# Lecture 4: Backpropagation and Neural Networks

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 1

# Administrative

## Assignment 1 due Thursday April 20, 11:59pm on Canvas

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 2

# Administrative

# **Project:** TA specialities and some project ideas are posted on Piazza

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 3 - 3

April 11, 2017

# Administrative

# **Google Cloud:** All registered students will receive an email this week with instructions on how to redeem \$100 in credits

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 4

## Where we are...

$$egin{aligned} s &= f(x;W) = Wx & ext{scores function} \ L_i &= \sum_{j 
eq y_i} \max(0,s_j-s_{y_i}+1) & ext{SVM loss} \ L &= rac{1}{N} \sum_{i=1}^N L_i + \sum_k W_k^2 & ext{data loss + regularization} \end{aligned}$$



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 5

# Optimization





#### # Vanilla Gradient Descent

while True:

Landscape image is CC0 1.0 public domain Walking man image is CC0 1.0 public domain weights\_grad = evaluate\_gradient(loss\_fun, data, weights)
weights += - step size \* weights grad # perform parameter update

Fei-Fei Li & Justin Johnson & Serena Yeung

#### Lecture 4 - 6

# Gradient descent

$$rac{df(x)}{dx} = \lim_{h o 0} rac{f(x+h) - f(x)}{h}$$

**Numerical gradient**: slow :(, approximate :(, easy to write :) **Analytic gradient**: fast :), exact :), error-prone :(

In practice: Derive analytic gradient, check your implementation with numerical gradient

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 7

# **Computational graphs**



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 8



Figure copyright Alex Krizhevsky, Ilya Sutskever, and Geoffrey Hinton, 2012. Reproduced with permission.

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 9



Figure reproduced with permission from a Twitter post by Andrej Karpathy.

Lecture 4 - 10



#### Lecture 4 -

$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 12

$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4

$$q=x+y$$
  $rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$ 

$$f=qz$$
  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

Want: 
$$\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$$

Fei-Fei Li & Justin Johnson & Serena Yeung

$$x \frac{-2}{y 5} + q 3$$

$$x \frac{f -12}{t}$$

$$z \frac{-4}{t}$$

April 13, 2017

Lecture 4 - 13

$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4

$$q=x+y$$
  $rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$ 

$$f=qz$$
  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

$$-4$$

$$\frac{\partial f}{\partial f}$$

**q** 3

+

Want:  $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$ 

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 14

x -2

y 5

Ζ

$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4

$$q=x+y \hspace{0.5cm} rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$$

$$f=qz$$
  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

$$rac{\partial f}{\partial f}$$

\*

f -12

Want:  $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$ 

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 15

**q** 3

x -2

y 5

Ζ

$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4

$$q=x+y$$
  $rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$ 

$$f=qz$$
  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

Want: 
$$\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$$

Fei-Fei Li & Justin Johnson & Serena Yeung

x -2 **q** 3 y 5 f -12 \* Ζ ∂f  $\partial z$ 

Lecture 4 - 16

$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4

$$q=x+y \hspace{0.5cm} rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$$

$$f=qz$$
  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

Want: 
$$\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$$

Fei-Fei Li & Justin Johnson & Serena Yeung

$$x \frac{-2}{y 5}$$

$$y \frac{5}{z \frac{-4}{3}}$$

$$\frac{\partial f}{\partial z}$$

Lecture 4 - 17

$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4

$$q=x+y$$
  $rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$ 

$$f=qz$$
  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

Want: 
$$\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$$

Fei-Fei Li & Justin Johnson & Serena Yeung

x -2 **q** 3 y 5 f -12 \* Ζ -4 3

Lecture 4 - 18

$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4

$$q=x+y$$
  $rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$ 

$$f=qz$$
  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

Want: 
$$\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$$

Fei-Fei Li & Justin Johnson & Serena Yeung

x -2 3 y 5 f -12 \* Ζ -4 3

Lecture 4 - 19

$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4

$$q=x+y$$
  $rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$ 

$$f=qz$$
  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

Nant: 
$$\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y},$$

Fei-Fei Li & Justin Johnson & Serena Yeung

 $\frac{\partial f}{\partial z}$ 

x 
$$\frac{-2}{y}$$
  
y  $\frac{5}{z}$   
z  $\frac{-4}{3}$   
 $\frac{\partial f}{\partial y}$ 

Lecture 4 - 20

$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4

$$q=x+y$$
  $rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$ 

$$egin{aligned} f = qz & rac{\partial f}{\partial q} = z, rac{\partial f}{\partial z} = q \ \end{aligned}$$
 Want:  $rac{\partial f}{\partial x}, rac{\partial f}{\partial y}, rac{\partial f}{\partial z} \end{aligned}$ 

x 
$$\frac{-2}{y}$$
  
y  $\frac{5}{-4}$   
z  $\frac{-4}{3}$   
Chain rule:  
 $\frac{\partial f}{\partial y}$   
 $\frac{\partial f}{\partial y}$ 

April 13, 2017

$$\frac{\partial f}{\partial y} = \frac{\partial f}{\partial q} \frac{\partial q}{\partial y}$$

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 21

у

Ζ

$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4

$$q=x+y$$
  $rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$ 

$$f=qz$$
  $rac{\partial f}{\partial q}=z, rac{\partial f}{\partial z}=q$ 

Want: 
$$\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial y}$$

Fei-Fei Li & Justin Johnson & Serena Yeung

Z

$$x \frac{-2}{y \frac{5}{-4}} + \frac{q 3}{-4} + \frac{q 3}{\sqrt{1-12}} + \frac{f -12}{\sqrt{1-12}} + \frac{f -12}{\sqrt{$$

Lecture 4 - 22

$$f(x, y, z) = (x + y)z$$
  
e.g. x = -2, y = 5, z = -4

$$q=x+y$$
  $rac{\partial q}{\partial x}=1, rac{\partial q}{\partial y}=1$ 

$$f = qz$$
  $rac{\partial f}{\partial q} = z, rac{\partial f}{\partial z} = q$   
Want:  $rac{\partial f}{\partial x}, rac{\partial f}{\partial y}, rac{\partial f}{\partial z}$ 

$$x \frac{-2}{-4}$$

$$y \frac{5}{-4}$$

$$z \frac{-4}{3}$$

$$\frac{\partial f}{\partial x} = \frac{\partial f}{\partial q} \frac{\partial q}{\partial x}$$

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 23



Lecture 4 - 24



Lecture 4 - 25



Lecture 4 - 26



Lecture 4 - 27



Lecture 4 - 28



$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 30

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 31

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 32

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 33

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 34

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 35

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 36
$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 37

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 38

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 39

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 40

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 41



Lecture 4 - 42

$$f(w,x)=rac{1}{1+e^{-(w_0x_0+w_1x_1+w_2)}}$$



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 43

$$\begin{aligned} f(w,x) &= \frac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}} & \sigma(x) &= \frac{1}{1 + e^{-x}} & \text{sigmoid function} \\ \frac{d\sigma(x)}{dx} &= \frac{e^{-x}}{(1 + e^{-x})^2} = \left(\frac{1 + e^{-x} - 1}{1 + e^{-x}}\right) \left(\frac{1}{1 + e^{-x}}\right) = (1 - \sigma(x))\sigma(x) \end{aligned}$$



Lecture 4 - 44

$$\begin{aligned} f(w,x) &= \frac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}} & \sigma(x) &= \frac{1}{1 + e^{-x}} & \text{sigmoid function} \\ \frac{d\sigma(x)}{dx} &= \frac{e^{-x}}{(1 + e^{-x})^2} = \left(\frac{1 + e^{-x} - 1}{1 + e^{-x}}\right) \left(\frac{1}{1 + e^{-x}}\right) = (1 - \sigma(x))\sigma(x) \end{aligned}$$



Lecture 4 - 45

add gate: gradient distributor



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 46

add gate: gradient distributor

Q: What is a **max** gate?



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 47

add gate: gradient distributormax gate: gradient router



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 48

add gate: gradient distributormax gate: gradient routerQ: What is a mul gate?



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 49

add gate: gradient distributormax gate: gradient routermul gate: gradient switcher



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 50

# Gradients add at branches

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 51



Lecture 4 - 52

#### Vectorized operations



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 53



Lecture 4 - 54



Lecture 4 - 55

# Vectorized operations



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 -



Lecture 4 -

# A vectorized example: $f(x, W) = ||W \cdot x||^2 = \sum_{i=1}^{n} (W \cdot x)_i^2$

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 58

# A vectorized example: $f(x, W) = ||W \cdot x||^2 = \sum_{i=1}^n (W \cdot x)_i^2$ $\bigcup_{i \in \mathbb{R}^n \in \mathbb{R}^{n \times n}} ||W \cdot x||^2 = \sum_{i=1}^n (W \cdot x)_i^2$

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 59

A vectorized example:  $f(x, W) = ||W \cdot x||^2 = \sum_{i=1}^{n} (W \cdot x)_i^2$ 



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 60



Lecture 4 - 61



Lecture 4 - 62



Lecture 4 - 63

A vectorized example: 
$$f(x, W) = ||W \cdot x||^2 = \sum_{i=1}^{n} (W \cdot x)_i^2$$
  
 $\begin{bmatrix} 0.1 & 0.5 \\ -0.3 & 0.8 \end{bmatrix}_W$   
 $\begin{bmatrix} 0.2 \\ 0.4 \end{bmatrix}_X$   
 $q = W \cdot x = \begin{pmatrix} W_{1,1}x_1 + \dots + W_{1,n}x_n \\ \vdots \\ W_{n,1}x_1 + \dots + W_{n,n}x_n \end{pmatrix}$   
 $f(q) = ||q||^2 = q_1^2 + \dots + q_n^2$   
 $\frac{\partial f}{\partial q_i} = 2q_i$   
 $\nabla_q f = 2q$ 

Lecture 4 - 64

A vectorized example: 
$$f(x, W) = ||W \cdot x||^2 = \sum_{i=1}^{n} (W \cdot x)_i^2$$
  

$$\begin{bmatrix} 0.1 & 0.5 \\ -0.3 & 0.8 \end{bmatrix}_W$$

$$\begin{bmatrix} 0.2 \\ 0.4 \end{bmatrix}_x$$

$$\begin{bmatrix} 0.22 \\ 0.26 \end{bmatrix}_x$$

$$\begin{bmatrix} 0.22 \\ 0.26 \end{bmatrix}_x$$

$$\begin{bmatrix} 0.2 \\ 0.116 \\ 1.00 \end{bmatrix}$$

$$\begin{bmatrix} 0.2 \\ 0.44 \\ 0.52 \end{bmatrix}$$

$$\begin{bmatrix} 0.116 \\ 1.00 \end{bmatrix}$$

$$\frac{\partial f}{\partial q_i} = 2q_i$$

$$\begin{bmatrix} 0 \\ 0.44 \\ 0.52 \end{bmatrix}$$

$$\int Q_q f = 2q$$

Lecture 4 - 65



Lecture 4 - 66



Lecture 4 - 67



Lecture 4 - 68



Lecture 4 - 69



Lecture 4 - 70



Lecture 4 - 71



Lecture 4 - 72


Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 73



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 74

## Modularized implementation: forward / backward API



Graph (or Net) object (rough psuedo code)

class ComputationalGraph(object):
#
<pre>def forward(inputs):</pre>
<pre># 1. [pass inputs to input gates]</pre>
<pre># 2. forward the computational graph:</pre>
<pre>for gate in self.graph.nodes_topologically_sorted():</pre>
gate.forward()
<pre>return loss # the final gate in the graph outputs the loss</pre>
<pre>def backward():</pre>
<pre>for gate in reversed(self.graph.nodes_topologically_sorted()):</pre>
<pre>gate.backward() # little piece of backprop (chain rule applied)</pre>
<pre>return inputs_gradients</pre>

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 75

## Modularized implementation: forward / backward API



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 76

## Modularized implementation: forward / backward API



(x,y,z are scalars)

class Mu	<pre>ultiplyGate(object):</pre>
def	<pre>forward(x,y):</pre>
	$z = x^*y$
	<pre>self.x = x # must keep these around!</pre>
	self.y = y
	return z
def	backward(dz):
	dx = self.y * dz # [dz/dx * dL/dz]
	dy = self.x * dz # [dz/dy * dL/dz]
	return [dx, dy]

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 77

## **Example: Caffe layers**

Branch: master - caffe / src / c	caffe / layers / Create new	file Upload files	Find file	History	
shelhamer committed on GitHul	b Merge pull request #4630 from BIGene/Ioad_hdf5_fix …	Latest commit	e687a71 21	days ago	
<u>/11</u>					
absval_layer.cpp	dismantle layer headers		a year ago		
absval_layer.cu	dismantle layer headers		a year ago		
accuracy_layer.cpp	dismantle layer headers		a year ago		
argmax_layer.cpp	dismantle layer headers		ay	/ear ago	
base_conv_layer.cpp	enable dilated deconvolution		ay	/ear ago	
base_data_layer.cpp	Using default from proto for prefetch		3 mor	nths ago	
base_data_layer.cu	Switched multi-GPU to NCCL		3 mor	nths ago	
batch_norm_layer.cpp	Add missing spaces besides equal signs in batch_norm_layer.cpp		4 mor	nths ago	
batch_norm_layer.cu	dismantle layer headers		ay	/ear ago	
batch_reindex_layer.cpp	dismantle layer headers		ay	/ear ago	
batch_reindex_layer.cu	dismantle layer headers		ay	/ear ago	
bias_layer.cpp	Remove incorrect cast of gemm int arg to Dtype in BiasLayer		ay	/ear ago	
bias_layer.cu	Separation and generalization of ChannelwiseAffineLayer into BiasLa	iyer	ay	/ear ago	
bnll_layer.cpp	dismantle layer headers		ay	/ear ago	
bnll_layer.cu	dismantle layer headers		ay	/ear ago	
concat_layer.cpp	dismantle layer headers		ay	/ear ago	
Concat_layer.cu	dismantle layer headers		ay	/ear ago	
Contrastive_loss_layer.cpp	dismantle layer headers		ay	/ear ago	
Contrastive_loss_layer.cu	dismantle layer headers		ay	/ear ago	
conv_layer.cpp	add support for 2D dilated convolution		ay	/ear ago	
Conv_layer.cu	dismantle layer headers		ay	/ear ago	
crop_layer.cpp	remove redundant operations in Crop layer (#5138)		2 mor	nths ago	
E crop_layer.cu	remove redundant operations in Crop layer (#5138)		2 mor	nths ago	
cudnn_conv_layer.cpp	dismantle layer headers		ay	/ear ago	
cudnn_conv_layer.cu	Add cuDNN v5 support, drop cuDNN v3 support		11 mor	nths ago	

cudnn_lcn_layer.cpp	dismantle layer headers	a year ago
Cudnn_lcn_layer.cu	dismantle layer headers	a year ago
Cudnn_Irn_layer.cpp	dismantle layer headers	a year ago
E cudnn_Irn_layer.cu	dismantle layer headers	a year ago
cudnn_pooling_layer.cpp	dismantle layer headers	a year ago
Cudnn_pooling_layer.cu	dismantle layer headers	a year ago
Cudnn_relu_layer.cpp	Add cuDNN v5 support, drop cuDNN v3 support	11 months ago
E cudnn_relu_layer.cu	Add cuDNN v5 support, drop cuDNN v3 support	11 months ago
Cudnn_sigmoid_layer.cpp	Add cuDNN v5 support, drop cuDNN v3 support	11 months ago
Cudnn_sigmoid_layer.cu	Add cuDNN v5 support, drop cuDNN v3 support	11 months ago
Cudnn_softmax_layer.cpp	dismantle layer headers	a year ago
cudnn_softmax_layer.cu	dismantle layer headers	a year ago
Cudnn_tanh_layer.cpp	Add cuDNN v5 support, drop cuDNN v3 support	11 months ago
Cudnn_tanh_layer.cu	Add cuDNN v5 support, drop cuDNN v3 support	11 months ago
data_layer.cpp	Switched multi-GPU to NCCL	3 months ago
deconv_layer.cpp	enable dilated deconvolution	a year ago
deconv_layer.cu	dismantle layer headers	a year ago
dropout_layer.cpp	supporting N-D Blobs in Dropout layer Reshape	a year ago
dropout_layer.cu	dismantle layer headers	a year ago
dummy_data_layer.cpp	dismantle layer headers	a year ago
eltwise_layer.cpp	dismantle layer headers	a year ago
eltwise_layer.cu	dismantle layer headers	a year ago
elu_layer.cpp	ELU layer with basic tests	a year ago
elu_layer.cu	ELU layer with basic tests	a year ago
embed_layer.cpp	dismantle layer headers	a year ago
embed_layer.cu	dismantle layer headers	a year ago
euclidean_loss_layer.cpp	dismantle layer headers	a year ago
euclidean_loss_layer.cu	dismantle layer headers	a year ago
exp_layer.cpp	Solving issue with exp layer with base e	a year ago
exp laver.cu	dismantle laver headers	a vear ago

Caffe is licensed under BSD 2-Clause

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 78



Caffe is licensed under BSD 2-Clause

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 79

# In Assignment 1: Writing SVM / Softmax

### Stage your forward/backward computation!



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 80

# Summary so far...

- neural nets will be very large: impractical to write down gradient formula by hand for all parameters
- **backpropagation** = recursive application of the chain rule along a computational graph to compute the gradients of all inputs/parameters/intermediates
- implementations maintain a graph structure, where the nodes implement the forward() / backward() API
- **forward**: compute result of an operation and save any intermediates needed for gradient computation in memory
- **backward**: apply the chain rule to compute the gradient of the loss function with respect to the inputs

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 81

# **Next: Neural Networks**

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 82

(**Before**) Linear score function: f = Wx

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 83

(**Before**) Linear score function: (**Now**) 2-layer Neural Network

$$egin{aligned} f &= Wx \ f &= W_2 \max(0, W_1 x) \end{aligned}$$

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 84

(Before) Linear score function: f = Wx(Now) 2-layer Neural Network  $f = W_2 \max(0, W_1x)$ 



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 85



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 86

(Before) Linear score function:

(**Now**) 2-layer Neural Network or 3-layer Neural Network

$$f = Wx$$

$$f=W_2\max(0,W_1x)$$

$$f=W_3\max(0,W_2\max(0,W_1x))$$

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 87

### Full implementation of training a 2-layer Neural Network needs ~20 lines:

```
import numpy as np
 1
    from numpy.random import randn
 3
    N, D_in, H, D out = 64, 1000, 100, 10
 4
    x, y = randn(N, D_in), randn(N, D_out)
 5
    w1, w2 = randn(D_in, H), randn(H, D_out)
 6
 7
    for t in range(2000):
 8
      h = 1 / (1 + np.exp(-x.dot(w1)))
 9
      y_pred = h.dot(w2)
10
      loss = np.square(y_pred - y).sum()
11
12
      print(t, loss)
13
14
      grad_y_pred = 2.0 * (y_pred - y)
15
      grad_w2 = h.T.dot(grad_y_pred)
16
      grad h = grad y pred.dot(w2.T)
17
      grad w1 = x.T.dot(grad h * h * (1 - h))
18
      w1 = 1e - 4 * grad w1
19
20
      w2 = 1e - 4 * grad w2
```

### Fei-Fei Li & Justin Johnson & Serena Yeung

```
Lecture 4 - 88
```

# In Assignment 2: Writing a 2-layer net

<pre># receive W1,W2,b1,b2 (weights/biases), X (data)</pre>
# forward pass:
<pre>h1 = # function of X,W1,b1</pre>
<pre>scores = # function of h1,W2,b2</pre>
<pre>loss = # (several lines of code to evaluate Softmax loss)</pre>
<pre># backward pass:</pre>
dscores = #
dh1,dW2,db2 = #
dW1,db1 = #

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 89



This image by Fotis Bobolas is licensed under CC-BY 2.0

Fei-Fei Li & Justin Johnson & Serena Yeung

### Lecture 4 - 90



is licensed under CC-BY 3.0

### Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 91



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 92



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 93



### Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 94

## Be very careful with your brain analogies!

### **Biological Neurons:**

- Many different types
- Dendrites can perform complex non-linear computations
- Synapses are not a single weight but a complex non-linear dynamical system
- Rate code may not be adequate

[Dendritic Computation. London and Hausser]

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 95

# Activation functions







 $\begin{array}{l} \textbf{Maxout} \\ \max(w_1^T x + b_1, w_2^T x + b_2) \end{array}$ 



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 96

# Neural networks: Architectures



Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 97

## Example feed-forward computation of a neural network

```
class Neuron:
    # ...
    def neuron_tick(inputs):
        """ assume inputs and weights are 1-D numpy arrays and bias is a number """
        cell_body_sum = np.sum(inputs * self.weights) + self.bias
        firing_rate = 1.0 / (1.0 + math.exp(-cell_body_sum)) # sigmoid activation function
        return firing_rate
```

We can efficiently evaluate an entire layer of neurons.

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 98

### Example feed-forward computation of a neural network



# forward-pass of a 3-layer neural network: f = lambda x: 1.0/(1.0 + np.exp(-x)) # activation function (use sigmoid) x = np.random.randn(3, 1) # random input vector of three numbers (3x1) h1 = f(np.dot(W1, x) + b1) # calculate first hidden layer activations (4x1) h2 = f(np.dot(W2, h1) + b2) # calculate second hidden layer activations (4x1) out = np.dot(W3, h2) + b3 # output neuron (1x1)

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 4 - 99

# Summary

- We arrange neurons into fully-connected layers
- The abstraction of a **layer** has the nice property that it allows us to use efficient vectorized code (e.g. matrix multiplies)

Lecture 4 -

April 13, 2017

- Neural networks are not really neural
- Next time: Convolutional Neural Networks

Fei-Fei Li & Justin Johnson & Serena Yeung