Lecture 13: Generative Models

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 13 - 1 May 18, 2017

Administrative

Midterm grades released on Gradescope this week

A3 due next Friday, 5/26

HyperQuest deadline extended to Sunday 5/21, 11:59pm

Poster session is June 6

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Lecture 13 - 2 May 18, 2017

Overview

- Unsupervised Learning
- Generative Models
 - PixelRNN and PixelCNN
 - Variational Autoencoders (VAE)
 - Generative Adversarial Networks (GAN)

Lecture 13 -

3

May 18, 2017

Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

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Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.





Classification

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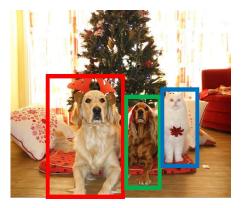
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Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.



DOG, DOG, CAT

Object Detection

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Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.



TREE, SKY

Semantic Segmentation

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Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.



A cat sitting on a suitcase on the floor

Image captioning

Caption generated using <u>neuraltalk2</u> <u>Image</u> is <u>CC0 Public domain</u>.

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Unsupervised Learning

Data: x Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

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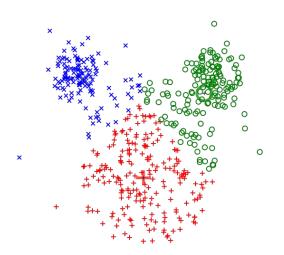
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Unsupervised Learning

Data: x Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.



K-means clustering

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Unsupervised Learning

Data: x Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

original data space

3-d

Principal Component Analysis (Dimensionality reduction)

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2-d

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Reconstructed data Unsupervised Learning L2 Loss function: $\|x - \hat{x}\|^2$ Reconstructed Just data, no labels! \hat{x} input data Encoder: 4-layer conv Decoder Decoder: 4-layer upconv **Goal**: Learn some underlying Features zhidden structure of the data Encoder Input data \boldsymbol{x} **Examples**: Clustering, dimensionality reduction, feature Autoencoders learning, density estimation, etc.

(Feature learning)

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Data: x

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Input data

Unsupervised Learning

Data: x Just data, no labels!

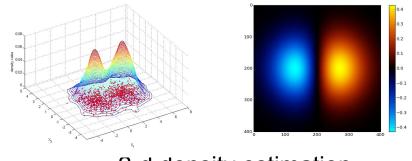
Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.



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1-d density estimation



2-d density estimation

2-d density images left and right are CC0 public domain

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Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc. **Unsupervised Learning**

Data: x Just data, no labels!

Goal: Learn some underlying hidden *structure* of the data

Examples: Clustering, dimensionality reduction, feature learning, density estimation, etc.

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Supervised Learning

Data: (x, y) x is data, y is label

Goal: Learn a *function* to map x -> y

Examples: Classification, regression, object detection, semantic segmentation, image captioning, etc.

Unsupervised Learning

Training data is cheap Data: x Holy grail: Solve unsupervised learning Just data, no labels! => understand structure of visual world Goal: Learn some underlying hidden structure of the data **Examples**: Clustering, dimensionality reduction, feature

learning, density estimation, etc.

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Generative Models

Given training data, generate new samples from same distribution





Training data ~ $p_{data}(x)$ Generated samples ~ $p_{model}(x)$ Want to learn $p_{model}(x)$ similar to $p_{data}(x)$

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Generative Models

Given training data, generate new samples from same distribution

+



Training data ~ $p_{data}(x)$ Generated samples ~ $p_{model}(x)$

Want to learn $p_{model}(x)$ similar to $p_{data}(x)$

Addresses density estimation, a core problem in unsupervised learning **Several flavors:**

- Explicit density estimation: explicitly define and solve for p_{model}(x)
- Implicit density estimation: learn model that can sample from p_{model}(x) w/o explicitly defining it

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Why Generative Models?

- Realistic samples for artwork, super-resolution, colorization, etc.



 Generative models of time-series data can be used for simulation and planning (reinforcement learning applications!)

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 Training generative models can also enable inference of latent representations that can be useful as general features

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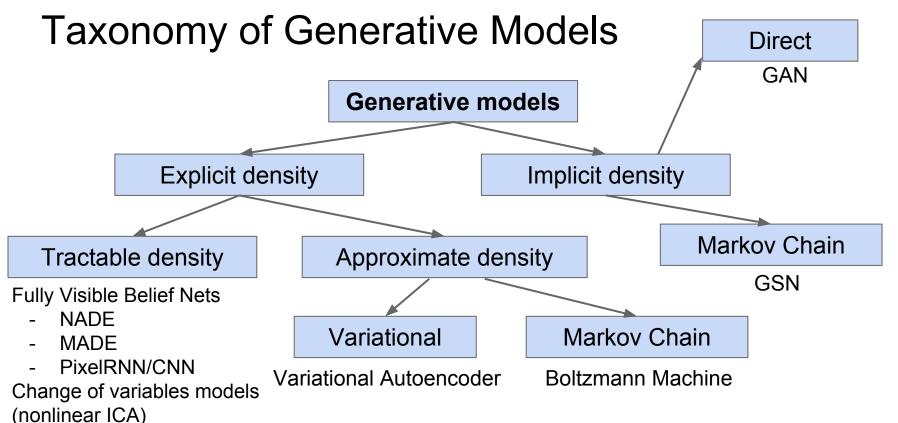


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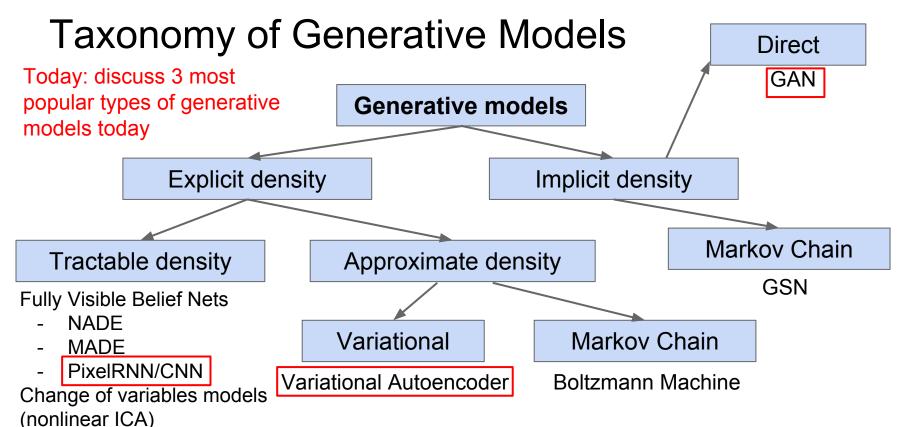


Figure copyright and adapted from Ian Goodfellow, Tutorial on Generative Adversarial Networks, 2017.

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PixelRNN and PixelCNN

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Fully visible belief network

Explicit density model

Use chain rule to decompose likelihood of an image x into product of 1-d distributions:

$$p(x) = \prod_{i=1}^{n} p(x_i | x_1, ..., x_{i-1})$$

$$\uparrow$$
Relihood of
Reprobability of i'th pixel value

Likelihood of
image xProbability of i'th pixel value
given all previous pixels

Then maximize likelihood of training data

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Fully visible belief network

Explicit density model

Use chain rule to decompose likelihood of an image x into product of 1-d distributions:

$$p(x) = \prod_{i=1}^{n} p(x_i | x_1, ..., x_{i-1})$$

$$\uparrow$$
Likelihood of image x
Probability of i'th pixel value given all previous pixels
Complex distribution over pixel values => Express using a neural network!

Then maximize

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Fully visible belief network

Explicit density model

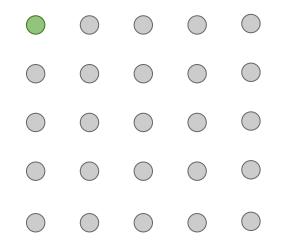
Use chain rule to decompose likelihood of an image x into product of 1-d distributions:

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Generate image pixels starting from corner

Dependency on previous pixels modeled using an RNN (LSTM)

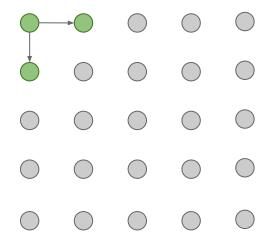


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Generate image pixels starting from corner

Dependency on previous pixels modeled using an RNN (LSTM)

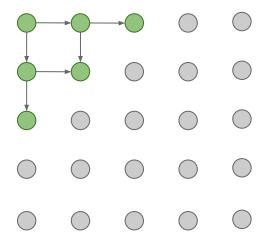


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Generate image pixels starting from corner

Dependency on previous pixels modeled using an RNN (LSTM)



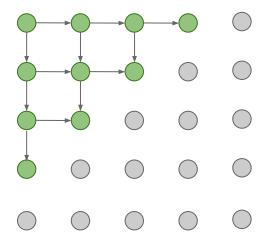
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Generate image pixels starting from corner

Dependency on previous pixels modeled using an RNN (LSTM)

Drawback: sequential generation is slow!



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Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region

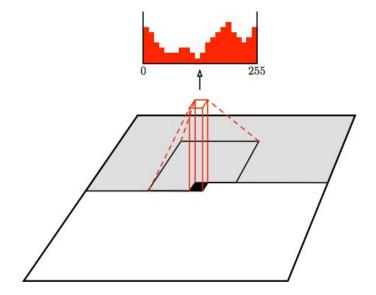


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Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region

Training: maximize likelihood of training images

$$p(x) = \prod_{i=1}^{n} p(x_i | x_1, ..., x_{i-1})$$

Softmax loss at each pixel

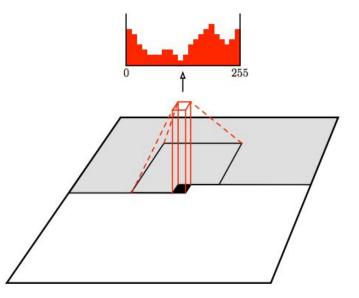


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Still generate image pixels starting from corner

Dependency on previous pixels now modeled using a CNN over context region

Training is faster than PixelRNN (can parallelize convolutions since context region values known from training images)

Generation must still proceed sequentially => still slow

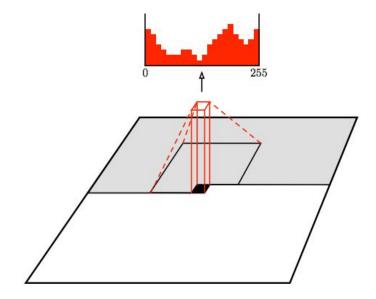
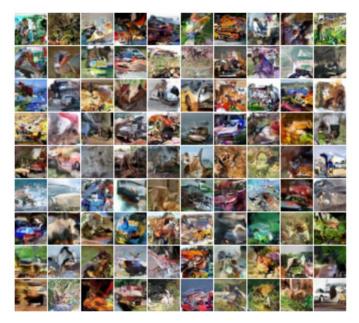


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Generation Samples







32x32 ImageNet

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PixelRNN and **PixelCNN**

Pros:

- Can explicitly compute likelihood p(x)
- Explicit likelihood of training data gives good evaluation metric
- Good samples

Con:

- Sequential generation => slow

Improving PixelCNN performance

- Gated convolutional layers
- Short-cut connections
- Discretized logistic loss
- Multi-scale
- Training tricks
- Etc...

See

- Van der Oord et al. NIPS 2016
- Salimans et al. 2017 (PixelCNN++)

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Variational Autoencoders (VAE)

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So far...

PixelCNNs define tractable density function, optimize likelihood of training data: $p_{\theta}(x) = \prod_{i=1}^{n} p_{\theta}(x_i | x_1, ..., x_{i-1})$

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So far...

PixelCNNs define tractable density function, optimize likelihood of training data: $p_{\theta}(x) = \prod_{i=1}^{n} p_{\theta}(x_i | x_1, ..., x_{i-1})$

VAEs define intractable density function with latent z:

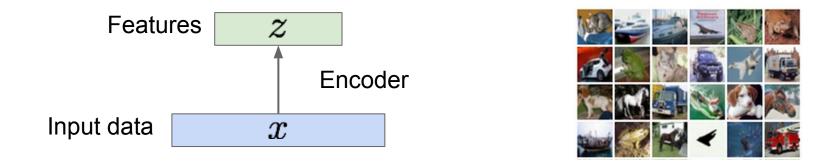
$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Cannot optimize directly, derive and optimize lower bound on likelihood instead

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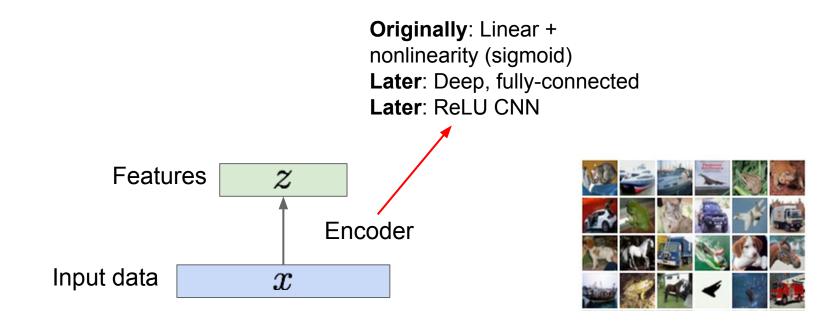
Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data



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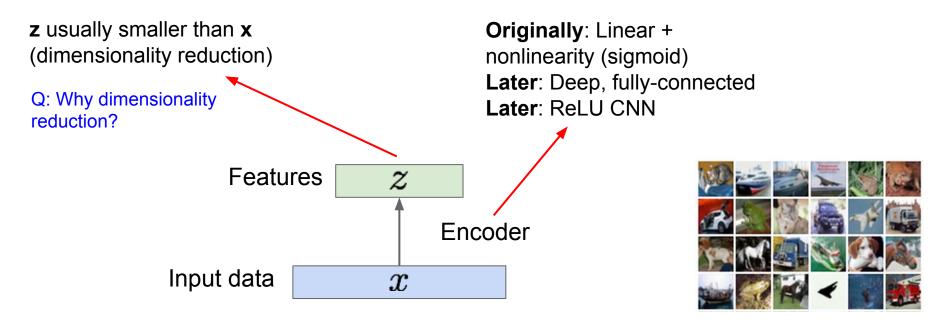
Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data



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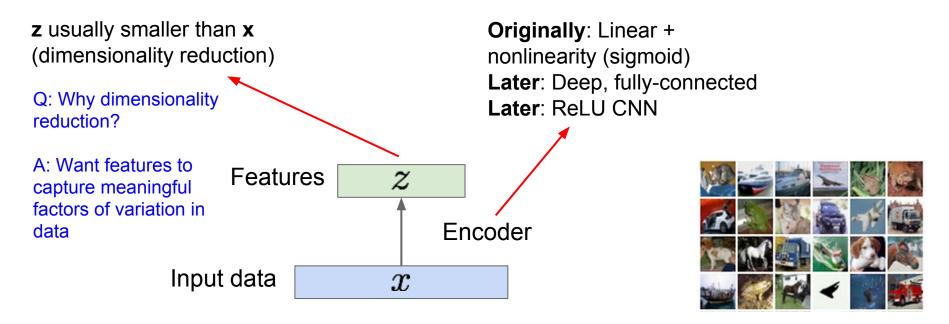
Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data



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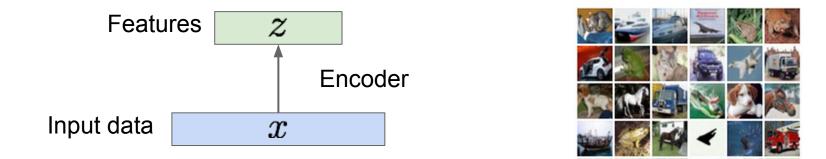
Unsupervised approach for learning a lower-dimensional feature representation from unlabeled training data



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How to learn this feature representation?

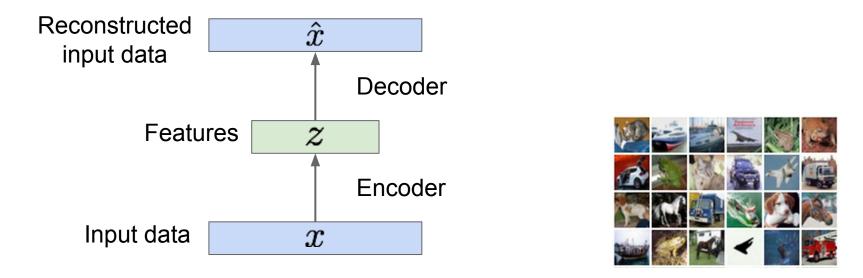


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How to learn this feature representation?

Train such that features can be used to reconstruct original data "Autoencoding" - encoding itself

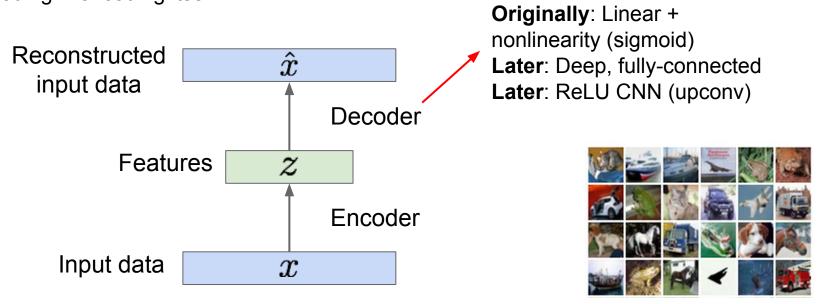


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How to learn this feature representation?

Train such that features can be used to reconstruct original data "Autoencoding" - encoding itself

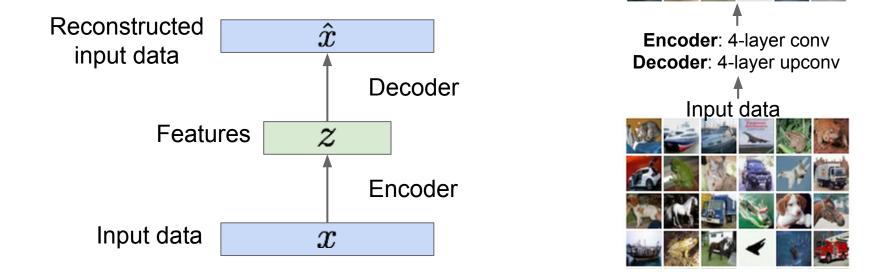


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How to learn this feature representation?

Train such that features can be used to reconstruct original data "Autoencoding" - encoding itself

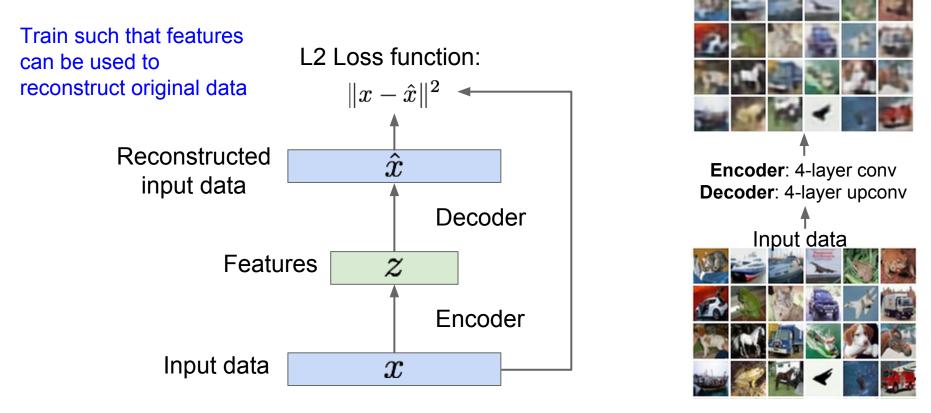


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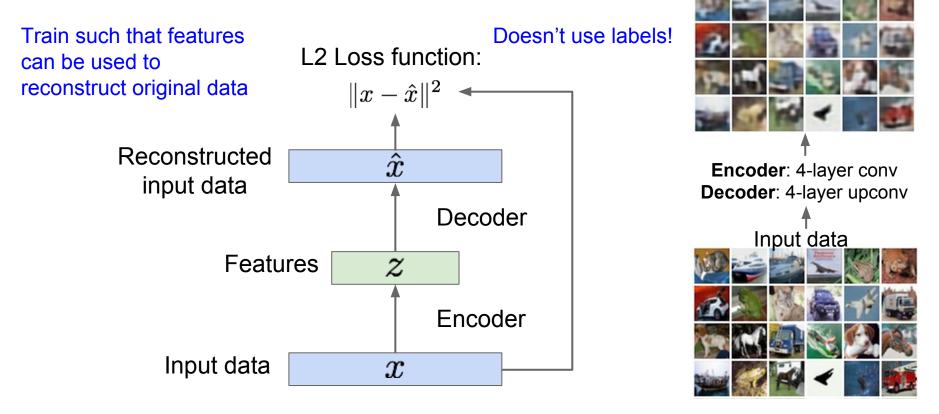
Reconstructed data

Some background first: Autoencoders Reconstructed data



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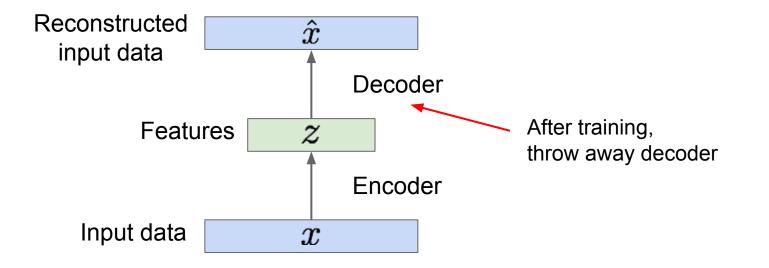
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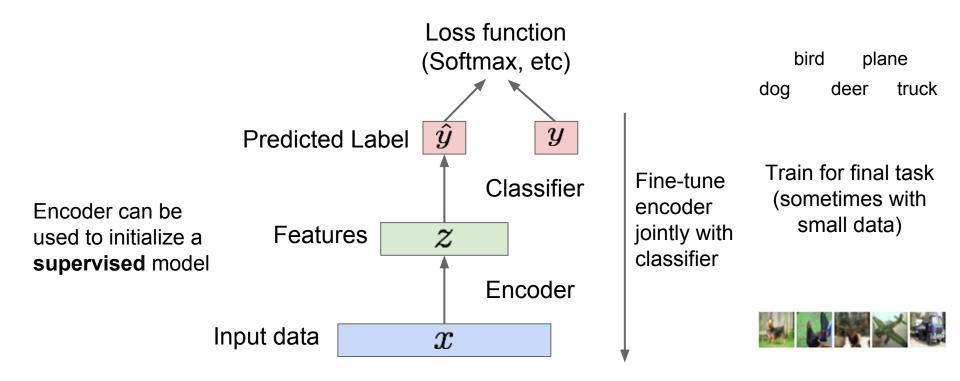
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Reconstructed data



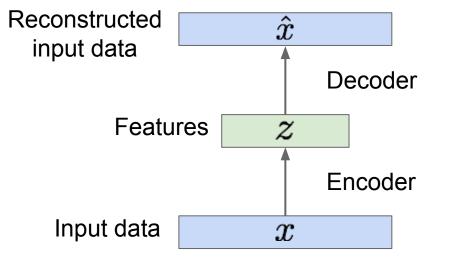
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Autoencoders can reconstruct data, and can learn features to initialize a supervised model

Features capture factors of variation in training data. Can we generate new images from an autoencoder?

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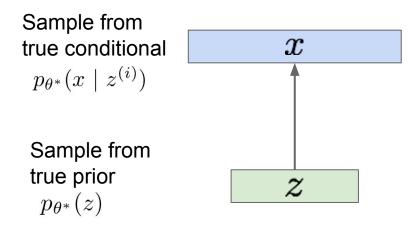
Probabilistic spin on autoencoders - will let us sample from the model to generate data!

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Probabilistic spin on autoencoders - will let us sample from the model to generate data!

Assume training data $\{x^{(i)}\}_{i=1}^N$ is generated from underlying unobserved (latent) representation **z**



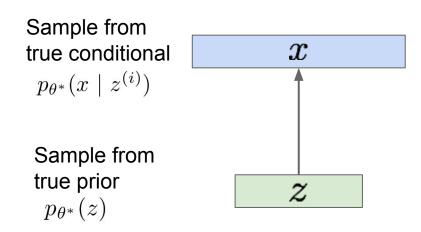
Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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Probabilistic spin on autoencoders - will let us sample from the model to generate data!

Assume training data $\{x^{(i)}\}_{i=1}^N$ is generated from underlying unobserved (latent) representation **z**



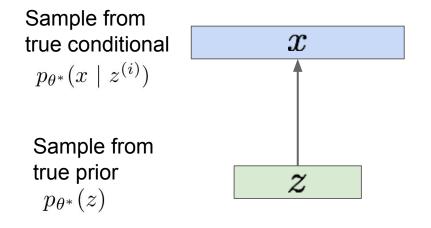
Intuition (remember from autoencoders!):x is an image, z is latent factors used to generate x: attributes, orientation, etc.

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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We want to estimate the true parameters θ^* of this generative model.



Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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Sample from
true conditional \boldsymbol{x} $p_{\theta^*}(x \mid z^{(i)})$ \boldsymbol{x} Sample from
true prior
 $p_{\theta^*}(z)$ \boldsymbol{z}

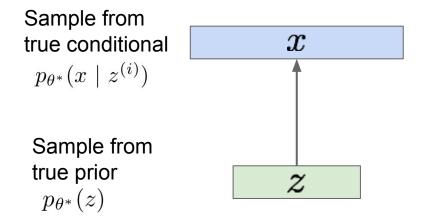
We want to estimate the true parameters θ^* of this generative model.

How should we represent this model?

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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We want to estimate the true parameters θ^* of this generative model.

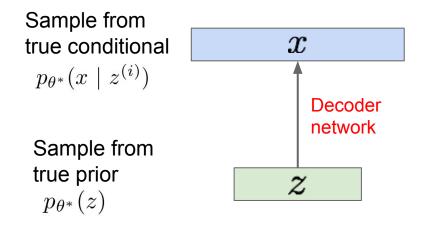
How should we represent this model?

Choose prior p(z) to be simple, e.g. Gaussian. Reasonable for latent attributes, e.g. pose, how much smile.

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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We want to estimate the true parameters θ^* of this generative model.

How should we represent this model?

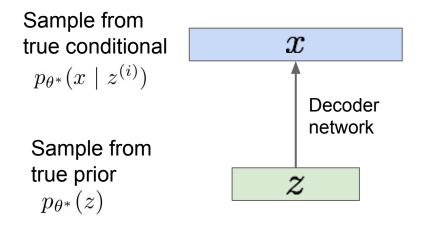
Choose prior p(z) to be simple, e.g. Gaussian.

Conditional p(x|z) is complex (generates image) => represent with neural network

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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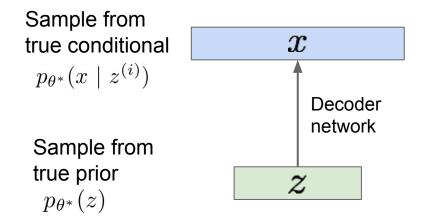
We want to estimate the true parameters θ^* of this generative model.

How to train the model?

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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We want to estimate the true parameters θ^* of this generative model.

How to train the model?

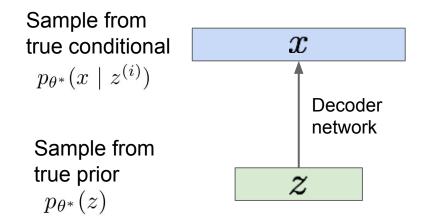
Remember strategy for training generative models from FVBNs. Learn model parameters to maximize likelihood of training data

$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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We want to estimate the true parameters θ^* of this generative model.

How to train the model?

Remember strategy for training generative models from FVBNs. Learn model parameters to maximize likelihood of training data

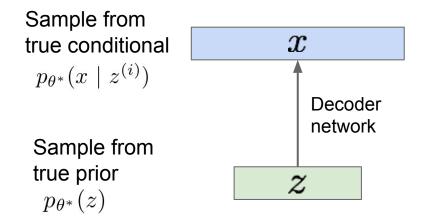
$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Now with latent z

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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We want to estimate the true parameters θ^* of this generative model.

How to train the model?

Remember strategy for training generative models from FVBNs. Learn model parameters to maximize likelihood of training data

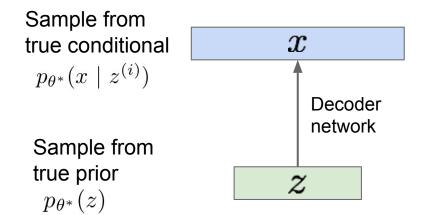
$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Q: What is the problem with this?

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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We want to estimate the true parameters θ^* of this generative model.

How to train the model?

Remember strategy for training generative models from FVBNs. Learn model parameters to maximize likelihood of training data

$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Q: What is the problem with this?

Intractable!

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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Data likelihood: $p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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Data likelihood: $p_{\theta}(x) = \int p_{\theta}(z)p_{\theta}(x|z)dz$ Simple Gaussian prior

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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Data likelihood: $p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$

Decoder neural network

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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Data likelihood:
$$p_{\theta}(x) = \int p_{\theta}(z)p_{\theta}(x|z)dz$$

Intractible to compute $p(x|z)$ for every z!

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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Variational Autoencoders: Intractability Data likelihood: $p_{\theta}(x) = \int p_{\theta}(z)p_{\theta}(x|z)dz$

Posterior density also intractable: $p_{\theta}(z|x) = p_{\theta}(x|z)p_{\theta}(z)/p_{\theta}(x)$

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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Variational Autoencoders: Intractability Data likelihood: $p_{\theta}(x) = \int p_{\theta}(z)p_{\theta}(x|z)dz$

Posterior density also intractable: $p_{\theta}(z|x) = p_{\theta}(x|z)p_{\theta}(z)/p_{\theta}(x)$

Intractable data likelihood

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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Data likelihood: $p_{\theta}(x) = \int p_{\theta}(z)p_{\theta}(x|z)dz$

Posterior density also intractable: $p_{\theta}(z|x) = p_{\theta}(x|z)p_{\theta}(z)/p_{\theta}(x)$

Solution: In addition to decoder network modeling $p_{\theta}(x|z)$, define additional encoder network $q_{\phi}(z|x)$ that approximates $p_{\theta}(z|x)$

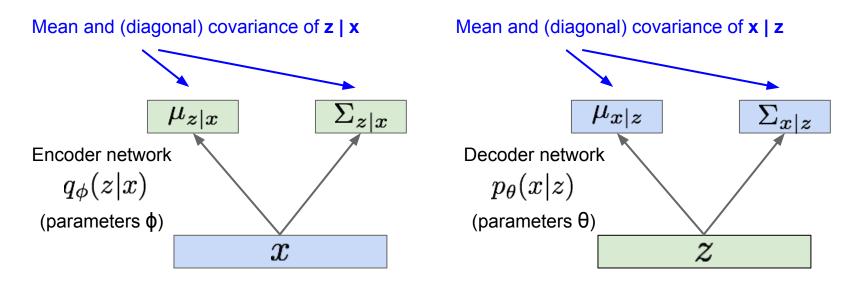
Will see that this allows us to derive a lower bound on the data likelihood that is tractable, which we can optimize

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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Since we're modeling probabilistic generation of data, encoder and decoder networks are probabilistic

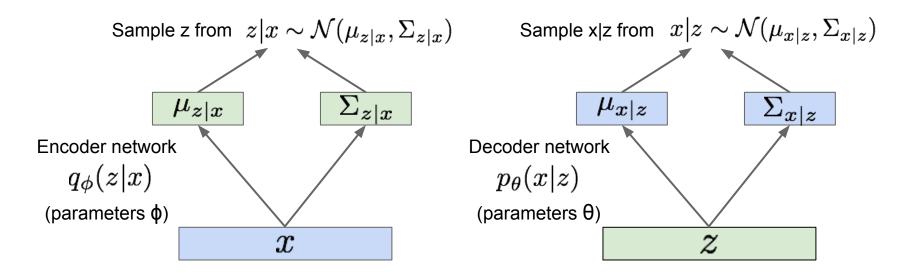


Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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Since we're modeling probabilistic generation of data, encoder and decoder networks are probabilistic

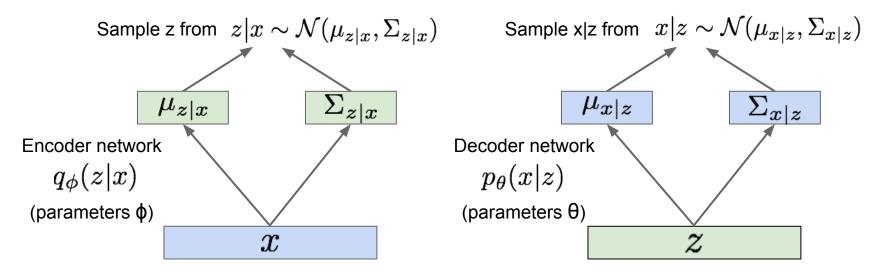


Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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Since we're modeling probabilistic generation of data, encoder and decoder networks are probabilistic



Encoder and decoder networks also called "recognition"/"inference" and "generation" networks Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

 $\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)})\right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$

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come in handy later

Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)}) \right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$
Taking expectation wrt. z
(using encoder network) will

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Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)}) \right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$
$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \right] \quad (\text{Bayes' Rule})$$

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Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)}) \right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$
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Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

$$\begin{split} \log p_{\theta}(x^{(i)}) &= \mathbf{E}_{z \sim q_{\phi}(z \mid x^{(i)})} \left[\log p_{\theta}(x^{(i)}) \right] & (p_{\theta}(x^{(i)}) \text{ Does not depend on } z) \\ &= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z) p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \right] & (\text{Bayes' Rule}) \\ &= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z) p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \frac{q_{\phi}(z \mid x^{(i)})}{q_{\phi}(z \mid x^{(i)})} \right] & (\text{Multiply by constant}) \\ &= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z)} \right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z \mid x^{(i)})} \right] & (\text{Logarithms}) \end{split}$$

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Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

$$\begin{split} \log p_{\theta}(x^{(i)}) &= \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)}) \right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z) \\ &= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \right] \quad (\text{Bayes' Rule}) \\ &= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \frac{q_{\phi}(z \mid x^{(i)})}{q_{\phi}(z \mid x^{(i)})} \right] \quad (\text{Multiply by constant}) \\ &= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z)} \right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z \mid x^{(i)})} \right] \quad (\text{Logarithms}) \\ &= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z)) + D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z \mid x^{(i)})) \end{split}$$

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Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)})\right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$

$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)}|z)p_{\theta}(z)}{p_{\theta}(z|x^{(i)})}\right] \quad (\text{Bayes' Rule})$$

$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)}|z)p_{\theta}(z)}{p_{\theta}(z|x^{(i)})}\frac{q_{\phi}(z|x^{(i)})}{q_{\phi}(z|x^{(i)})}\right] \quad (\text{Multiply by constant})$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)}|z)\right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z|x^{(i)})}{p_{\theta}(z)}\right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z|x^{(i)})}{p_{\theta}(z|x^{(i)})}\right] \quad (\text{Logarithms})$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)}|z)\right] - D_{KL}(q_{\phi}(z|x^{(i)})||p_{\theta}(z)) + D_{KL}(q_{\phi}(z|x^{(i)})||p_{\theta}(z|x^{(i)}))$$

$$The expectation wrt. z (using encoder network) let us write nice KL terms$$

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Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)}) \right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$

$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \right] \quad (\text{Bayes' Rule})$$

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$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z)} \right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z \mid x^{(i)})} \right] \quad (\text{Logarithms})$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid p_{\theta}(z)) + D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid p_{\theta}(z \mid x^{(i)})) \right]$$

$$\stackrel{\uparrow}{=} \mathbf{D}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid p_{\theta}(z)) + D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid p_{\theta}(z \mid x^{(i)})) \right]$$

$$\stackrel{\uparrow}{=} \mathbf{D}_{z} \left[\log p_{\theta}(x^{(i)} \mid z) \right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid p_{\theta}(z)) + D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid p_{\theta}(z \mid x^{(i)})) \right]$$

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Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)})\right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$

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$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)}|z)p_{\theta}(z)}{p_{\theta}(z|x^{(i)})}\frac{q_{\phi}(z|x^{(i)})}{q_{\phi}(z|x^{(i)})}\right] \quad (\text{Multiply by constant})$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)}|z)\right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z|x^{(i)})}{p_{\theta}(z)}\right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z|x^{(i)})}{p_{\theta}(z|x^{(i)})}\right] \quad (\text{Logarithms})$$

$$= \underbrace{\mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)}|z)\right] - D_{KL}(q_{\phi}(z|x^{(i)})||p_{\theta}(z))}_{\mathcal{L}(x^{(i)},\theta,\phi)} + \underbrace{D_{KL}(q_{\phi}(z|x^{(i)})||p_{\theta}(z|x^{(i)}))}_{\geq 0} \right]$$

Tractable lower bound which we can take gradient of and optimize! ($p_{\theta}(x|z)$ differentiable, KL term differentiable)

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V

Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)})\right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$

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$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)}|z)p_{\theta}(z)}{p_{\theta}(z|x^{(i)})}\frac{q_{\phi}(z|x^{(i)})}{q_{\phi}(z|x^{(i)})}\right] \quad (\text{Multiply by constant})$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)}|z)\right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z|x^{(i)})}{p_{\theta}(z)}\right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z|x^{(i)})}{p_{\theta}(z|x^{(i)})}\right] \quad (\text{Logarithms})$$

$$= \underbrace{\mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)}|z)\right] - D_{KL}(q_{\phi}(z|x^{(i)})||p_{\theta}(z)) + D_{KL}(q_{\phi}(z|x^{(i)})||p_{\theta}(z|x^{(i)}))\right]}_{>0}$$

$$= \underbrace{\mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)}|z)\right] - D_{KL}(q_{\phi}(z|x^{(i)})||p_{\theta}(z)) + D_{KL}(q_{\phi}(z|x^{(i)})||p_{\theta}(z|x^{(i)}))\right]}_{>0}$$

$$= \underbrace{\mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)}, \theta, \phi)\right]_{=\mathbf{T}}_{\mathbf{T}} \underbrace{\mathbf{E}_{z}(x^{(i)}, \theta, \phi)}_{=\mathbf{T}}_{\mathbf{T}} \underbrace{\mathbf{E}_{z}(x^{(i)}, \theta, \phi)}_{=\mathbf{T}}_{\mathbf{T}} \underbrace{\mathbf{E}_{z}(x^{(i)}, \theta, \phi)}_{=\mathbf{T}}_{\mathbf{T}} \underbrace{\mathbf{E}_{z}(x^{(i)}, \theta, \phi)}_{=\mathbf{T}}_{\mathbf{T}} \underbrace{\mathbf{E}_{z}(x^{(i)}, \theta, \phi)}_{=\mathbf{T}}_{=\mathbf{T}} \underbrace{\mathbf{E}_{z}(x^{(i)}, \theta, \phi)}_{=\mathbf{T}}_{\mathbf{T}} \underbrace{\mathbf{E}_{z}(x^{(i)}, \theta, \phi)}_{=\mathbf{T}}_{\mathbf{T}} \underbrace{\mathbf{E}_{z}(x^{(i)}, \theta, \phi)}_{=\mathbf{T}}_{\mathbf{T}} \underbrace{\mathbf{E}_{z}(x^{(i)}, \theta, \phi)}_{=\mathbf{T}}_{=\mathbf{T}} \underbrace{\mathbf{E}_{z}(x^{(i)}, \theta, \phi)}_{=\mathbf{T}}_{=\mathbf{T}}_{=\mathbf{T}} \underbrace{\mathbf{E}_{z}(x^{(i)}, \theta, \phi)}_{=\mathbf{T}}_{=\mathbf{T}}_{=\mathbf{T}} \underbrace{\mathbf{E}_{z}(x^{(i)}, \theta, \phi)}_{=\mathbf{T}}_{=\mathbf{T}}_{=\mathbf{T}} \underbrace{\mathbf{E}_{z}(x^{(i)}, \theta, \phi)}_{=\mathbf{T}}_{=\mathbf{T}}_{=\mathbf{T}}_{=\mathbf{T}}_{=\mathbf{T}}_{=\mathbf{T}} \underbrace{\mathbf{E}_{z}(x^{(i)}, \theta, \phi)}_{=\mathbf{T}}_{$$

Now equipped with our encoder and decoder networks, let's work out the (log) data likelihood:

$$\log p_{\theta}(x^{(i)}) = \mathbf{E}_{z \sim q_{\phi}(z|x^{(i)})} \left[\log p_{\theta}(x^{(i)})\right] \quad (p_{\theta}(x^{(i)}) \text{ Does not depend on } z)$$

$$= \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})}\right] \quad (\text{Bayes' Rule}) \qquad \text{Make approximate posterior distribution the input data} = \mathbf{E}_{z} \left[\log \frac{p_{\theta}(x^{(i)} \mid z)p_{\theta}(z)}{p_{\theta}(z \mid x^{(i)})} \frac{q_{\phi}(z \mid x^{(i)})}{q_{\phi}(z \mid x^{(i)})}\right] \quad (\text{Multiply by constant}) \qquad \text{close to prior}$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z)\right] - \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z)}\right] + \mathbf{E}_{z} \left[\log \frac{q_{\phi}(z \mid x^{(i)})}{p_{\theta}(z \mid x^{(i)})}\right] \quad (\text{Logarithms})$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z)\right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z)) + D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z \mid x^{(i)}))\right]$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z)\right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z)) + D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z \mid x^{(i)}))\right]$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z)\right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z)) + D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z \mid x^{(i)}))\right]$$

$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z)\right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z)) + D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z \mid x^{(i)}))\right]$$

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$$= \mathbf{E}_{z} \left[\log p_{\theta}(x^{(i)} \mid z)\right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) || p_{\theta}(z \mid x^{(i)}) || p_{\theta}(z \mid x^{(i)})\right]$$

Putting it all together: maximizing the likelihood lower bound

$$\underbrace{\mathbf{E}_{z}\left[\log p_{\theta}(x^{(i)} \mid z)\right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid\mid p_{\theta}(z))}_{\mathcal{L}(x^{(i)}, \theta, \phi)}$$

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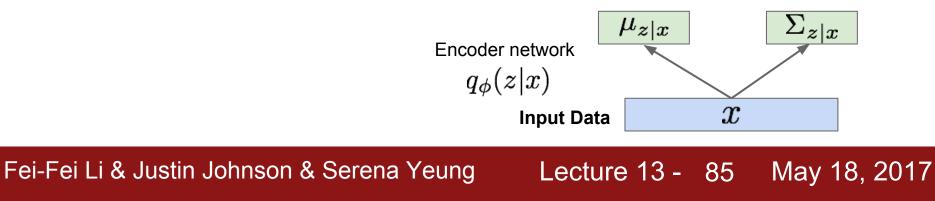
Putting it all together: maximizing the likelihood lower bound

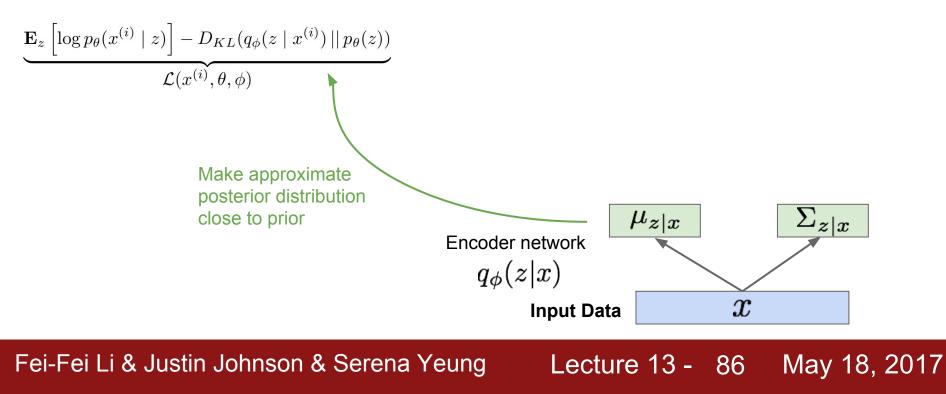
$$\underbrace{\mathbf{E}_{z}\left[\log p_{\theta}(x^{(i)} \mid z)\right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid\mid p_{\theta}(z))}_{\mathcal{L}(x^{(i)}, \theta, \phi)}$$

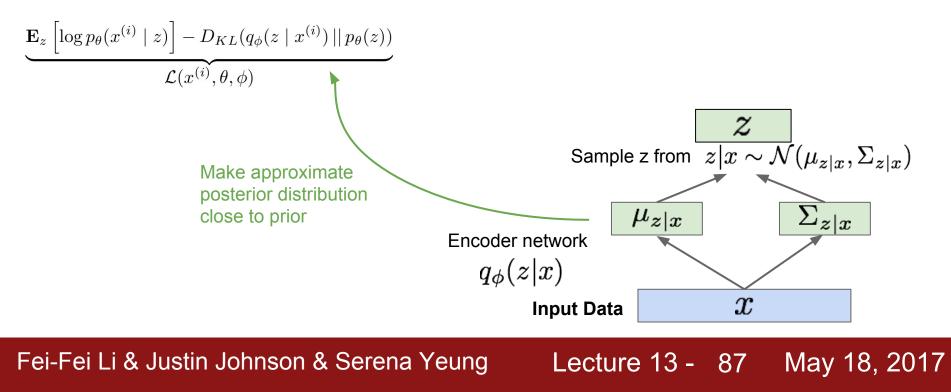
Let's look at computing the bound (forward pass) for a given minibatch of input data

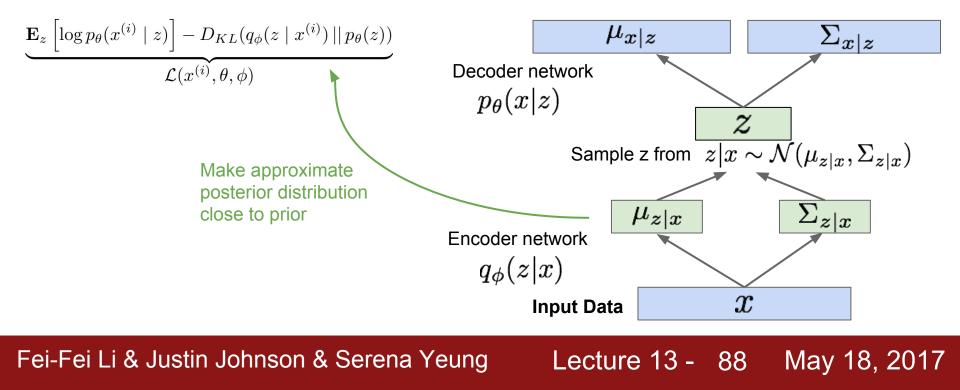


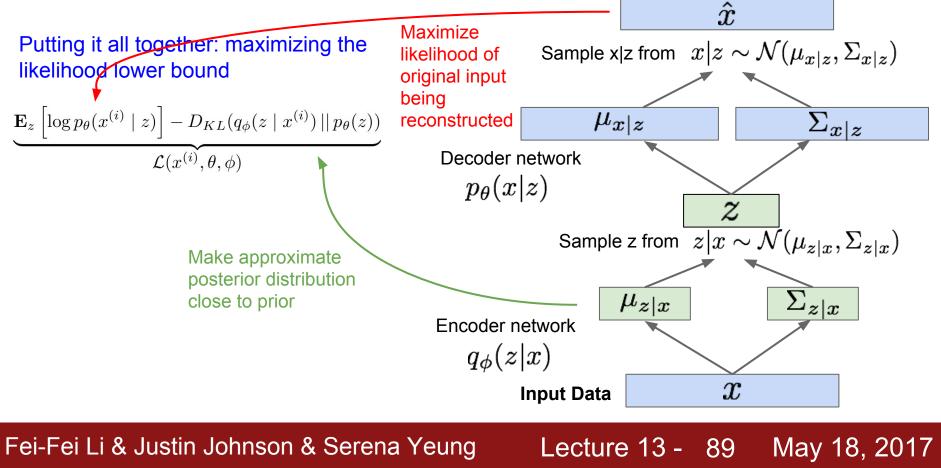
$$\underbrace{\mathbf{E}_{z}\left[\log p_{\theta}(x^{(i)} \mid z)\right] - D_{KL}(q_{\phi}(z \mid x^{(i)}) \mid\mid p_{\theta}(z))}_{\mathcal{L}(x^{(i)}, \theta, \phi)}$$

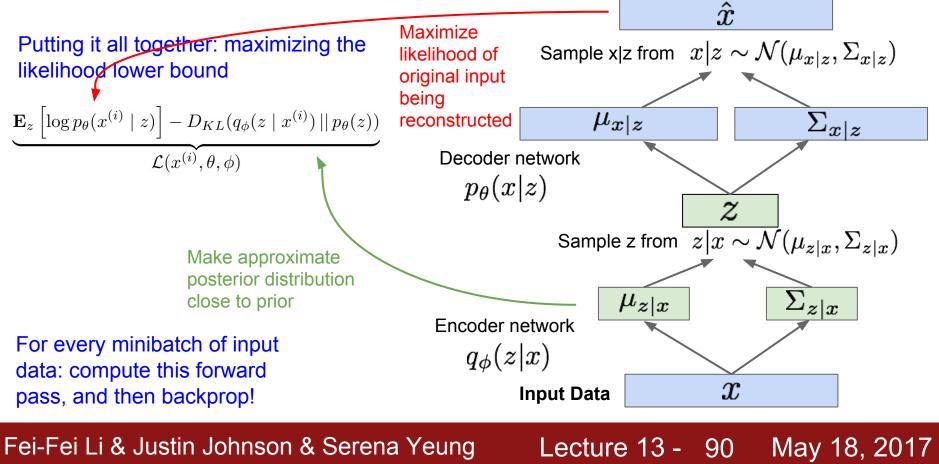




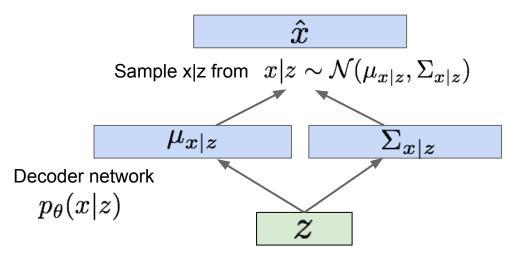








Use decoder network. Now sample z from prior!



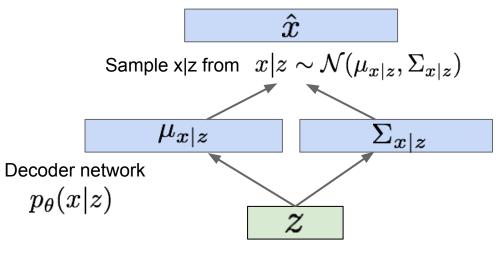
Sample z from $\, z \sim \mathcal{N}(0, I) \,$

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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Use decoder network. Now sample z from prior!



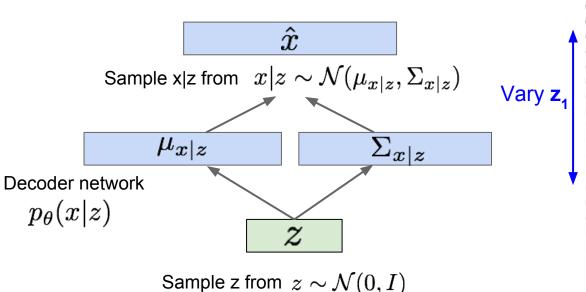
Sample z from $\, z \sim \mathcal{N}(0, I) \,$

Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

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2000000000000 5 6 6

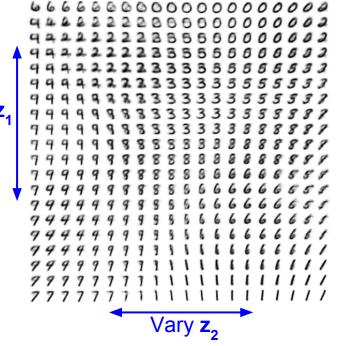
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Kingma and Welling, "Auto-Encoding Variational Bayes", ICLR 2014

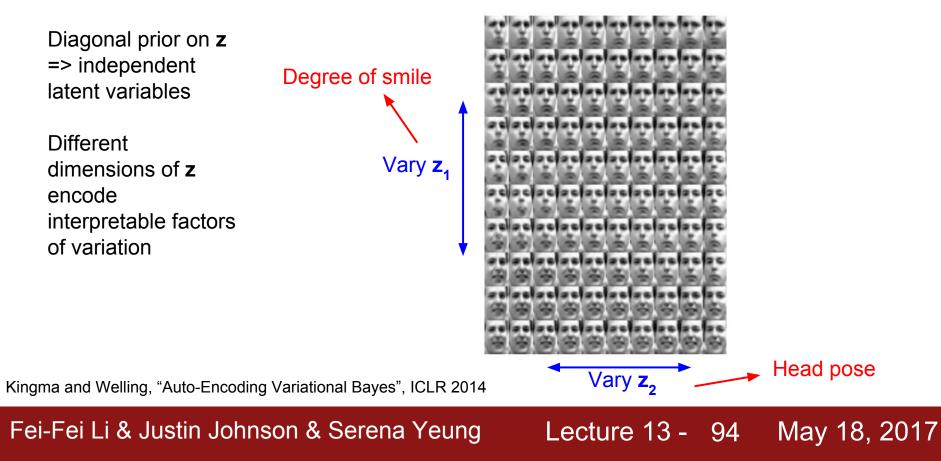
Use decoder network. Now sample z from prior!

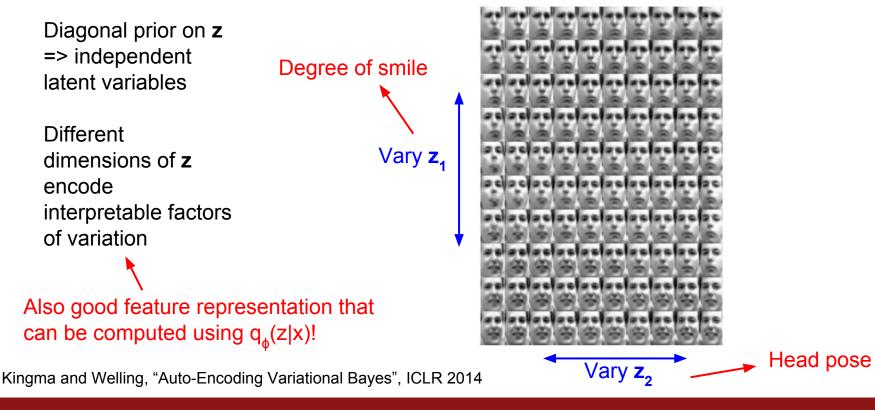
Data manifold for 2-d z



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Labeled Faces in the Wild

32x32 CIFAR-10

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Probabilistic spin to traditional autoencoders => allows generating data Defines an intractable density => derive and optimize a (variational) lower bound

Pros:

- Principled approach to generative models
- Allows inference of q(z|x), can be useful feature representation for other tasks

Cons:

- Maximizes lower bound of likelihood: okay, but not as good evaluation as PixelRNN/PixelCNN
- Samples blurrier and lower quality compared to state-of-the-art (GANs)

Active areas of research:

 More flexible approximations, e.g. richer approximate posterior instead of diagonal Gaussian

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- Incorporating structure in latent variables

Generative Adversarial Networks (GAN)

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So far...

PixelCNNs define tractable density function, optimize likelihood of training data: $p_{\theta}(x) = \prod_{i=1}^{n} p_{\theta}(x_i | x_1, ..., x_{i-1})$

VAEs define intractable density function with latent z:

$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$

Cannot optimize directly, derive and optimize lower bound on likelihood instead

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So far...

PixelCNNs define tractable density function, optimize likelihood of training data: $p_{\theta}(x) = \prod_{i=1}^{n} p_{\theta}(x_i | x_1, ..., x_{i-1})$

VAEs define intractable density function with latent z:

$$p_{ heta}(x) = \int p_{ heta}(z) p_{ heta}(x|z) dz$$

Cannot optimize directly, derive and optimize lower bound on likelihood instead

What if we give up on explicitly modeling density, and just want ability to sample?

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So far...

PixelCNNs define tractable density function, optimize likelihood of training data: $p_{\theta}(x) = \prod_{i=1}^{n} p_{\theta}(x_i | x_1, ..., x_{i-1})$

VAEs define intractable density function with latent z:

$$p_{\theta}(x) = \int p_{\theta}(z) p_{\theta}(x|z) dz$$

Cannot optimize directly, derive and optimize lower bound on likelihood instead

What if we give up on explicitly modeling density, and just want ability to sample?

GANs: don't work with any explicit density function! Instead, take game-theoretic approach: learn to generate from training distribution through 2-player game

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Generative Adversarial Networks

Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

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Problem: Want to sample from complex, high-dimensional training distribution. No direct way to do this!

Solution: Sample from a simple distribution, e.g. random noise. Learn transformation to training distribution.

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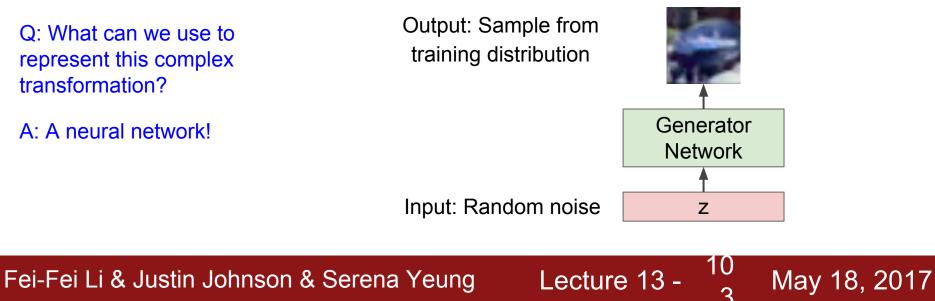
Q: What can we use to represent this complex transformation?

Generative Adversarial Networks

Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

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Solution: Sample from a simple distribution, e.g. random noise. Learn transformation to training distribution.



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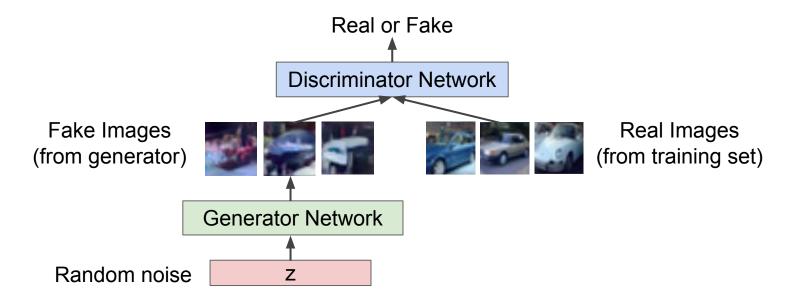
Generator network: try to fool the discriminator by generating real-looking images **Discriminator network**: try to distinguish between real and fake images

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Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

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Generator network: try to fool the discriminator by generating real-looking images **Discriminator network**: try to distinguish between real and fake images



Fake and real images copyright Emily Denton et al. 2015. Reproduced with permission.

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Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

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Generator network: try to fool the discriminator by generating real-looking images **Discriminator network**: try to distinguish between real and fake images

Train jointly in minimax game

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

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Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

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Generator network: try to fool the discriminator by generating real-looking images **Discriminator network**: try to distinguish between real and fake images

Train jointly in **minimax game**

Minimax objective function:

Discriminator outputs likelihood in (0,1) of real image

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$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Discriminator output for for real data x Discriminator output for generated fake data G(z)

Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

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Discriminator output for real data x Discriminator output for generated fake data G(z)

Discriminator outputs likelihood in (0,1) of real image

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- Discriminator (θ_d) wants to **maximize objective** such that D(x) is close to 1 (real) and D(G(z)) is close to 0 (fake)
- Generator (θ_g) wants to **minimize objective** such that D(G(z)) is close to 1 (discriminator is fooled into thinking generated G(z) is real)

Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

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Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Alternate between:

1. Gradient ascent on discriminator

$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

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2. Gradient descent on generator

$$\min_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z)))$$

Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Gradient signal

where sample is already good

dominated by region

-D(G(z)))

0.8

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1.0

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Alternate between:

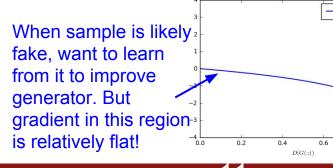
1. Gradient ascent on discriminator

$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

2. Gradient descent on generator

$$\min_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z)))$$

In practice, optimizing this generator objective does not work well!



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Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

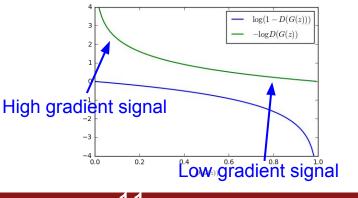
Alternate between:

1. Gradient ascent on discriminator

$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

2. Instead: Gradient ascent on generator, different objective $\max_{\theta_g} \mathbb{E}_{z \sim p(z)} \log(D_{\theta_d}(G_{\theta_g}(z)))$

Instead of minimizing likelihood of discriminator being correct, now maximize likelihood of discriminator being wrong. Same objective of fooling discriminator, but now higher gradient signal for bad samples => works much better! Standard in practice.



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Minimax objective function:

$$\min_{\theta_g} \max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

Alternate between:

1. Gradient ascent on discriminator

$$\max_{\theta_d} \left[\mathbb{E}_{x \sim p_{data}} \log D_{\theta_d}(x) + \mathbb{E}_{z \sim p(z)} \log(1 - D_{\theta_d}(G_{\theta_g}(z))) \right]$$

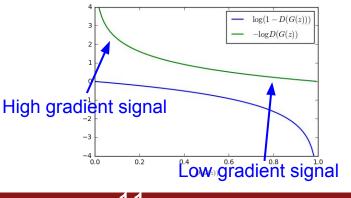
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Instead of minimizing likelihood of discriminator being correct, now maximize likelihood of discriminator being wrong. Same objective of fooling discriminator, but now higher gradient signal for bad samples => works much better! Standard in practice.

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Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Aside: Jointly training two networks is challenging, can be unstable. Choosing objectives with better loss landscapes helps training, is an active area of research.



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Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

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Putting it together: GAN training algorithm

for number of training iterations do for k steps do

- Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_g(z)$.
- Sample minibatch of m examples $\{x^{(1)}, \ldots, x^{(m)}\}$ from data generating distribution $p_{\text{data}}(x)$.

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• Update the discriminator by ascending its stochastic gradient:

$$\nabla_{\theta_d} \frac{1}{m} \sum_{i=1}^m \left[\log D_{\theta_d}(x^{(i)}) + \log(1 - D_{\theta_d}(G_{\theta_g}(z^{(i)}))) \right]$$

end for

- Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_g(z)$.
- Update the generator by ascending its stochastic gradient (improved objective):

$$\nabla_{\theta_g} \frac{1}{m} \sum_{i=1}^m \log(D_{\theta_d}(G_{\theta_g}(z^{(i)})))$$

end for

Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

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Putting it together: GAN training algorithm

for number of training iterations do

for k steps do

- Sample minibatch of m noise samples $\{z^{(1)}, \ldots, z^{(m)}\}$ from noise prior $p_g(z)$.
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end for

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end for

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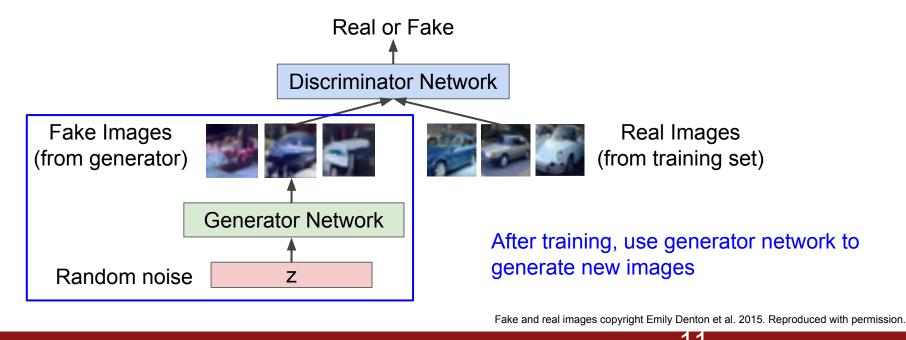
Some find k=1 more stable, others use k > 1, no best rule.

Recent work (e.g. Wasserstein GAN) alleviates this problem, better stability!

Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

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Generator network: try to fool the discriminator by generating real-looking images **Discriminator network**: try to distinguish between real and fake images

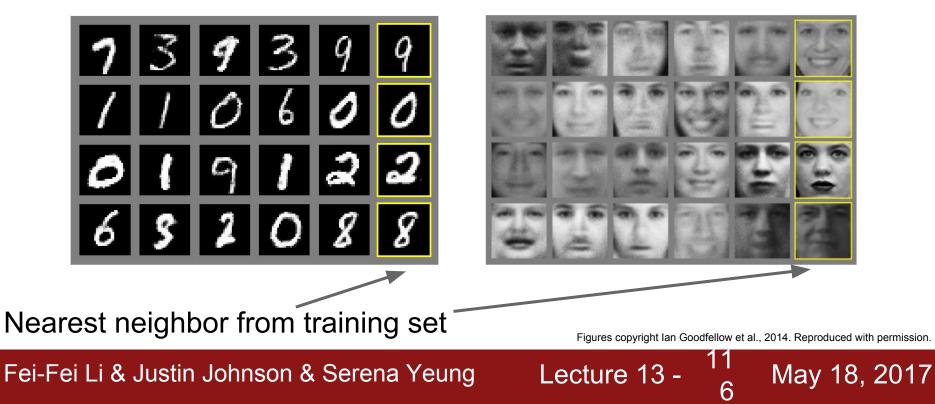


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Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Generative Adversarial Nets

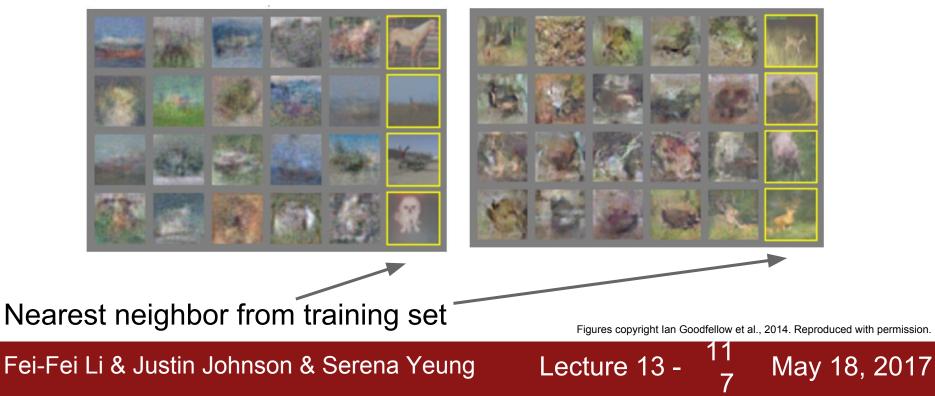
Generated samples



Ian Goodfellow et al., "Generative Adversarial Nets", NIPS 2014

Generative Adversarial Nets

Generated samples (CIFAR-10)



Generator is an upsampling network with fractionally-strided convolutions Discriminator is a convolutional network

Architecture guidelines for stable Deep Convolutional GANs

- Replace any pooling layers with strided convolutions (discriminator) and fractional-strided convolutions (generator).
- Use batchnorm in both the generator and the discriminator.
- Remove fully connected hidden layers for deeper architectures.
- Use ReLU activation in generator for all layers except for the output, which uses Tanh.

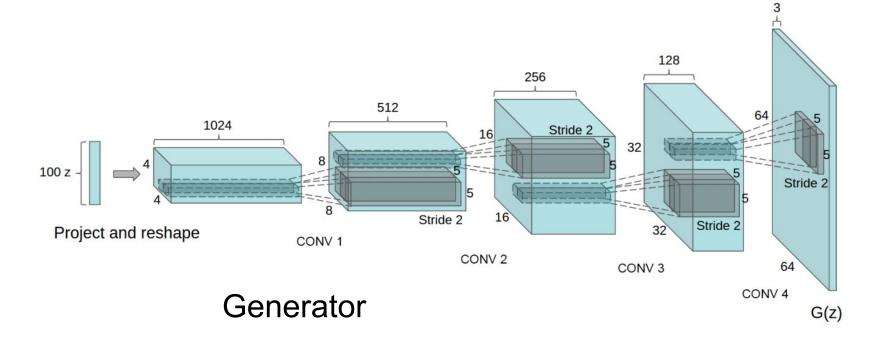
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• Use LeakyReLU activation in the discriminator for all layers.

Radford et al, "Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks", ICLR 2016



Radford et al, "Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks", ICLR 2016

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Samples from the model look amazing!



Radford et al, ICLR 2016

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Interpolating between random points in laten space

Radford et al, ICLR 2016



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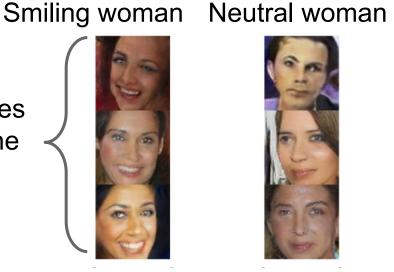
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Radford et al, ICLR 2016

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Samples from the model



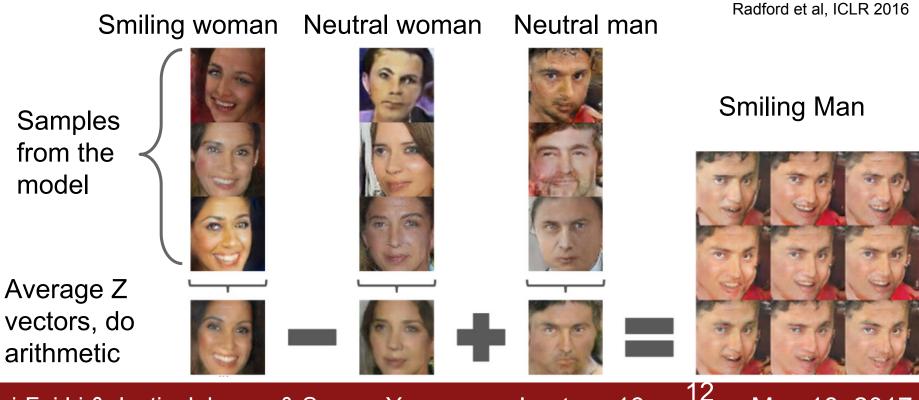




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Neutral man

Radford et al, ICLR 2016 Neutral woman Smiling woman Neutral man Samples from the model Average Z vectors, do arithmetic 12 Lecture 13 -May 18, 2017 Fei-Fei Li & Justin Johnson & Serena Yeung

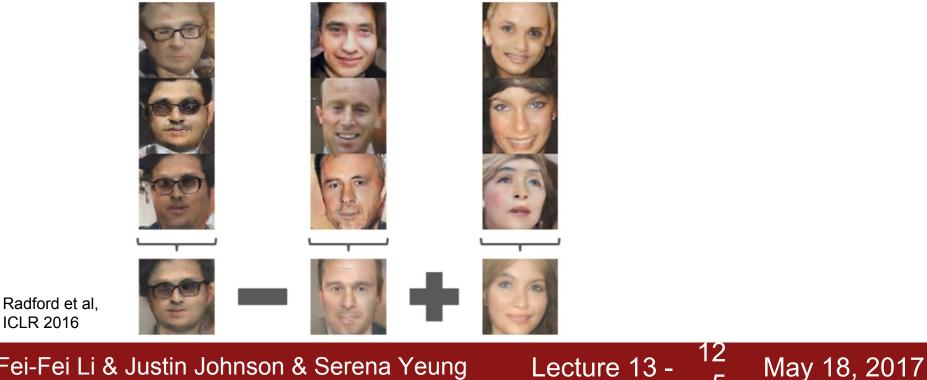


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Glasses man No glasses man No glasses woman



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ICLR 2016

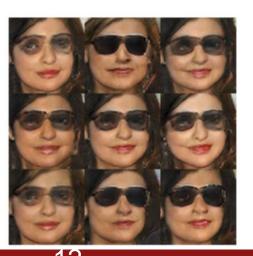
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Glasses man No glasses man

Radford et al, ICLR 2016

Woman with glasses



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No glasses woman

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2017: Year of the GAN

Better training and generation





a) Church outdoor.



(b) Dining room.

(c) Kitchen (d) Conference room LSGAN, Mao et al. 2017.



BEGAN. Bertholet et al. 2017.

Source->Target domain transfer

Output



horse \rightarrow zebra



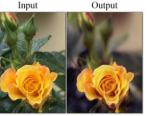
 $zebra \rightarrow horse$



apple \rightarrow orange











→ summer Yosemite.





→ winter Yosemite

Text -> Image Synthesis

this small bird has a pink breast and crown, and black almost all black with a red primaries and secondaries.

this magnificent fellow is crest, and white cheek patch.





Reed et al. 2017.

Many GAN applications







Pix2pix. Isola 2017. Many examples at https://phillipi.github.io/pix2pix/

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"The GAN Zoo"

- GAN Generative Adversarial Networks
- 3D-GAN Learning a Probabilistic Latent Space of Object Shapes via 3D Generative-Adversarial Modeling
- acGAN Face Aging With Conditional Generative Adversarial Networks
- AC-GAN Conditional Image Synthesis With Auxiliary Classifier GANs
- AdaGAN AdaGAN: Boosting Generative Models
- AEGAN Learning Inverse Mapping by Autoencoder based Generative Adversarial Nets
- AffGAN Amortised MAP Inference for Image Super-resolution
- AL-CGAN Learning to Generate Images of Outdoor Scenes from Attributes and Semantic Layouts
- ALI Adversarially Learned Inference
- · AM-GAN Generative Adversarial Nets with Labeled Data by Activation Maximization
- AnoGAN Unsupervised Anomaly Detection with Generative Adversarial Networks to Guide Marker Discovery
- ArtGAN ArtGAN: Artwork Synthesis with Conditional Categorial GANs
- b-GAN b-GAN: Unified Framework of Generative Adversarial Networks
- Bayesian GAN Deep and Hierarchical Implicit Models
- BEGAN BEGAN: Boundary Equilibrium Generative Adversarial Networks
- BiGAN Adversarial Feature Learning
- BS-GAN Boundary-Seeking Generative Adversarial Networks
- CGAN Conditional Generative Adversarial Nets
- CaloGAN CaloGAN: Simulating 3D High Energy Particle Showers in Multi-Layer Electromagnetic Calorimeters
 with Generative Adversarial Networks
- CCGAN Semi-Supervised Learning with Context-Conditional Generative Adversarial Networks
- CatGAN Unsupervised and Semi-supervised Learning with Categorical Generative Adversarial Networks
- CoGAN Coupled Generative Adversarial Networks

- Context-RNN-GAN Contextual RNN-GANs for Abstract Reasoning Diagram Generation
- C-RNN-GAN C-RNN-GAN: Continuous recurrent neural networks with adversarial training
- CS-GAN Improving Neural Machine Translation with Conditional Sequence Generative Adversarial Nets
- CVAE-GAN CVAE-GAN: Fine-Grained Image Generation through Asymmetric Training
- CycleGAN Unpaired Image-to-Image Translation using Cycle-Consistent Adversarial Networks
- DTN Unsupervised Cross-Domain Image Generation
- DCGAN Unsupervised Representation Learning with Deep Convolutional Generative Adversarial Networks
- DiscoGAN Learning to Discover Cross-Domain Relations with Generative Adversarial Networks
- DR-GAN Disentangled Representation Learning GAN for Pose-Invariant Face Recognition
- DualGAN DualGAN: Unsupervised Dual Learning for Image-to-Image Translation
- EBGAN Energy-based Generative Adversarial Network
- f-GAN f-GAN: Training Generative Neural Samplers using Variational Divergence Minimization
- FF-GAN Towards Large-Pose Face Frontalization in the Wild
- GAWWN Learning What and Where to Draw
- GeneGAN GeneGAN: Learning Object Transfiguration and Attribute Subspace from Unpaired Data
- Geometric GAN Geometric GAN
- GoGAN Gang of GANs: Generative Adversarial Networks with Maximum Margin Ranking
- GP-GAN GP-GAN: Towards Realistic High-Resolution Image Blending
- IAN Neural Photo Editing with Introspective Adversarial Networks
- iGAN Generative Visual Manipulation on the Natural Image Manifold
- IcGAN Invertible Conditional GANs for image editing
- ID-CGAN Image De-raining Using a Conditional Generative Adversarial Network
- Improved GAN Improved Techniques for Training GANs

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- InfoGAN InfoGAN: Interpretable Representation Learning by Information Maximizing Generative Adversarial Nets
- LAGAN Learning Particle Physics by Example: Location-Aware Generative Adversarial Networks for Physics
 Synthesis
- LAPGAN Deep Generative Image Models using a Laplacian Pyramid of Adversarial Networks

https://github.com/hindupuravinash/the-gan-zoo

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"The GAN Zoo"

See also: <u>https://github.com/soumith/ganhacks</u> for tips and tricks for trainings GANs

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https://github.com/hindupuravinash/the-gan-zoo

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GANs

Don't work with an explicit density function Take game-theoretic approach: learn to generate from training distribution through 2-player game

Pros:

- Beautiful, state-of-the-art samples!

Cons:

- Trickier / more unstable to train
- Can't solve inference queries such as p(x), p(z|x)

Active areas of research:

- Better loss functions, more stable training (Wasserstein GAN, LSGAN, many others)

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Lecture 13 -

- Conditional GANs, GANs for all kinds of applications

Recap

Generative Models

- PixelRNN and PixelCNN Explicit density model, optimizes exact likelihood, good samples. But inefficient sequential generation.
- Variational Autoencoders (VAE) Optimize variational lower bound on likelihood. Useful latent representation, inference queries. But current sample quality not the best.
- Generative Adversarial Networks (GANs) Game-theoretic approach, best samples! But can be tricky and unstable to train, no inference queries.

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But can be tricky and unstable to train, no inference queries.

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Also recent work in combinations of these types of models! E.g. Adversarial Autoencoders (Makhanzi 2015) and PixelVAE (Gulrajani 2016)

Recap

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Next time: Reinforcement Learning