & \mathbf{m}_{N_r} - \bar{\mathbf{m}} \end{bmatrix}$$
$$X_c = \sqrt{N_r - 1}U\Sigma V^T = \sqrt{N_r - 1}\Phi V^T$$

$$\mathbf{n} = \Phi \boldsymbol{\xi} + \bar{\mathbf{m}}$$

PCA:

Perform neural style transfer using PCA model as content image,

$$\begin{split} L_{\rm t} &= \sum_{l=1}^{L} \alpha_l L_{\rm c}^l + \lambda \sum_{l=1}^{L} \beta_l L_{\rm s}^l + \omega L_{\rm h}, \\ L_{\rm c}^l &= \frac{1}{2N_l D_l} \sum_{ij} (F_l[O] - F_l[I])_{ij}^2, \\ L_{\rm s}^l &= \frac{1}{2N_l^2} \sum_{ij} (G_l[O] - G_l[S])_{ij}^2. \\ L_{\rm h} &= \sum_{ij} h_{ij} (I - O)_{ij}^2. \end{split}$$

Total loss

Style loss

Well data loss

$$\mathbf{m} = \underset{\mathbf{x}}{\operatorname{argmin}} \Big\{ ||\Phi \boldsymbol{\xi} + \bar{\mathbf{m}} - \mathbf{x}||_{2}^{2} + \gamma \mathbf{x}^{T} (\mathbf{1} - \mathbf{x}) \Big\}, x_{i} \in [0, 1].$$



- **O-PCA** result
- **CNN PCA result**



Conclusions

- Applied both neural style transfer and fast neural style transfer algorithm for reservoir reparameterization problem.
- Included hard data loss in the style transfer algorithm to ensure that output model honors hard data.
- The CNN-PCA algorithm outperforms O-PCA method in terms of preserving channel connectivity and flow statistics, especially for unconditional models.

Reference

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[3] H.X. Vo and L.J. Durlofsky. A new differentiable parameterization based on principal component analysis for the low-dimensional representation of complex geological models. *Mathematical Geosciences*, 46(7):775–813, 2014.

