# Lecture 7: Training Neural Networks, Part 2

Fei-Fei Li & Justin Johnson & Serena Yeung

Lecture 7 - 1 April 25, 2017

#### Administrative

- Assignment 1 is being graded, stay tuned
- Project proposals due today by 11:59pm
- Assignment 2 is out, due Thursday May 4 at 11:59pm

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Lecture 7 - 2 April 25, 2017

#### Administrative: Google Cloud

- STOP YOUR INSTANCES when not in use!

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## Administrative: Google Cloud

- STOP YOUR INSTANCES when not in use!
- Keep track of your spending!
- GPU instances are much more expensive than CPU instances only use GPU instance when you need it (e.g. for A2 only on TensorFlow / PyTorch notebooks)

Lecture 7 - 4

<u>April 25, 2017</u>

### Last time: Activation Functions



Leaky ReLU  $\max(0.1x, x)$ 



 $\begin{array}{l} \textbf{Maxout} \\ \max(w_1^T x + b_1, w_2^T x + b_2) \end{array}$ 



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### Last time: Activation Functions



Leaky ReLU  $\max(0.1x, x)$ 



 $\begin{array}{l} \textbf{Maxout} \\ \max(w_1^T x + b_1, w_2^T x + b_2) \end{array}$ 



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## Last time: Weight Initialization



#### Initialization too small:

Activations go to zero, gradients also zero, No learning

Initialization too big: Activations saturate (for tanh), Gradients zero, no learning

#### Initialization just right:

Nice distribution of activations at all layers, Learning proceeds nicely

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## Last time: Data Preprocessing



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## Last time: Data Preprocessing

**Before normalization**: classification loss very sensitive to changes in weight matrix; hard to optimize After normalization: less sensitive to small changes in weights; easier to optimize



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#### Last time: Batch Normalization

Input: 
$$x: N \times D$$

#### Learnable params:

 $\gamma, \beta: D$ 

# Intermediates: $\frac{\mu, \sigma : D}{\hat{r} \cdot N \times D}$

**Output**:  $y: N \times D$ 



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#### Last time: Babysitting Learning



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## Last time: Hyperparameter Search



#### Coarse to fine search

ſ	val_acc:	0.412000,	lr:	1.405206e-04,	reg:	4.793564e-01,	(1 /	100)
	val_acc:	0.214000,	lr:	7.231888e-06,	reg:	2.321281e-04,	(2 /	100)
	val_acc:	0.208000,	lr:	2.119571e-06,	reg:	8.011857e+01,	(3 /	100)
	val acc:	0.196000,	lr:	1.551131e-05,	reg:	4.374936e-05,	(4 /	100)
	val acc:	0.079000,	lr:	1.753300e-05,	reg:	1.200424e+03,	(5 /	100)
	val acc:	0.223000,	lr:	4.215128e-05,	reg:	4.196174e+01,	(6 /	100)
ſ	val_acc:	0.441000,	lr:	1.750259e-04,	reg:	2.110807e-04,	(7 /	100)
	val acc:	0.241000,	lr:	6.749231e-05,	reg:	4.226413e+01,	(8 /	100)
	val_acc:	0.482000,	lr:	4.296863e-04,	reg:	6.642555e-01,	(9 /	100)
	val_acc:	0.079000,	lr:	5.401602e-06,	reg:	1.599828e+04,	(10 /	100)
	val_acc:	0.154000,	lr:	1.618508e-06,	reg:	4.925252e-01,	(11 /	100)

val_acc:	0.527000, lr:	5.340517e-04,	reg:	4.097824e-01,	(0 / 100)
val_acc:	0.492000, tr:	2.279484e-04,	reg:	9.991345e-04,	(1 / 100)
val_acc:	0.512000, lr:	8.680827e-04,	reg:	1.349727e-02,	(2 / 100)
val acc:	0.461000, lr:	1.028377e-04,	reg:	1.220193e-02,	(3 / 100)
val acc:	0.460000, lr:	1.113730e-04,	reg:	5.244309e-02,	(4 / 100)
val acc:	0.498000, lr:	9.477776e-04,	reg:	2.001293e-03,	(5 / 100)
val acc:	0.469000, lr:	1.484369e-04,	reg:	4.328313e-01,	(6 / 100)
val acc:	0.522000, lr:	5.586261e-04,	reg:	2.312685e-04,	(7 / 100)
val acc:	0.530000, lr:	5.808183e-04,	req:	8.259964e-02,	(8 / 100)
val acc:	0.489000, lr:	1.979168e-04,	reg:	1.010889e-04,	(9 / 100)
val acc:	0.490000, lr:	2.036031e-04,	reg:	2.406271e-03,	(10 / 100)
val acc:	0.475000, lr:	2.021162e-04,	reg:	2.287807e-01,	(11 / 100)
val acc:	0.460000, lr:	1.135527e-04,	reg:	3.905040e-02,	(12 / 100)
val acc:	0.515000, lr:	6.947668e-04,	reg:	1.562808e-02,	(13 / 100)
val acc:	0.531000, lr:	9.471549e-04,	reg:	1.433895e-03,	(14 / 100)
val acc:	0.509000, lr:	3.140888e-04,	reg:	2.857518e-01,	(15 / 100)
val acc:	0.514000, lr:	6.438349e-04,	reg:	3.033781e-01,	(16 / 100)
val acc:	0.502000, lr:	3.921784e-04,	reg:	2.707126e-04,	(17 / 100)
val acc:	0.509000, lr:	9.752279e-04,	reg:	2.850865e-03,	(18 / 100)
val acc:	0.500000, lr:	2.412048e-04,	reg:	4.997821e-04,	(19 / 100)
val acc:	0.466000, lr:	1.319314e-04,	reg:	1.189915e-02,	(20 / 100)
val acc:	0.516000, lr:	8.039527e-04,	reg:	1.528291e-02,	(21 / 100)

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- Fancier optimization
- Regularization
- Transfer Learning

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#### Optimization

# Vanilla Gradient Descent

while True: weights\_grad = evaluate\_gradient(loss\_fun, data, weights) weights += - step\_size \* weights\_grad # perform parameter update



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What if loss changes quickly in one direction and slowly in another? What does gradient descent do?



Loss function has high **condition number**: ratio of largest to smallest singular value of the Hessian matrix is large

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What if loss changes quickly in one direction and slowly in another? What does gradient descent do?

Very slow progress along shallow dimension, jitter along steep direction



Loss function has high **condition number**: ratio of largest to smallest singular value of the Hessian matrix is large

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What if the loss function has a **local minima** or **saddle point**?



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What if the loss function has a **local minima** or **saddle point**?

Zero gradient, gradient descent gets stuck

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What if the loss function has a **local minima** or **saddle point**?

Saddle points much more common in high dimension

Dauphin et al, "Identifying and attacking the saddle point problem in high-dimensional non-convex optimization", NIPS 2014

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Our gradients come from minibatches so they can be noisy!

$$L(W) = \frac{1}{N} \sum_{i=1}^{N} L_i(x_i, y_i, W)$$

$$\nabla_W L(W) = \frac{1}{N} \sum_{i=1}^N \nabla_W L_i(x_i, y_i, W)$$



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#### SGD + Momentum

SGD

$$x_{t+1} = x_t - \alpha \nabla f(x_t)$$

#### while True:

- dx = compute\_gradient(x)
- x += learning\_rate \* dx

#### SGD+Momentum

$$v_{t+1} = \rho v_t + \nabla f(x_t)$$

 $x_{t+1} = x_t - \alpha v_{t+1}$ 

vx = 0
while True:
 dx = compute\_gradient(x)
 vx = rho \* vx + dx
 x += learning\_rate \* vx

- Build up "velocity" as a running mean of gradients
- Rho gives "friction"; typically rho=0.9 or 0.99

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## SGD + Momentum

#### **Gradient Noise**



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#### SGD + Momentum

Momentum update:



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Nesterov, "A method of solving a convex programming problem with convergence rate O(1/k<sup>2</sup>)", 1983 Nesterov, "Introductory lectures on convex optimization: a basic course", 2004 Sutskever et al, "On the importance of initialization and momentum in deel learning", ICML 2013

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$$v_{t+1} = \rho v_t - \alpha \nabla f(x_t + \rho v_t)$$
$$x_{t+1} = x_t + v_{t+1}$$

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$$v_{t+1} = \rho v_t - \alpha \nabla f(x_t + \rho v_t)$$
$$x_{t+1} = x_t + v_{t+1}$$

Annoying, usually we want update in terms of  $x_t, \nabla f(x_t)$ 

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$$v_{t+1} = \rho v_t - \alpha \nabla f(x_t + \rho v_t)$$
$$x_{t+1} = x_t + v_{t+1}$$

Annoying, usually we want update in terms of  $x_t, \nabla f(x_t)$ 

Change of variables 
$$\tilde{x}_t = x_t + \rho v_t$$
 and rearrange:

$$v_{t+1} = \rho v_t - \alpha \nabla f(\tilde{x}_t) \tilde{x}_{t+1} = \tilde{x}_t - \rho v_t + (1+\rho)v_{t+1} = \tilde{x}_t + v_{t+1} + \rho(v_{t+1} - v_t)$$

dx = compute\_gradient(x)
old\_v = v
v = rho \* v - learning\_rate \* dx
x += -rho \* old\_v + (1 + rho) \* v

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#### AdaGrad

grad\_squared = 0
while True:
 dx = compute\_gradient(x)
 grad\_squared += dx \* dx
 x -= learning\_rate \* dx / (np.sqrt(grad\_squared) + 1e-7)

Added element-wise scaling of the gradient based on the historical sum of squares in each dimension

Duchi et al, "Adaptive subgradient methods for online learning and stochastic optimization", JMLR 2011

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## AdaGrad





#### Q: What happens with AdaGrad?

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## AdaGrad





Q2: What happens to the step size over long time?

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## RMSProp



Tieleman and Hinton, 2012

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#### **RMSProp**



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## Adam (almost)

```
first_moment = 0
second_moment = 0
while True:
    dx = compute_gradient(x)
    first_moment = beta1 * first_moment + (1 - beta1) * dx
    second_moment = beta2 * second_moment + (1 - beta2) * dx * dx
    x -= learning_rate * first_moment / (np.sqrt(second_moment) + 1e-7))
```

Kingma and Ba, "Adam: A method for stochastic optimization", ICLR 2015

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## Adam (almost)



Sort of like RMSProp with momentum

#### Q: What happens at first timestep?

Kingma and Ba, "Adam: A method for stochastic optimization", ICLR 2015

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## Adam (full form)



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Bias correction for the fact that first and second moment estimates start at zero

Kingma and Ba, "Adam: A method for stochastic optimization", ICLR 2015

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## Adam (full form)



Bias correction for the fact that first and second moment estimates start at zero

Adam with beta1 = 0.9, beta2 = 0.999, and learning\_rate = 1e-3 or 5e-4 is a great starting point for many models!

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Kingma and Ba, "Adam: A method for stochastic optimization", ICLR 2015

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## Adam



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## Q: Which one of these learning rates is best to use?

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#### => Learning rate decay over time!

#### step decay:

e.g. decay learning rate by half every few epochs.

exponential decay:

$$lpha=lpha_0 e^{-kt}$$

1/t decay: $lpha=lpha_0/(1+kt)$ 

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## **First-Order Optimization**



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## **First-Order Optimization**



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second-order Taylor expansion:

$$J(\boldsymbol{\theta}) \approx J(\boldsymbol{\theta}_0) + (\boldsymbol{\theta} - \boldsymbol{\theta}_0)^{\top} \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0) + \frac{1}{2} (\boldsymbol{\theta} - \boldsymbol{\theta}_0)^{\top} \boldsymbol{H} (\boldsymbol{\theta} - \boldsymbol{\theta}_0)$$

Solving for the critical point we obtain the Newton parameter update:

$$\boldsymbol{\theta}^* = \boldsymbol{\theta}_0 - \boldsymbol{H}^{-1} \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0)$$

#### Q: What is nice about this update?

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second-order Taylor expansion:

$$J(\boldsymbol{\theta}) \approx J(\boldsymbol{\theta}_0) + (\boldsymbol{\theta} - \boldsymbol{\theta}_0)^\top \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0) + \frac{1}{2} (\boldsymbol{\theta} - \boldsymbol{\theta}_0)^\top \boldsymbol{H} (\boldsymbol{\theta} - \boldsymbol{\theta}_0)$$

Solving for the critical point we obtain the Newton parameter update:

$$\boldsymbol{\theta}^* = \boldsymbol{\theta}_0 - \boldsymbol{H}^{-1} \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0)$$

No hyperparameters! No learning rate!

#### Q: What is nice about this update?

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second-order Taylor expansion:

$$J(\boldsymbol{\theta}) \approx J(\boldsymbol{\theta}_0) + (\boldsymbol{\theta} - \boldsymbol{\theta}_0)^\top \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0) + \frac{1}{2} (\boldsymbol{\theta} - \boldsymbol{\theta}_0)^\top \boldsymbol{H} (\boldsymbol{\theta} - \boldsymbol{\theta}_0)$$

Solving for the critical point we obtain the Newton parameter update:

$$\boldsymbol{\theta}^* = \boldsymbol{\theta}_0 - \boldsymbol{H}^{-1} \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0)$$

Hessian has O(N<sup>2</sup>) elements Inverting takes O(N<sup>3</sup>) N = (Tens or Hundreds of) Millions

#### Q2: Why is this bad for deep learning?

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$$\boldsymbol{\theta}^* = \boldsymbol{\theta}_0 - \boldsymbol{H}^{-1} \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0)$$

- Quasi-Newton methods (BGFS most popular): instead of inverting the Hessian (O(n^3)), approximate inverse Hessian with rank 1 updates over time (O(n^2) each).
- **L-BFGS** (Limited memory BFGS): Does not form/store the full inverse Hessian.

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$$\boldsymbol{\theta}^* = \boldsymbol{\theta}_0 - \boldsymbol{H}^{-1} \nabla_{\boldsymbol{\theta}} J(\boldsymbol{\theta}_0)$$

- Quasi-Newton methods (BGFS most popular): instead of inverting the Hessian (O(n^3)), approximate inverse Hessian with rank 1 updates over time (O(n^2) each).
- **L-BFGS** (Limited memory BFGS): Does not form/store the full inverse Hessian.

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## L-BFGS

- Usually works very well in full batch, deterministic mode i.e. if you have a single, deterministic f(x) then L-BFGS will probably work very nicely
- **Does not transfer very well to mini-batch setting**. Gives bad results. Adapting L-BFGS to large-scale, stochastic setting is an active area of research.

Le et al, "On optimization methods for deep learning, ICML 2011"

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## In practice:

- Adam is a good default choice in most cases
- If you can afford to do full batch updates then try out
   L-BFGS (and don't forget to disable all sources of noise)

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## **Beyond Training Error**



help reduce training loss

But we really care about error on new data - how to reduce the gap?

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## Model Ensembles

- 1. Train multiple independent models
- 2. At test time average their results

## Enjoy 2% extra performance

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## Model Ensembles: Tips and Tricks

Instead of training independent models, use multiple snapshots of a single model during training!



Loshchilov and Hutter, "SGDR: Stochastic gradient descent with restarts", arXiv 2016 Huang et al, "Snapshot ensembles: train 1, get M for free", ICLR 2017 Figures copyright Yixuan Li and Geoff Pleiss, 2017. Reproduced with permission.

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## Model Ensembles: Tips and Tricks

Instead of training independent models, use multiple snapshots of a single model during training!



Loshchilov and Hutter, "SGDR: Stochastic gradient descent with restarts", arXiv 2016 Huang et al, "Snapshot ensembles: train 1, get M for free", ICLR 2017 Figures copyright Yixuan Li and Geoff Pleiss, 2017. Reproduced with permission.



Cyclic learning rate schedules can make this work even better!

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## Model Ensembles: Tips and Tricks

Instead of using actual parameter vector, keep a moving average of the parameter vector and use that at test time (Polyak averaging)



Polyak and Juditsky, "Acceleration of stochastic approximation by averaging", SIAM Journal on Control and Optimization, 1992.

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### How to improve single-model performance?



#### Regularization

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## Regularization: Add term to loss

$$L = rac{1}{N} \sum_{i=1}^{N} \sum_{j 
eq y_i} \max(0, f(x_i; W)_j - f(x_i; W)_{y_i} + 1) + \lambda R(W)$$

# In common use:L2 regularization $R(W) = \sum_k \sum_l W_{k,l}^2$ (Weight decay)L1 regularization $R(W) = \sum_k \sum_l |W_{k,l}|$ Elastic net (L1 + L2) $R(W) = \sum_k \sum_l \beta W_{k,l}^2 + |W_{k,l}|$

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In each forward pass, randomly set some neurons to zero Probability of dropping is a hyperparameter; 0.5 is common





Srivastava et al, "Dropout: A simple way to prevent neural networks from overfitting", JMLR 2014

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p = 0.5 # probability of keeping a unit active. higher = less dropout

```
def train_step(X):
    """ X contains the data """
```

```
# forward pass for example 3-layer neural network
H1 = np.maximum(0, np.dot(W1, X) + b1)
U1 = np.random.rand(*H1.shape)
```

# backward pass: compute gradients... (not shown)
# perform parameter update... (not shown)

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Example forward pass with a 3-layer network using dropout



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How can this possibly be a good idea?



Forces the network to have a redundant representation; Prevents co-adaptation of features



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How can this possibly be a good idea?



Another interpretation:

Dropout is training a large **ensemble** of models (that share parameters).

Each binary mask is one model

An FC layer with 4096 units has  $2^{4096} \sim 10^{1233}$  possible masks! Only ~  $10^{82}$  atoms in the universe...

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Dropout makes our output random!



Want to "average out" the randomness at test-time

$$y = f(x) = E_z \left[ f(x, z) \right] = \int p(z) f(x, z) dz$$

But this integral seems hard ...

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Want to approximate the integral

$$y = f(x) = E_z \left[ f(x, z) \right] = \int p(z) f(x, z) dz$$

Consider a single neuron.



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Want to approximate the integral

$$y = f(x) = E_z [f(x, z)] = \int p(z) f(x, z) dz$$

Consider a single neuron.



At test time we have: 
$$E[a] = w_1 x + w_2 y_3$$

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Want to approximate the integral

$$y = f(x) = E_z [f(x, z)] = \int p(z) f(x, z) dz$$

Consider a single neuron.



At test time we have:  $E[a] = w_1 x + w_2 y$ During training we have:  $E[a] = \frac{1}{4}(w_1 x + w_2 y) + \frac{1}{4}(w_1 x + 0y) + \frac{1}{4}(0x + w_2 y) + \frac{1}{4}(0x + w_2 y) = \frac{1}{2}(w_1 x + w_2 y)$ 

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Want to approximate the integral

$$y = f(x) = E_z \left[ f(x, z) \right] = \int p(z) f(x, z) dz$$

Consider a single neuron.



At test time we have:  $E[a] = w_1 x + w_2 y$ During training we have:  $E[a] = \frac{1}{4}(w_1 x + w_2 y) + \frac{1}{4}(w_1 x + 0y)$ At test time, **multiply** by dropout probability  $E[a] = \frac{1}{4}(w_1 x + w_2 y) + \frac{1}{4}(w_1 x + 0y)$  $+ \frac{1}{4}(0x + 0y) + \frac{1}{4}(0x + w_2 y)$ 

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```
def predict(X):
```

```
# ensembled forward pass
H1 = np.maximum(0, np.dot(W1, X) + b1) * p # NOTE: scale the activations
H2 = np.maximum(0, np.dot(W2, H1) + b2) * p # NOTE: scale the activations
out = np.dot(W3, H2) + b3
```

At test time all neurons are active always => We must scale the activations so that for each neuron: <u>output at test time</u> = <u>expected output at training time</u>

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""" Vanilla Dropout: Not recommended implementation (see notes below) """

**p** = 0.5 # probability of keeping a unit active. higher = less dropout



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**Dropout Summary** 

## More common: "Inverted dropout"

p = 0.5 # probability of keeping a unit active. higher = less dropout



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## Regularization: A common pattern

**Training**: Add some kind of randomness

$$y = f_W(x, z)$$

**Testing:** Average out randomness (sometimes approximate)

$$y = f(x) = E_z \left[ f(x, z) \right] = \int p(z) f(x, z) dz$$

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# Regularization: A common pattern

# **Training**: Add some kind of randomness

$$y = f_W(x, z)$$

**Testing:** Average out randomness (sometimes approximate)

$$y = f(x) = E_z [f(x, z)] = \int p(z)f(x, z)dz$$

**Example**: Batch Normalization

### **Training**: Normalize using stats from random minibatches

**Testing**: Use fixed stats to normalize

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# **Regularization: Data Augmentation**



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# **Regularization: Data Augmentation**



Transform image

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## Data Augmentation Horizontal Flips





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## Data Augmentation Random crops and scales

**Training**: sample random crops / scales ResNet:

- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch



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## Data Augmentation Random crops and scales

**Training**: sample random crops / scales ResNet:

- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch



# **Testing**: average a fixed set of crops ResNet:

- 1. Resize image at 5 scales: {224, 256, 384, 480, 640}
- 2. For each size, use 10 224 x 224 crops: 4 corners + center, + flips

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## Data Augmentation Color Jitter

Simple: Randomize contrast and brightness



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# Data Augmentation Color Jitter

Simple: Randomize contrast and brightness



### More Complex:

- 1. Apply PCA to all [R, G, B] pixels in training set
- 2. Sample a "color offset" along principal component directions
- 3. Add offset to all pixels of a training image

(As seen in [Krizhevsky et al. 2012], ResNet, etc)

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# Data Augmentation

Get creative for your problem!

## Random mix/combinations of :

- translation
- rotation
- stretching
- shearing,
- lens distortions, ... (go crazy)

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# Regularization: A common pattern

**Training**: Add random noise **Testing**: Marginalize over the noise

## Examples:

- Dropout
- **Batch Normalization**
- Data Augmentation

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## Regularization: A common pattern Training: Add random noise

Testing: Marginalize over the noise

### Examples:

Dropout Batch Normalization Data Augmentation DropConnect





Wan et al, "Regularization of Neural Networks using DropConnect", ICML 2013

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# Regularization: A common pattern

**Training**: Add random noise **Testing**: Marginalize over the noise

## Examples:

Dropout

Batch Normalization

Data Augmentation DropConnect Fractional Max Pooling



Graham, "Fractional Max Pooling", arXiv 2014

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# Regularization: A common pattern

**Training**: Add random noise **Testing**: Marginalize over the noise

### Examples:

Dropout

**Batch Normalization** 

Data Augmentation DropConnect

Fractional Max Pooling Stochastic Depth

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Huang et al, "Deep Networks with Stochastic Depth", ECCV 2016

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# **Transfer Learning**

# "You need a lot of a data if you want to train/use CNNs"

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### Transfer Learning with CNNs

1. Train on Imagenet

FC-1000
FC-4096
FC-4096
MaxPool
Conv-512
Conv-512
MaxPool
Conv-512
Conv-512
MaxPool
Maxi ool
Conv-256
Conv-256
MaxPool
Conv-128
Conv-128
MaxPool
Conv-64
Conv-64
Image

Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014

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### Transfer Learning with CNNs

1. Train on Imagenet

FC-1000	
FC-4096	
FC-4096	
MaxPool	
Conv-512	
Conv-512	
MaxPool	
Conv-512	
Conv-512	
MaxPool	
Conv-256	
Conv-256	
MaxPool	
Conv-128	
Conv-128	
MaxPool	
Conv-64	
Conv-64	

Image

2. Small Dataset (C classes)



Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014

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## Transfer Learning with CNNs

1. Train on Imagenet

FC-1000	
FC-4096	
FC-4096	
MaxPool	
Conv-512	
Conv-512	
MaxPool	
Conv-512	
Conv-512	
MaxPool	
Conv-256	
Conv-256 Conv-256	
Conv-256 Conv-256 MaxPool	
Conv-256 Conv-256 MaxPool Conv-128	
Conv-256 Conv-256 MaxPool Conv-128 Conv-128	
Conv-256 Conv-256 MaxPool Conv-128 Conv-128 MaxPool	
Conv-256 Conv-256 MaxPool Conv-128 Conv-128 MaxPool Conv-64	

Image

2. Small Dataset (C classes)



Donahue et al, "DeCAF: A Deep Convolutional Activation Feature for Generic Visual Recognition", ICML 2014 Razavian et al, "CNN Features Off-the-Shelf: An Astounding Baseline for Recognition", CVPR Workshops 2014



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FC-1000 FC-4096 FC-4096 MaxPool		very similar dataset	very different dataset
Conv-512 MaxPool Conv-512 Conv-512 Conv-512	very little data	?	?
MaxPool Conv-256 Conv-256 MaxPool Conv 128			
Conv-128 MaxPool Conv-64 Conv-64	quite a lot of data	?	?

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FC-1000 FC-4096 FC-4096 MaxPool		very similar dataset	very different dataset
Conv-512MaxPoolMore specificConv-512More specificConv-512MaxPoolConv-256Conv-256Conv-256More genericMaxPoolMaxPool	very little data	Use Linear Classifier on top layer	?
Conv-128 Conv-128 MaxPool Conv-64 Conv-64 Image	quite a lot of data	Finetune a few layers	?

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FC-1000 FC-4096 FC-4096 MaxPool		very similar dataset	very different dataset
Conv-512MaxPoolMore specificConv-512More specificMaxPoolMore genericMaxPoolMore genericMaxPoolMore generic	very little data	Use Linear Classifier on top layer	You're in trouble Try linear classifier from different stages
Conv-128 Conv-128 MaxPool Conv-64 Conv-64 Image	quite a lot of data	Finetune a few layers	Finetune a larger number of layers

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# Transfer learning with CNNs is pervasive... (it's the norm, not an exception)



#### Image Captioning: CNN + RNN



#### Karpathy and Fei-Fei, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015 Figure copyright IEEE, 2015. Reproduced for educational purposes.

Girshick, "Fast R-CNN", ICCV 2015 Figure copyright Ross Girshick, 2015. Reproduced with permission.

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# Transfer learning with CNNs is pervasive... (it's the norm, not an exception)



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# Transfer learning with CNNs is pervasive... (it's the norm, not an exception)



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## Takeaway for your projects and beyond:

Have some dataset of interest but it has < ~1M images?

- 1. Find a very large dataset that has similar data, train a big ConvNet there
- 2. Transfer learn to your dataset

Deep learning frameworks provide a "Model Zoo" of pretrained models so you don't need to train your own

Caffe: <u>https://github.com/BVLC/caffe/wiki/Model-Zoo</u> TensorFlow: <u>https://github.com/tensorflow/models</u> PyTorch: <u>https://github.com/pytorch/vision</u>

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# Summary

- Optimization
  - Momentum, RMSProp, Adam, etc
- Regularization
  - Dropout, etc
- Transfer learning
  - Use this for your projects!

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# Next time: Deep Learning Software!

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